

Mechatronics

VAM

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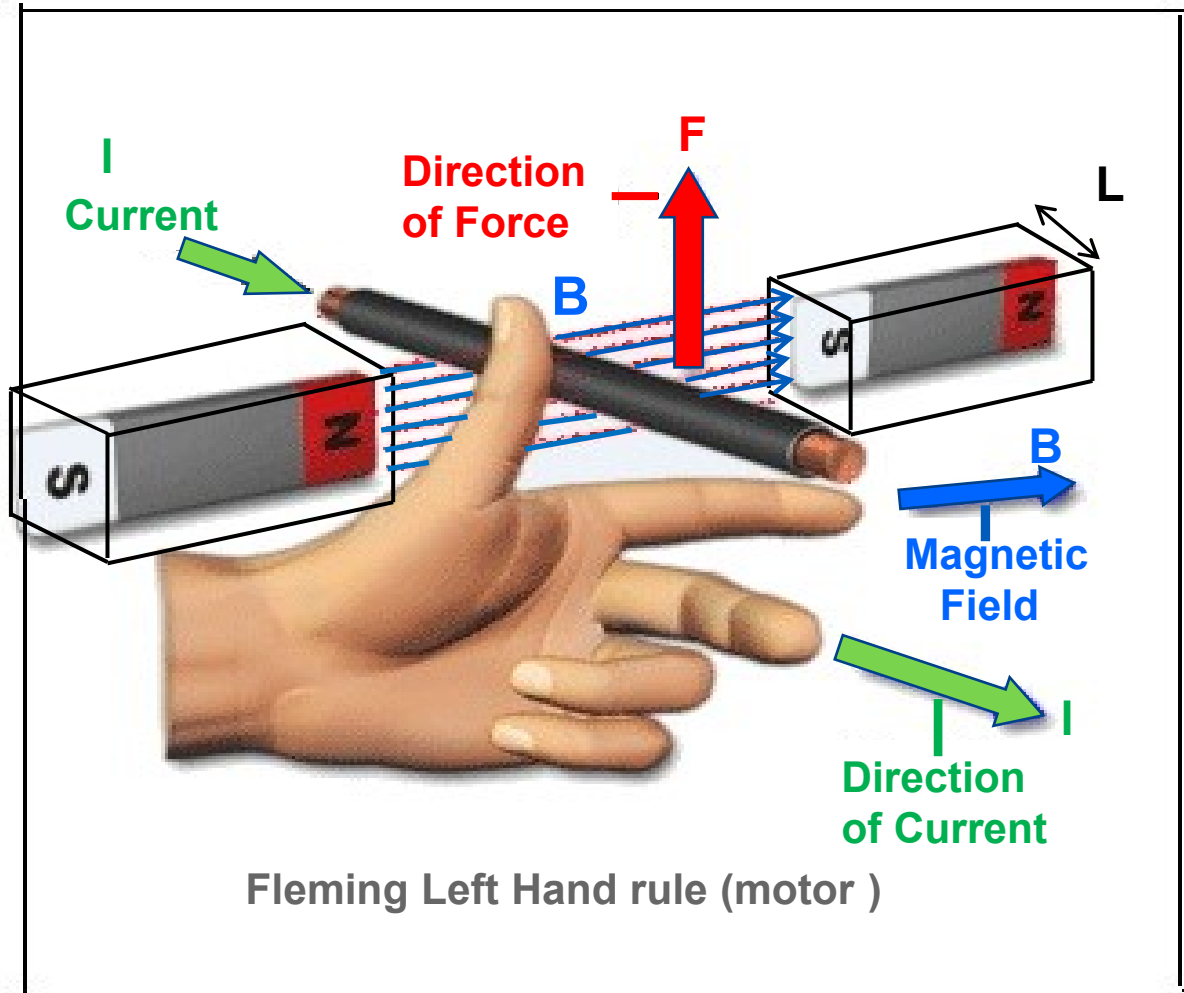
82-(0)10-3582-7056

Jan. 23 2020

Goal of this lecture

- **Understand magnetic field and magnetic circuit**
- **DC and AC system**
- **Classification of motors**
- **Fundamental principle of DC motor and AC motors**

Force in motor



$$F \text{ motor (force : N)} = B * I * L$$

B: magnetic flux density T(Tesla)

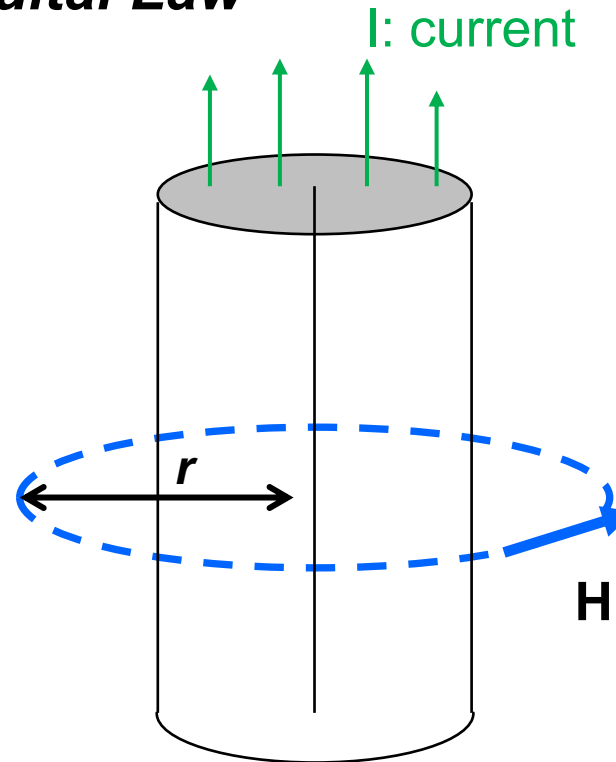
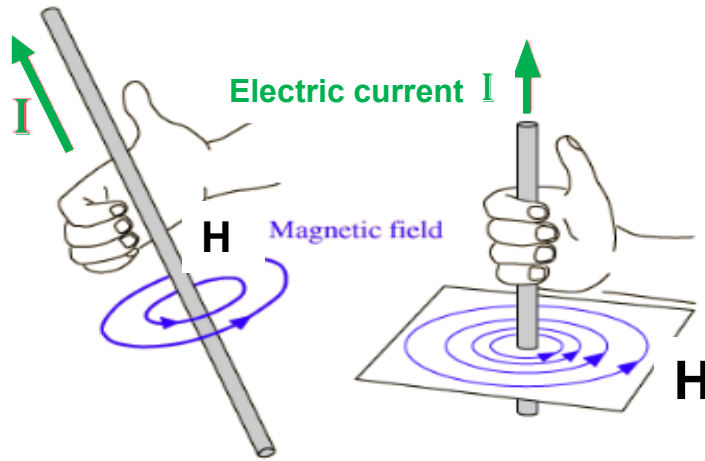
I : current A (Amper)

L: length of conductor (wire) in B (meter)

Magnetic field

- Magnetic field H (A/m) has nothing to do with materials

Right-Hand Rule: Ampere's Circuital Law



$$\oint \vec{H} \cdot d\vec{l} = I$$

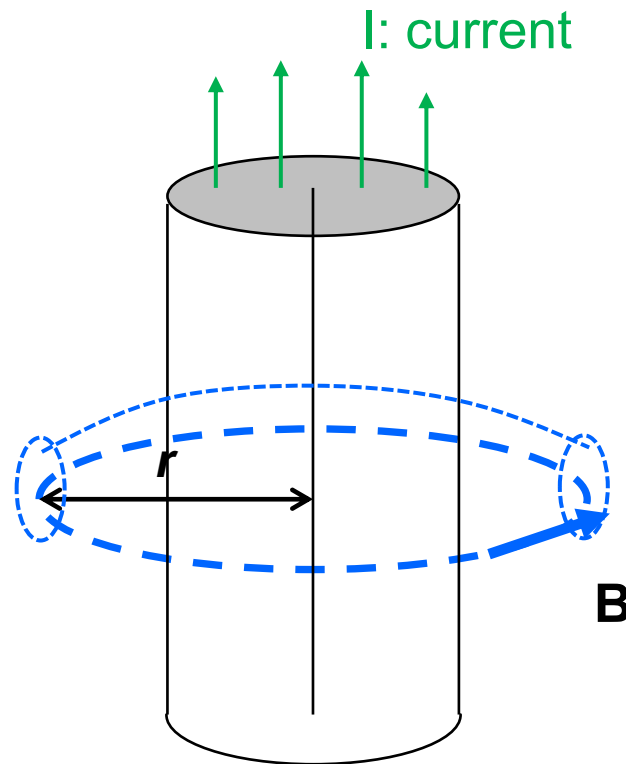
$$2\pi r H = I$$

$$H = \frac{I}{2\pi r}$$

Magnetic flux and Magnetic flux density

- Magnetic flux F (Wb: Weber) and Magnetic flux density B (T: Tesla Wb/m^2)

If material in green line is air/vacuum or steel,
Magnetic flux (magnetic flux density) is changing



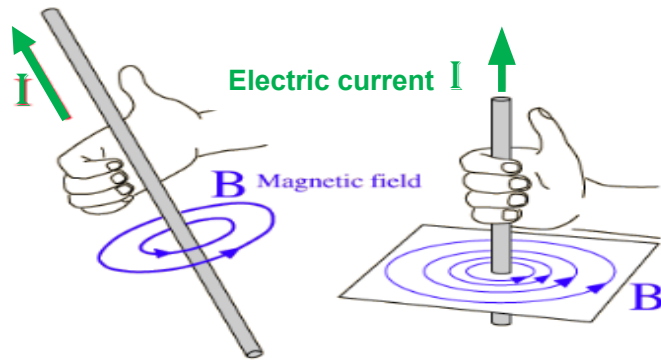
$$B = \mu_0 \text{ (air permeability)} * \mu_r \text{ (relative permeability of material)} * H$$

$$B_{\text{(in air)}} = \frac{I}{2\pi r} * \mu_0 \text{ (air permeability)}$$

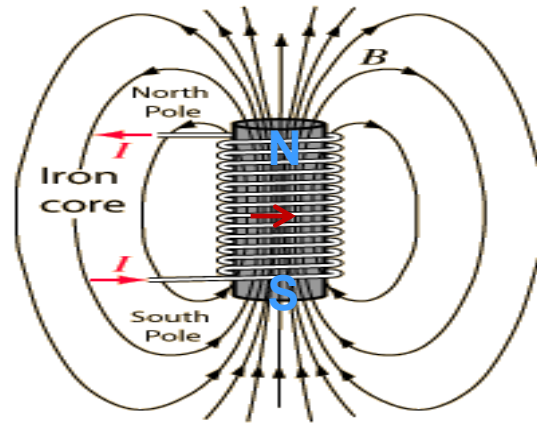
$$B_{\text{(in steel)}} = \frac{I}{2\pi r} * \mu_0 \text{ (air permeability)} * \mu_r \text{ (relative permeability of steel)}$$

Magnetic field

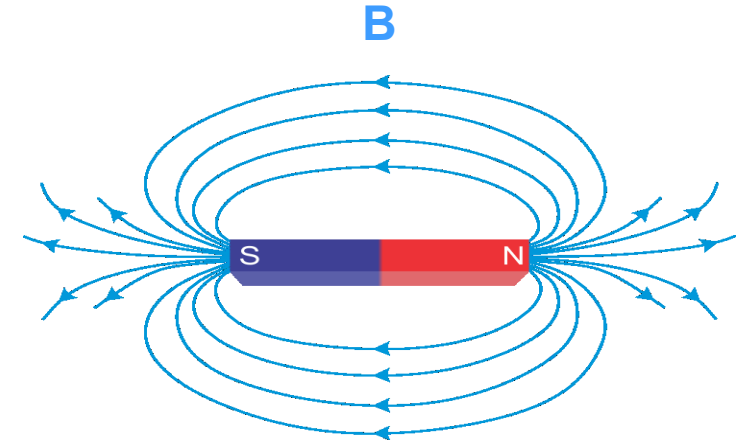
- Magnetic field H (A/m) Magnetic flux density B (Tesla)
 - Produced by electric current or magnets
 - Direction of the magnetic field is perpendicular to the wire (Right-Hand Rule: Ampere's Circuital Law)



wire(coil)



wire(coil)+steel



permanent magnets

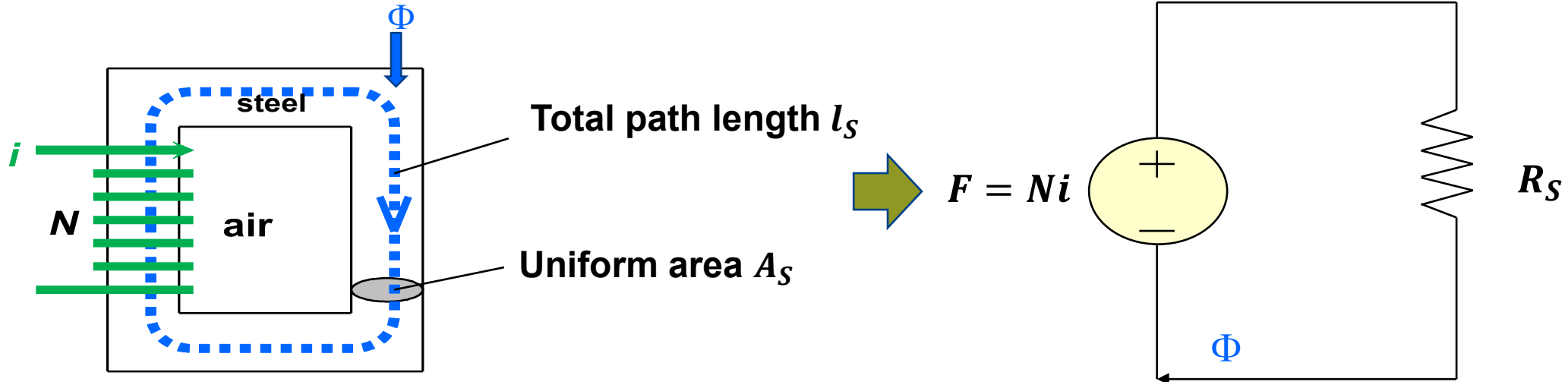
http://www.whatisamagneticfield.com/magnetic_field_generation.html

<https://www.quora.com/Can-we-create-a-magnet-by-placing-a-metal-in-an-electric-field>

<https://www.topperlearning.com/answer/a-what-are-magnetic-field-lines-how-is-the-direction-of-a-magnetic-field-at-a-point-determined-b-draw-field-lines-around-a-bar-magnet-along-its-length/br9v335nn>

Magnetic field

- Magnetic flux density B with iron core(steel)



$$R_s = (\text{magnetic resistance in steel}) = \frac{l_s}{\mu_s A_s}$$

μ_s (Magnetic permeability)

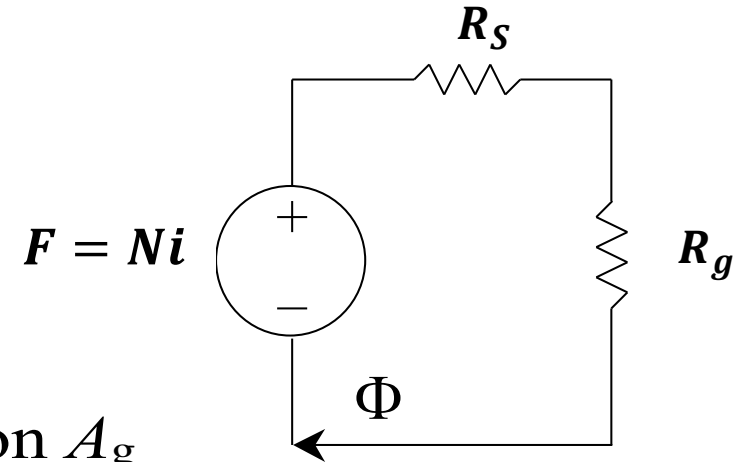
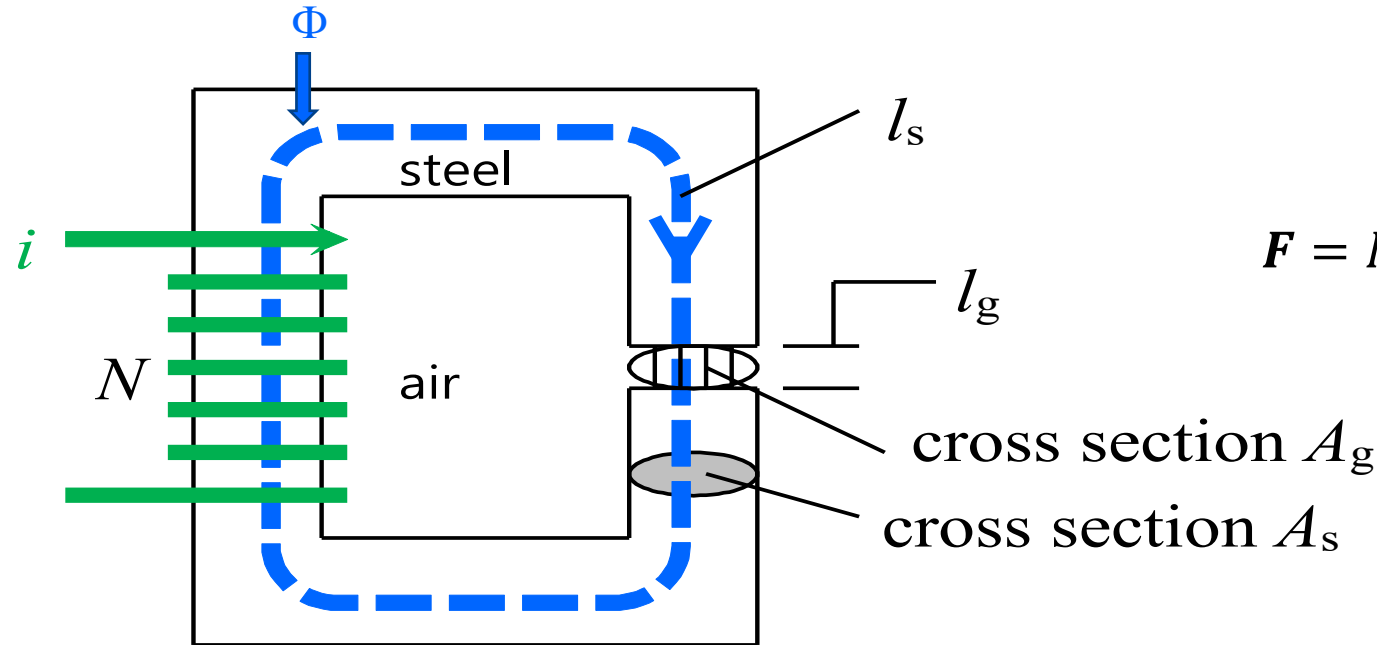
= μ_0 (air permeability) * μ_r (relative permeability)

$$F = Ni = R_s * \Phi$$

$$\Phi \text{ (Magnetic flux)} = F / R_s \Rightarrow \Phi = \frac{Ni}{\left[\frac{l_s}{\mu_s A_s} \right]} \Rightarrow B = \frac{\Phi}{A_s} = \frac{\mu_s Ni}{l_s}$$

Magnetic field

- **Magnetic flux density B** with iron core(steel) and air gap



R_g (magnetic resistance in air -gap)

$$F = Ni = (R_s + R_g) * \Phi$$

$$Ni = \Phi \left(\frac{l_s}{\mu_s A_s} + \frac{l_g}{\mu_o A_g} \right)$$

Permeability of steel is much greater than that of air in the gap

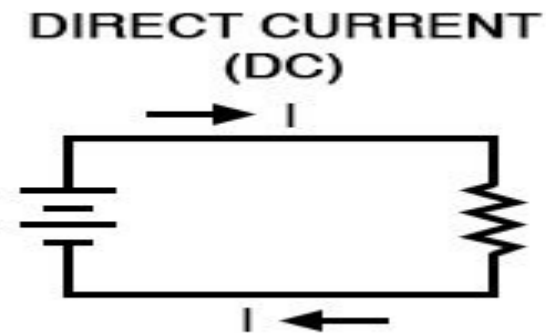
$$Ni \approx \Phi \frac{l_g}{\mu_o A_g}$$

$$\Phi \approx \frac{Ni \mu_o A_g}{l_g}$$

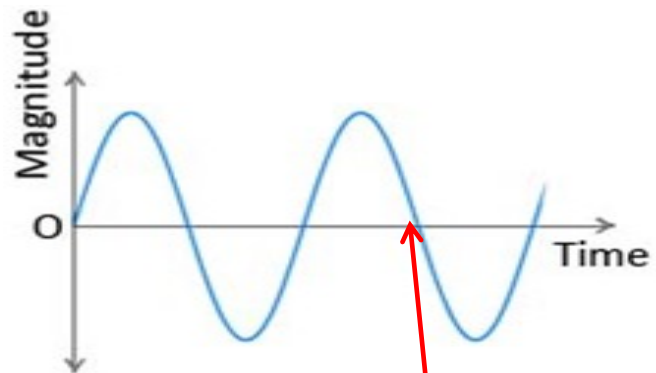
$$B = \frac{\Phi}{A_g} = \frac{\mu_o Ni}{l_g}$$

DC and AC system

- DC

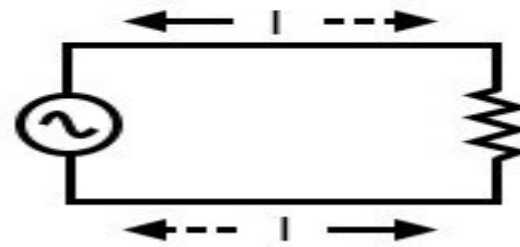


- AC



If 60 Hz, 0.0166 sec

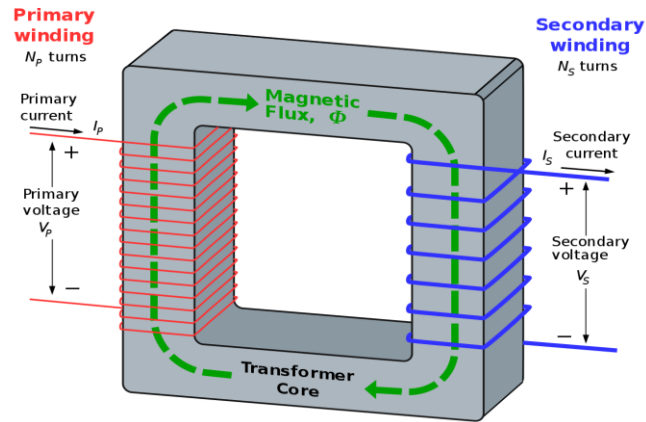
ALTERNATING CURRENT (AC)



DC and AC system

- AC: transformer

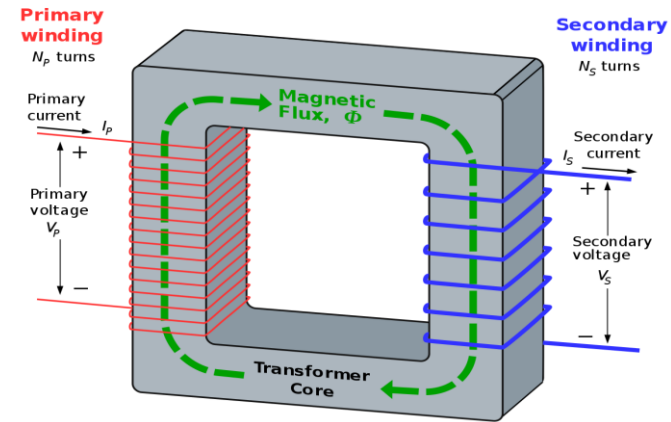
$N_p=10$
 100 V
 10 A
 1000 W



$N_s=5$
 50 V
 20 A
 1000 W

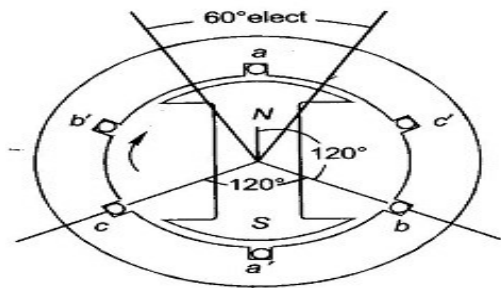
$N_p=10$
 100 V
 10 A
 1000 W

Phase 1

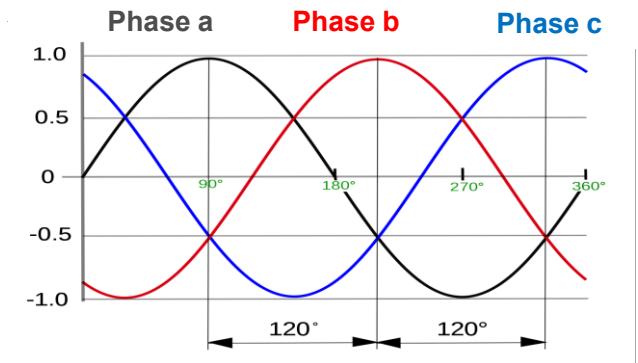
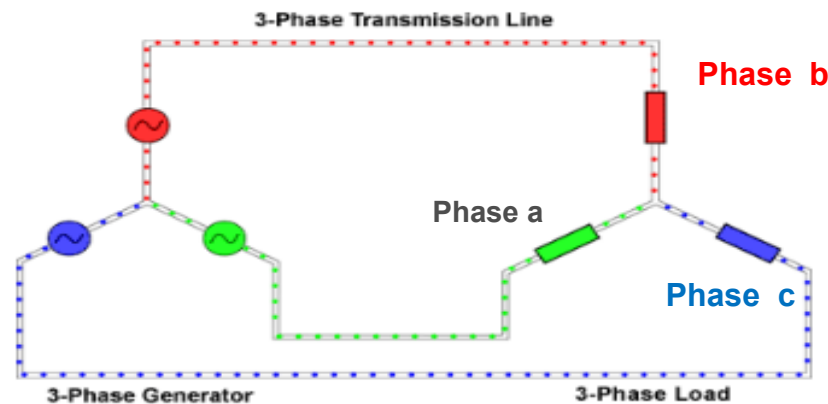


$N_s=20$
 200 V
 5 A
 1000 W

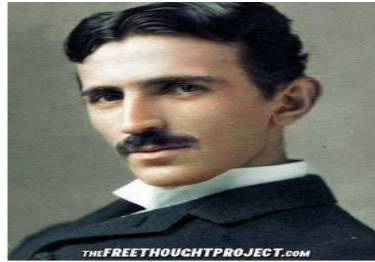
- AC: three-phase electric power (page 115, 116)



three-phase generator

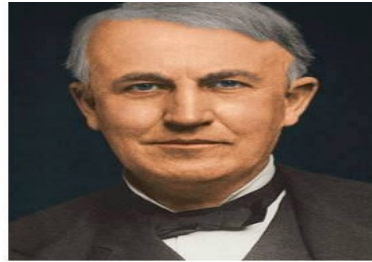


DC and AC system



NIKOLA TESLA

Inventor that created renewable energy and cared more about people than making money.



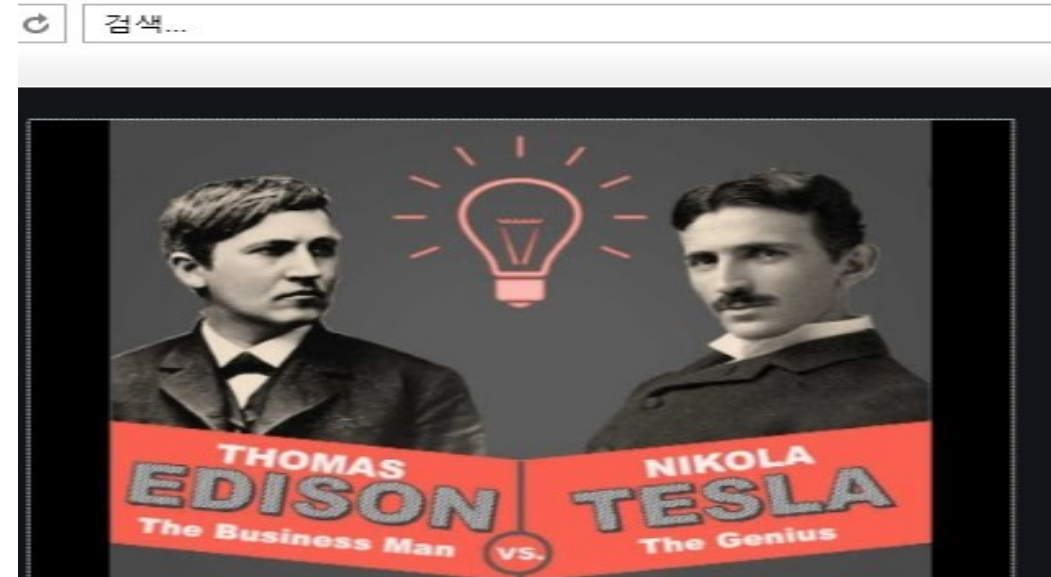
THOMAS EDISON

Wealthy businessman who created a way to charge money for electricity and methods to control energy resources.

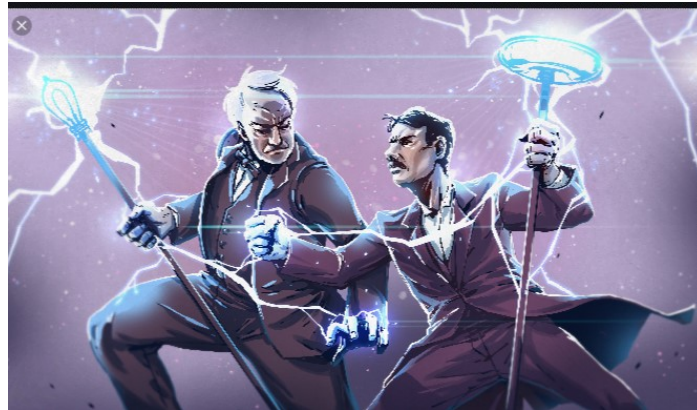
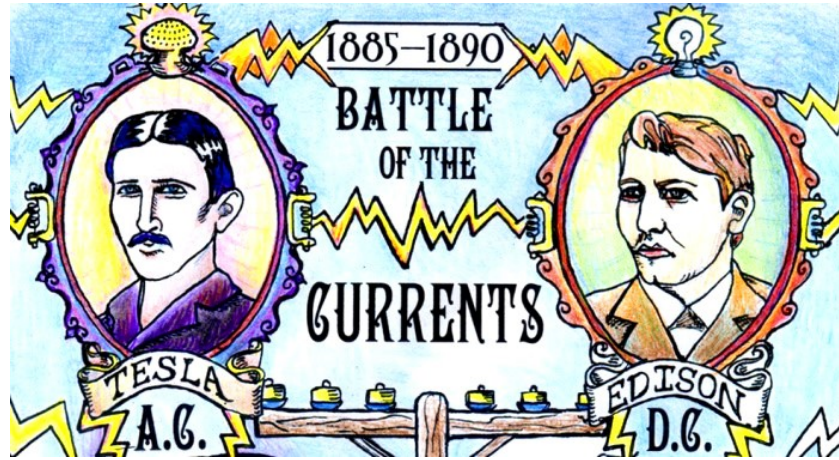
GUESS WHICH ONE YOUR TEXTBOOKS NEVER TOLD YOU ABOUT.



Tomorrow is Thomas Edison's birthday. Let's steal his day, like he did Tesla's inventions and celebrate Nikola Tesla with memes instead!

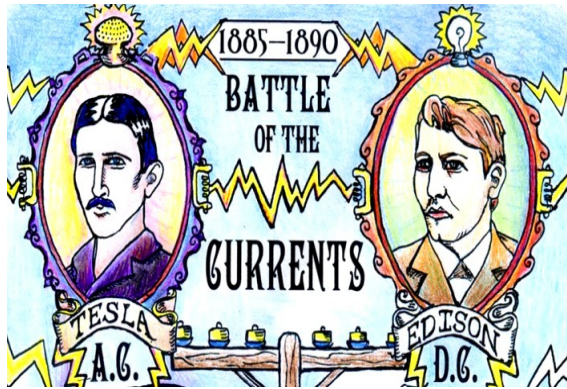


DC and AC system



<https://www.youtube.com/watch?v=5UYF23C2Hew>

DC and AC system



In 1888



Tesla
(Westinghouse)



Edison
(General Electric)



1st match in 1893



Tesla : winner



2nd match in 1895
first AC power plants
at Niagara Falls



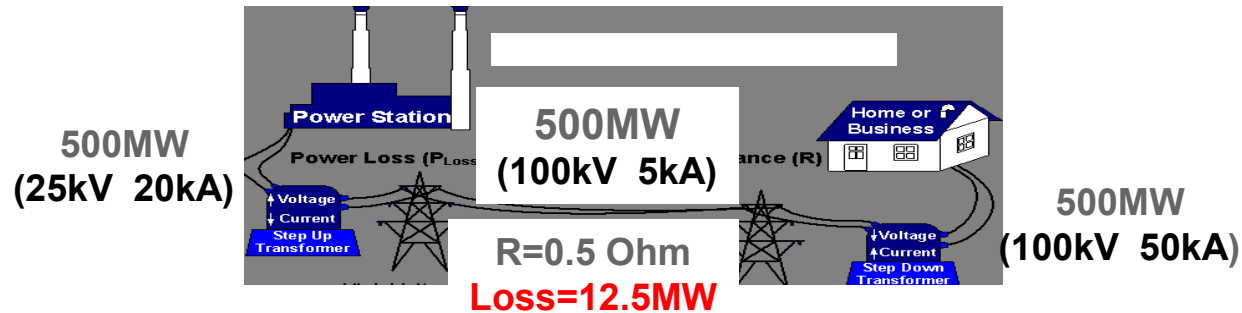
Tesla : winner

DC and AC system

- Step up transformer : higher voltage

Power line resistance: 0.5 Ohm

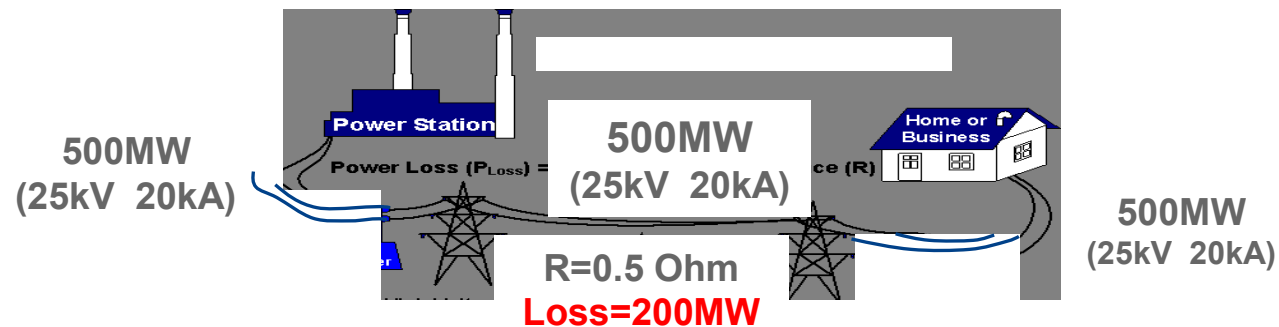
Power line resistance loss: $5000 \times 5000 \times 0.5 \text{ Ohm} = 12.5 \text{ MW}$ (2.5% of power: $12.5 \text{ MW} / 500 \text{ MW}$)



- Without step up transformer : lower voltage

Power line resistance: 0.5 Ohm

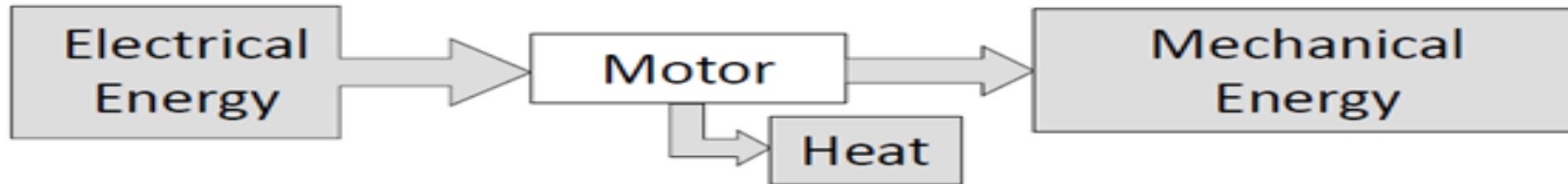
Power line resistance loss: $20000 \times 20000 \times 0.5 \text{ Ohm} = 200 \text{ MW}$ (40% of power: $200 \text{ MW} / 500 \text{ MW}$)



http://www.cmm.gov.mo/eng/exhibition/secondfloor/MoreInfo/2_4_3_HighVoltage.html

Classification of motors

- Electric Motor converts elec. energy into mechanical energy



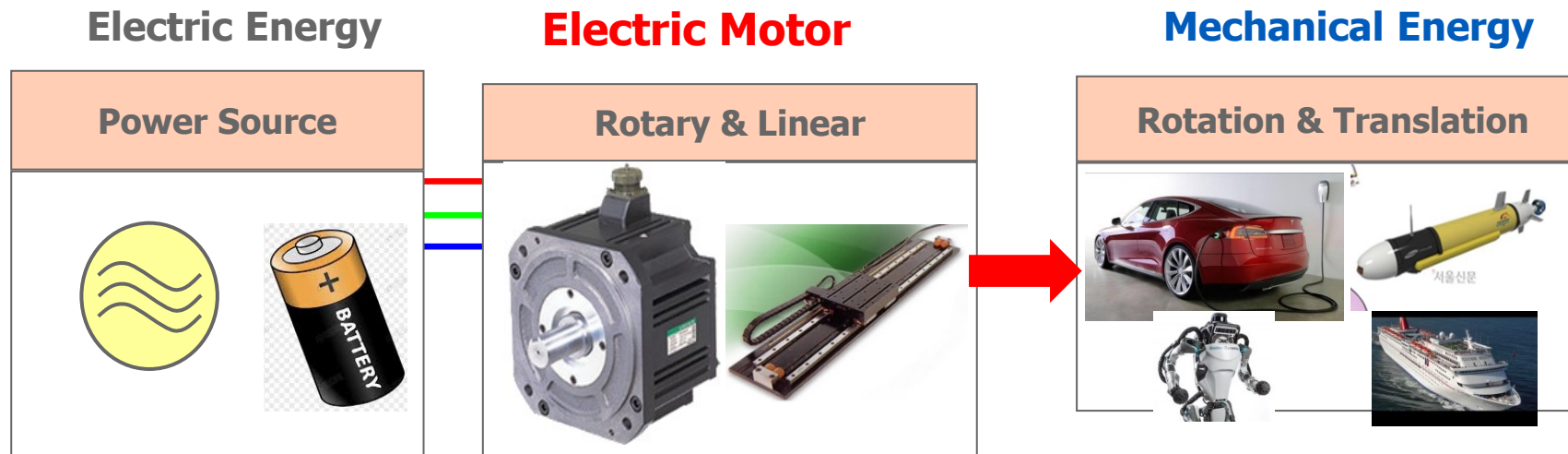
Energy conversion in electric motors is most commonly based on ***electromagnetism***. AC motors rely on *alternating current* to establish the desired magnetic fields, while DC motors use *direct current*.

Electrical Energy In > Mechanical Energy Out

Efficiency = output mechanical energy / input electrical energy

Classification of motors

- Electrical Motor Technical Requirements



- ✓ **High Efficiency (out-put/in-put) : Loss Reduction**
 - save energy and battery
 - Battery for EV 30,000 US\$ VS motor for EV 3,000 US\$
 - motor 5% efficiency up → save battery 1,500 US\$
- ✓ **High Power Density(power/weight):Weight Reduction**
 - compact system and save energy
- ✓ **High Accuracy(nano-micro meter accuracy) : Precision**

Classification of motors

- AC/DC Motor

Force in motor: Fleming's left hand rule

$$F = B * I * L$$

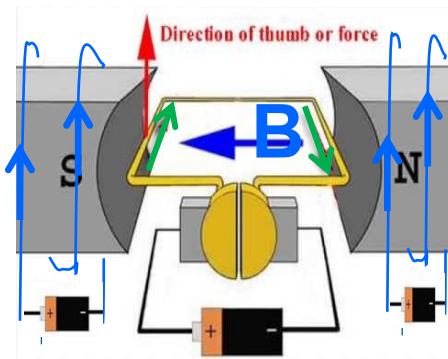
B: magnetic flux density

I: Current direction in coil

L: Coil length

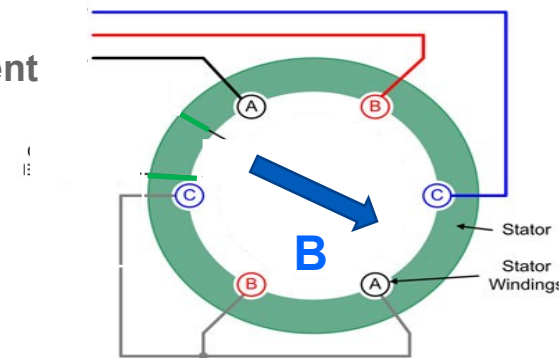
DC motor: **B magnetic flux** by DC current or permanent magnet

AC motor: **B magnetic flux** by AC current (**page 117**)



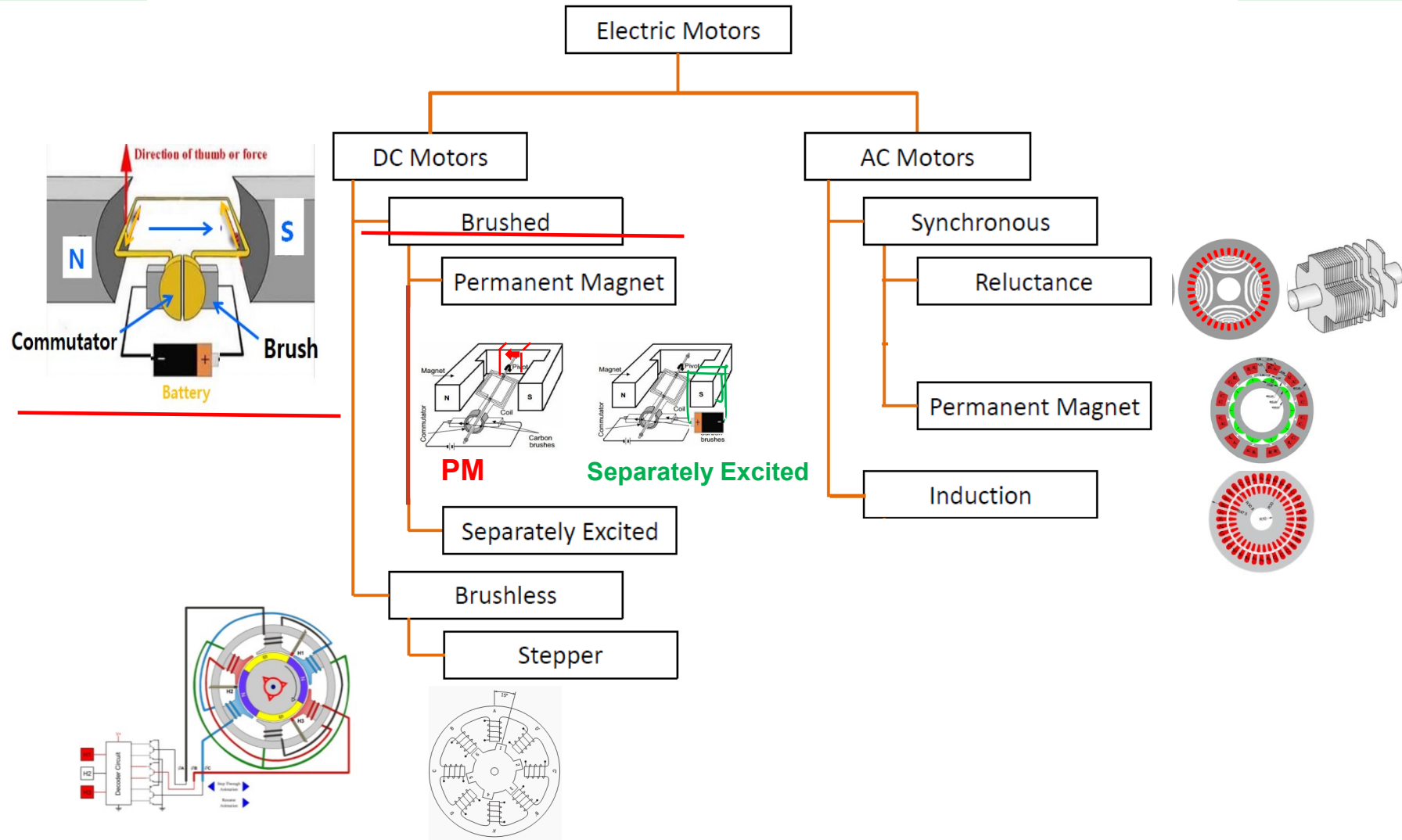
DC motor: **B magnetic flux**

3- phase
AC current

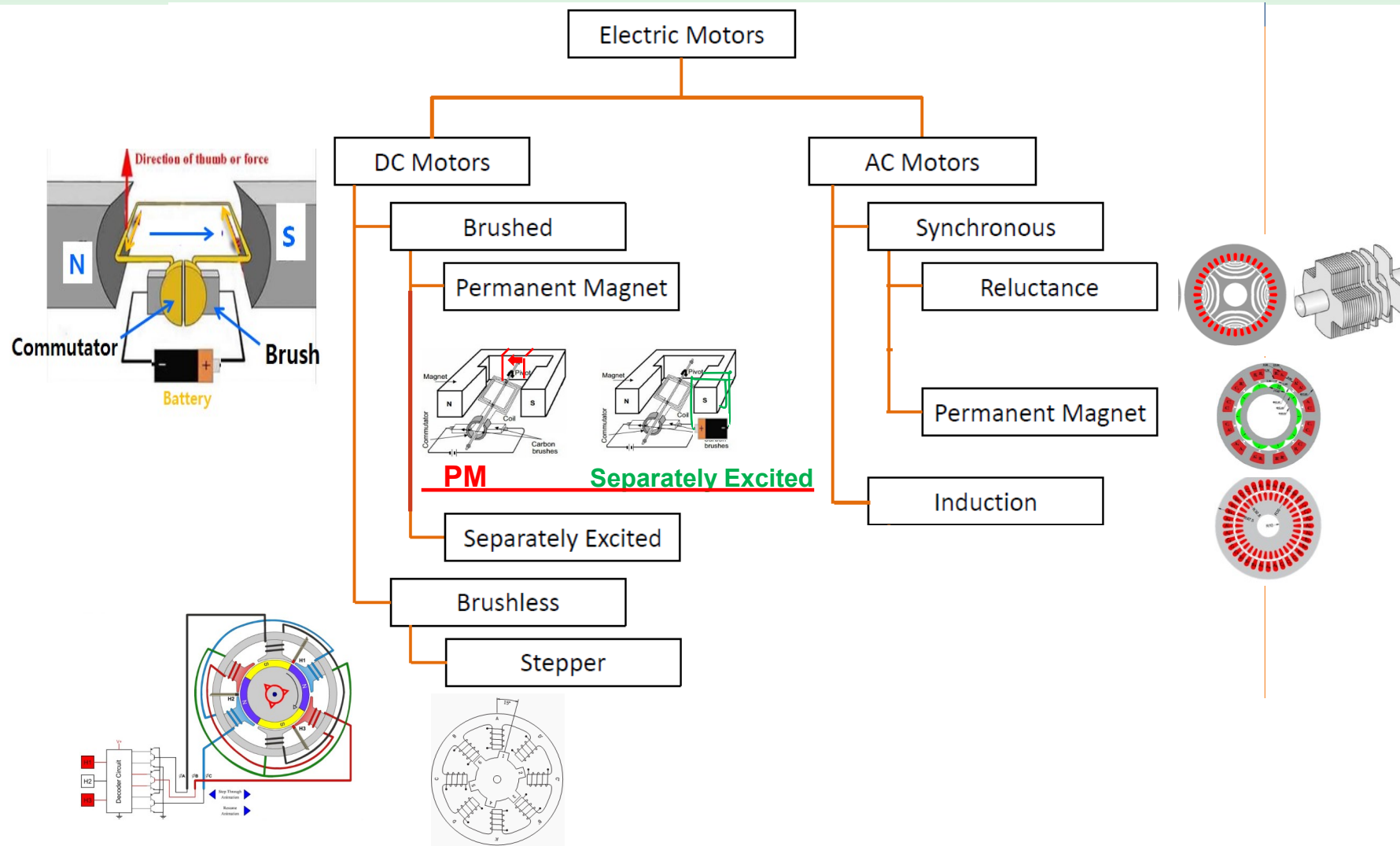


AC motor: **B magnetic flux**

Classification of motors

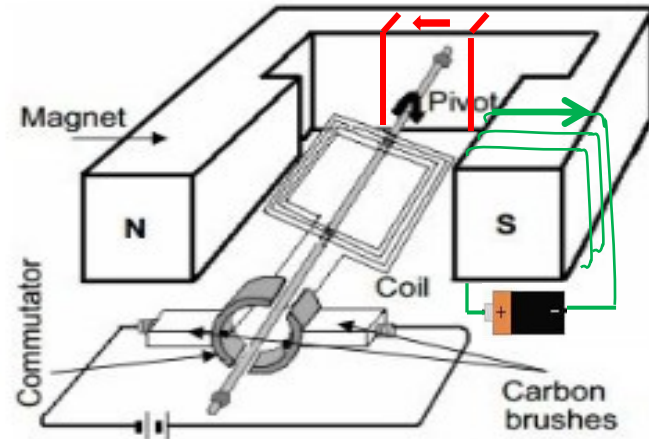


Classification of motors



Classification of motors

- permanent magnet(no power) or
- Separately Excited: electric magnet



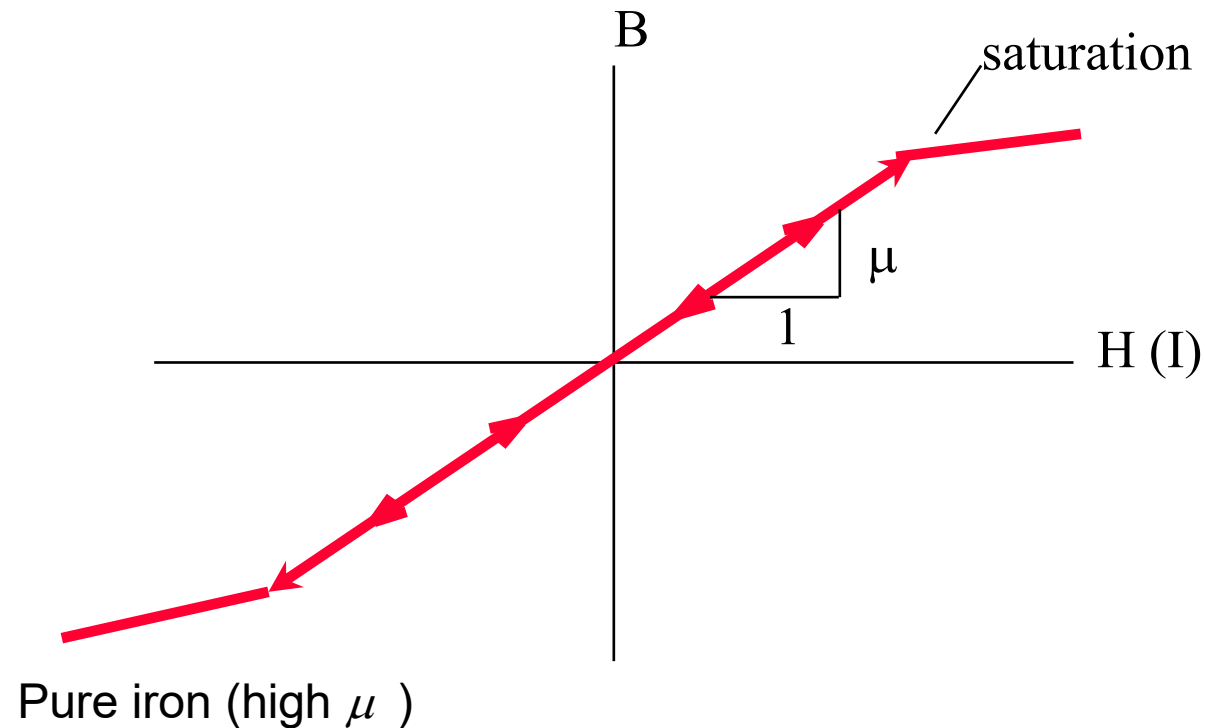
If permanent magnet is magnetized by pulse current,
PM can have magnetic flux without any thing.

But PM can be demagnetized by high temperature and high reverse magnetic flux.

https://www.google.co.kr/search?tbm=isch&q=dc+motor+principle&chips=q:dc+motor+principle,online_chips:generator,online_chips:magnetic&a=X&ved=0ahUKEwjd-t_3gY7kAhXDJaYKHfrUACMQ4IYIMygJ&biw=2163&bih=1049&dpr=0.8#imgrc=0mLQjwqmlPudsM:&spf=1566186140824

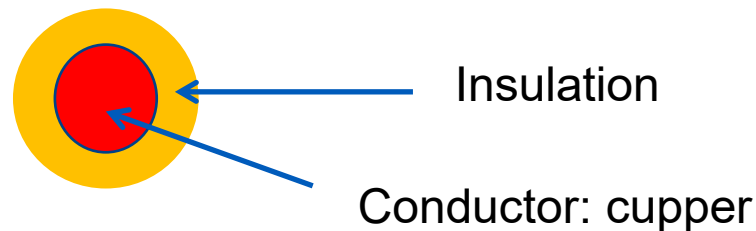
Classification of motors

- Limit of motor force in coil : $F=B*I*L$
 - B magnetic flux density in motor: 1.5(Tesla) because of saturation



Classification of motors

- Limit of motor force in coil : $F = B * I * L$
 - **I Current:** is limited by copper loss (heat)
current density in coil is 4-10 A/mm²
 - Max current density in coil depends on cooling system
 - Water and oil cooling system up to 10-20 A/mm²
 - The electric current density is measured in amperes per square meter



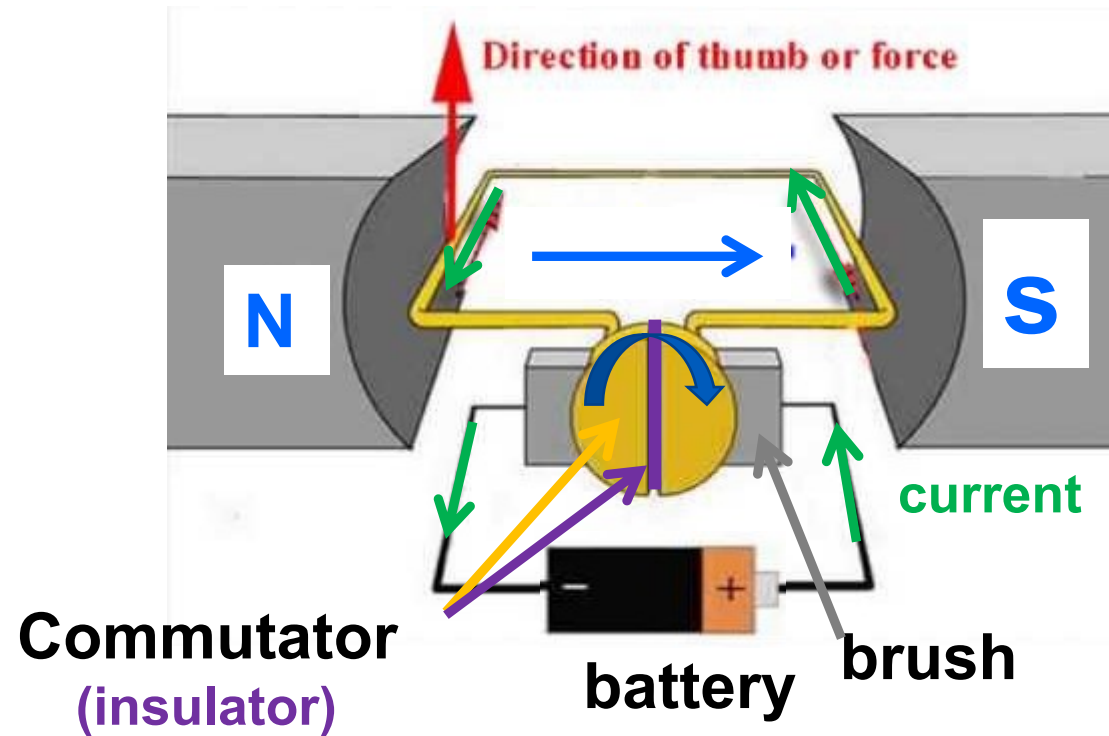
The current density = current in conductor / conductor area

DC motor working principle from Fleming's left hand rule

-B magnetic field : from N to S

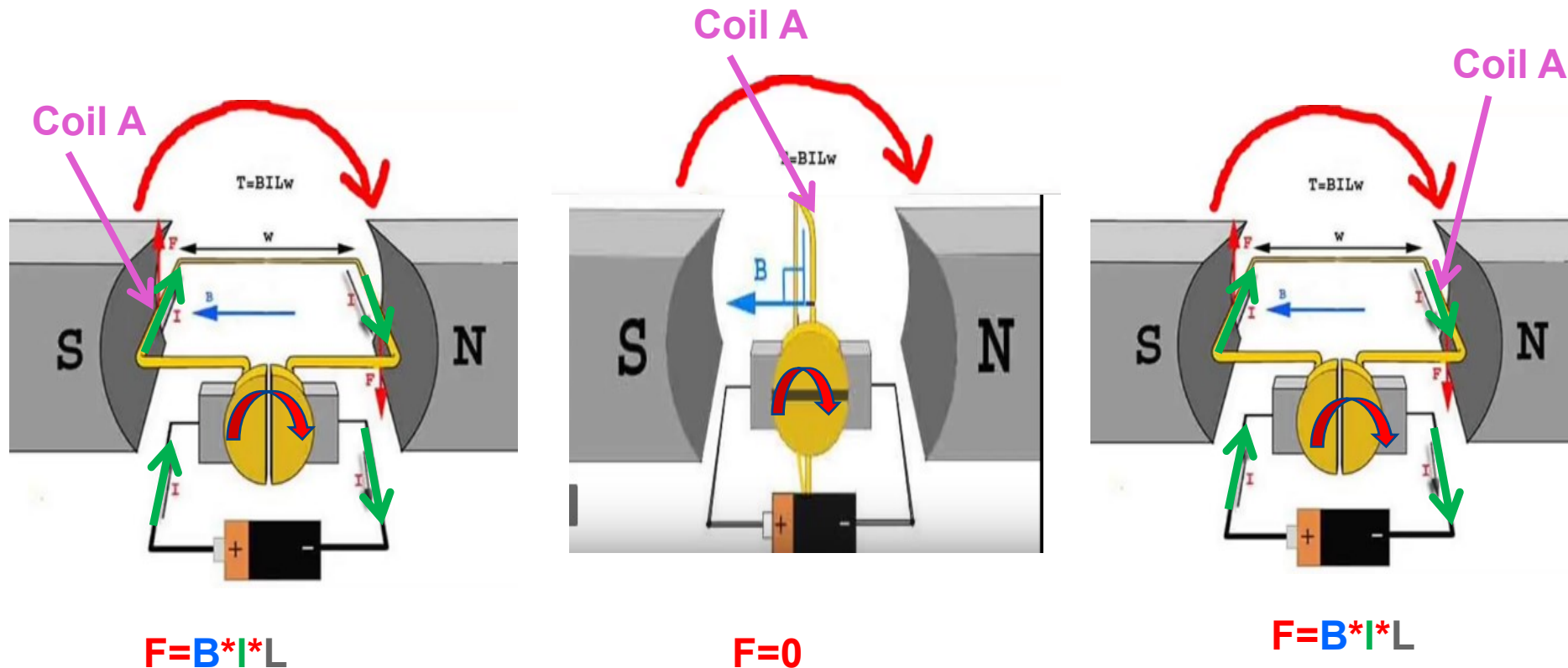
-I current direction in coil:

from battery +, brush, commutator, coil, commutator, brush to battery –



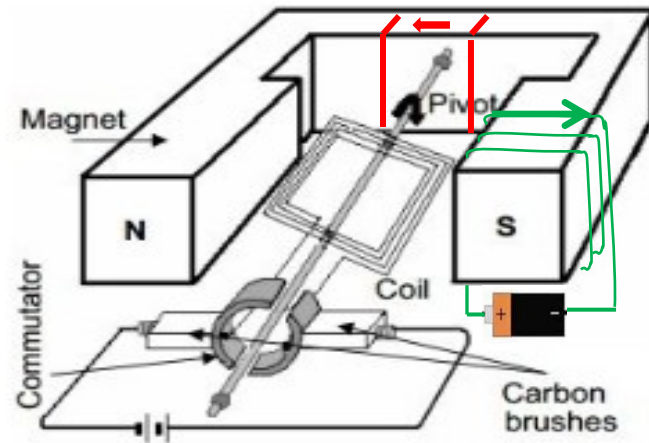
DC motor working principle from Fleming's left hand rule

- Function of commutator and brush



DC motor working principle from Fleming's left hand rule

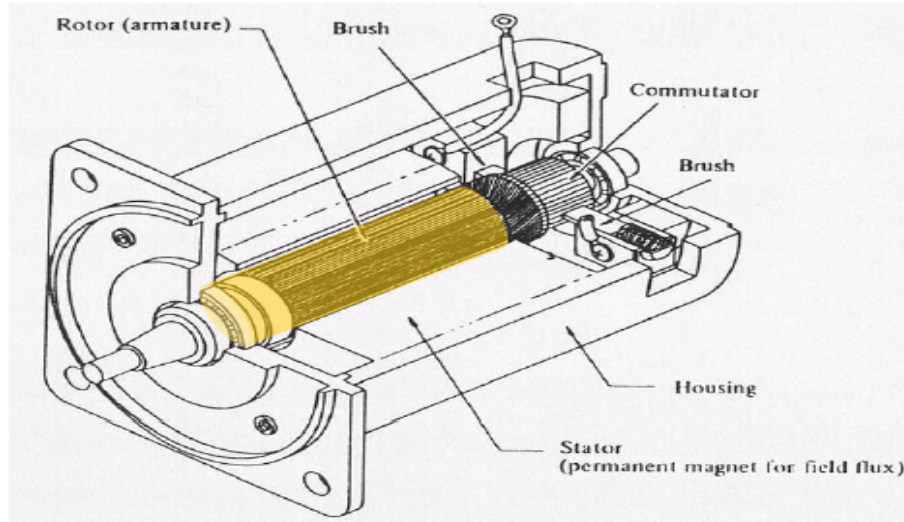
- How to make **B** magnetic field
 - **permanent magnet** or **electric magnet**



https://www.google.co.kr/search?tbm=isch&q=dc+motor+principle&chips=q:dc+motor+principle,online_chips:generator,online_chips:magnetic&sa=X&ved=0ahUKEwjd-t_3gY7kAhXDJaYKHfrUACMQ4IYIMygJ&biw=2163&bih=1049&dpr=0.8#imgrc=0mLQjwqmIPudsM:&spf=1566186140824

DC motor working principle from Fleming's left hand rule

● Rotor: mechanical terms



Motors are actuation devices (actuators) that generate ***torque***.

Mechanical Terms

- **Rotor**: rotating part of the motor.
- **Stator**: stationary part of the motor.
- **Commutator**: part of rotor in contact with the brushes
- **Brushes**: part of electrical circuit through which current is supplied to armature.

DC motor working principle from Fleming's left hand rule

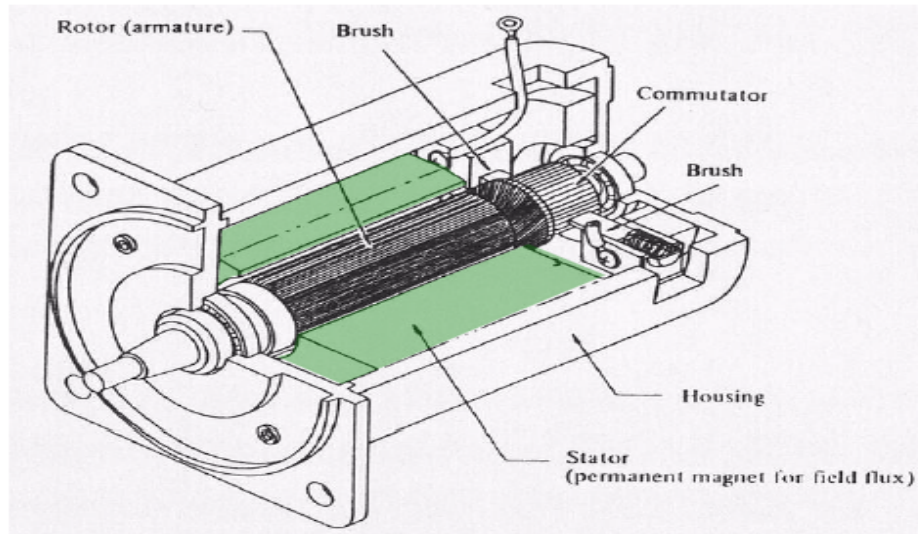
- Rotor: mechanical terms



Image: https://en.wikipedia.org/wiki/File:Electric_Motor_Rotor.jpg
<http://motorcorechina.com>

DC motor working principle from Fleming's left hand rule

● Stator : mechanical terms



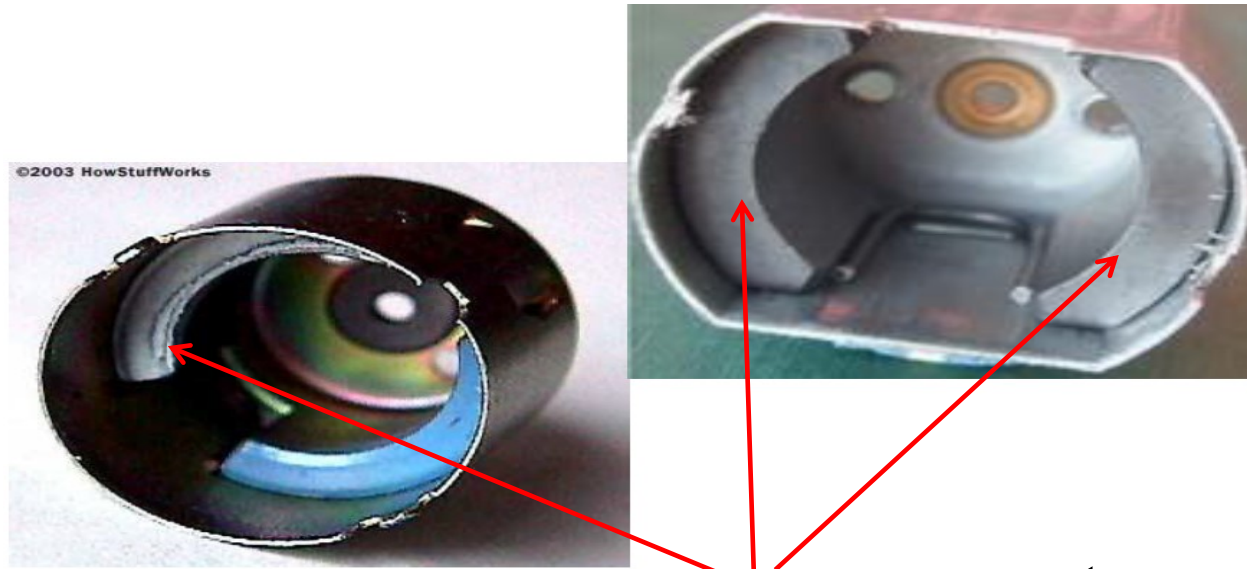
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DC motor working principle from Fleming's left hand rule

- **Stator : mechanical terms**

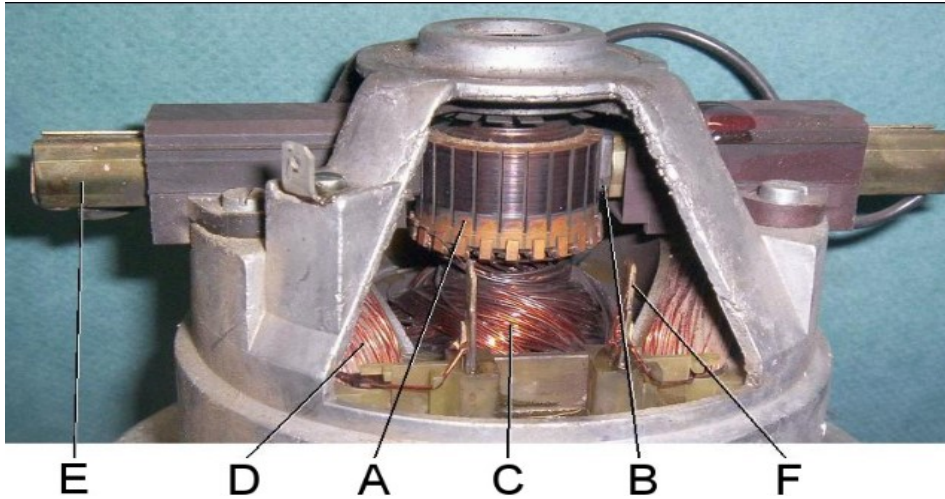


Images: <http://static.howstuffworks.com/gif/motor02.jpg>
<http://www.johnsonelectric.com/common/en/images/resources-for-engineers/automotive-applications/motion-technology/pmdc-motor/basic-configuration-04.jpg>

permanent magnet

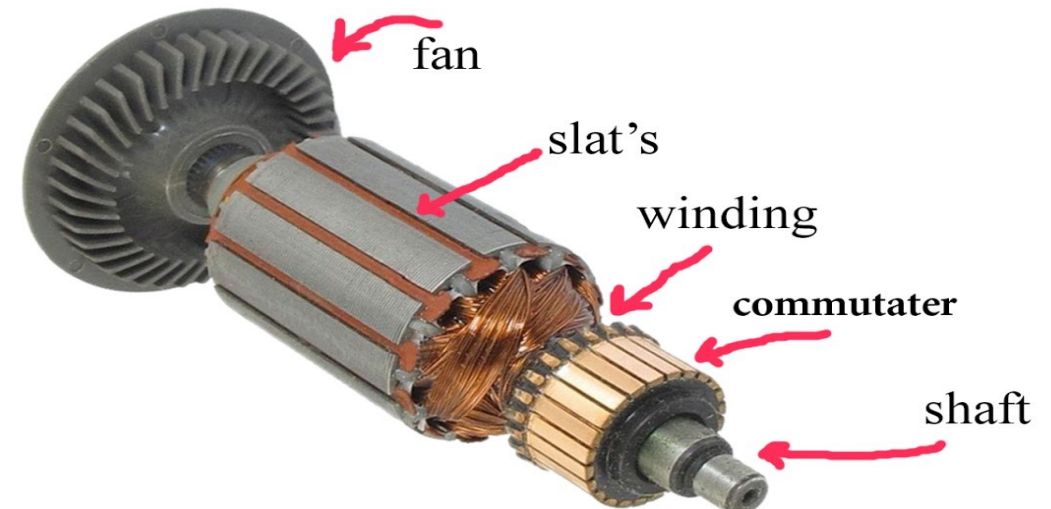
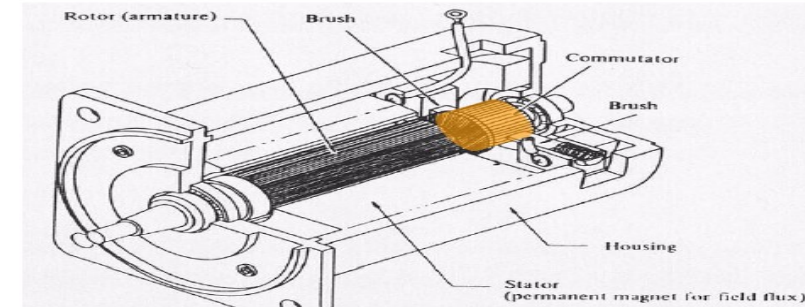
DC motor working principle from Fleming's left hand rule

● Commutator : mechanical terms



Parts: (A) commutator, (B) brush, (C) rotor (armature) windings, (D) stator (F) (field) windings, (E) brush guides

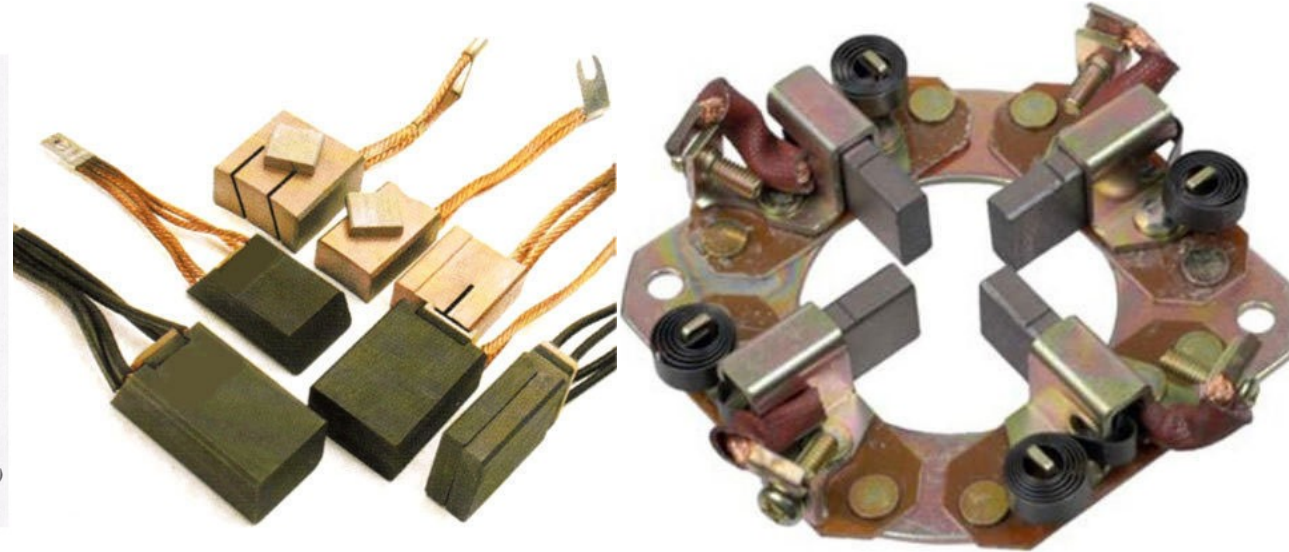
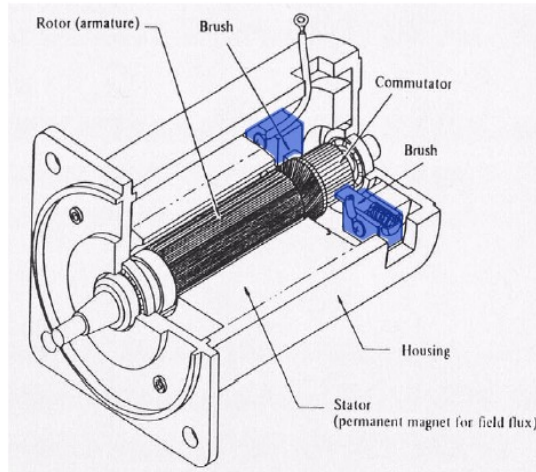
[https://en.wikipedia.org/wiki/Commutator_\(electric\)#/media/File:Universal_motor_commutator.jpg](https://en.wikipedia.org/wiki/Commutator_(electric)#/media/File:Universal_motor_commutator.jpg)



<https://www.technicalbabajan.com/2017/11/what-is-armature-armature-kya-armature.html>

DC motor working principle from Fleming's left hand rule

● Brush : mechanical terms

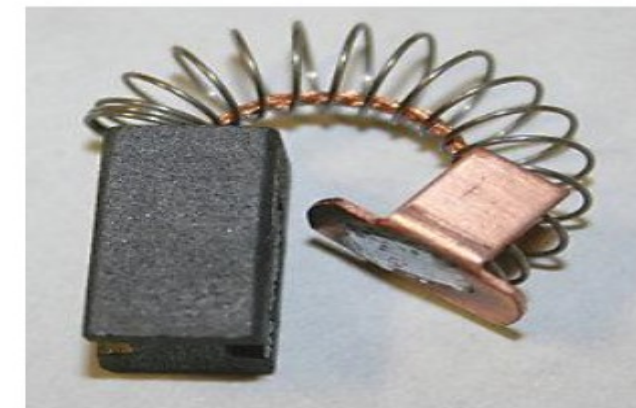
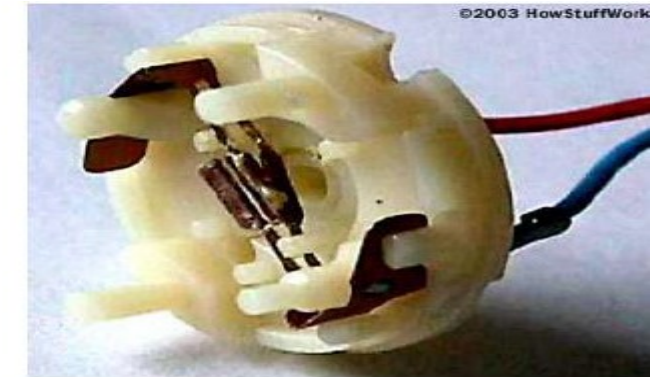
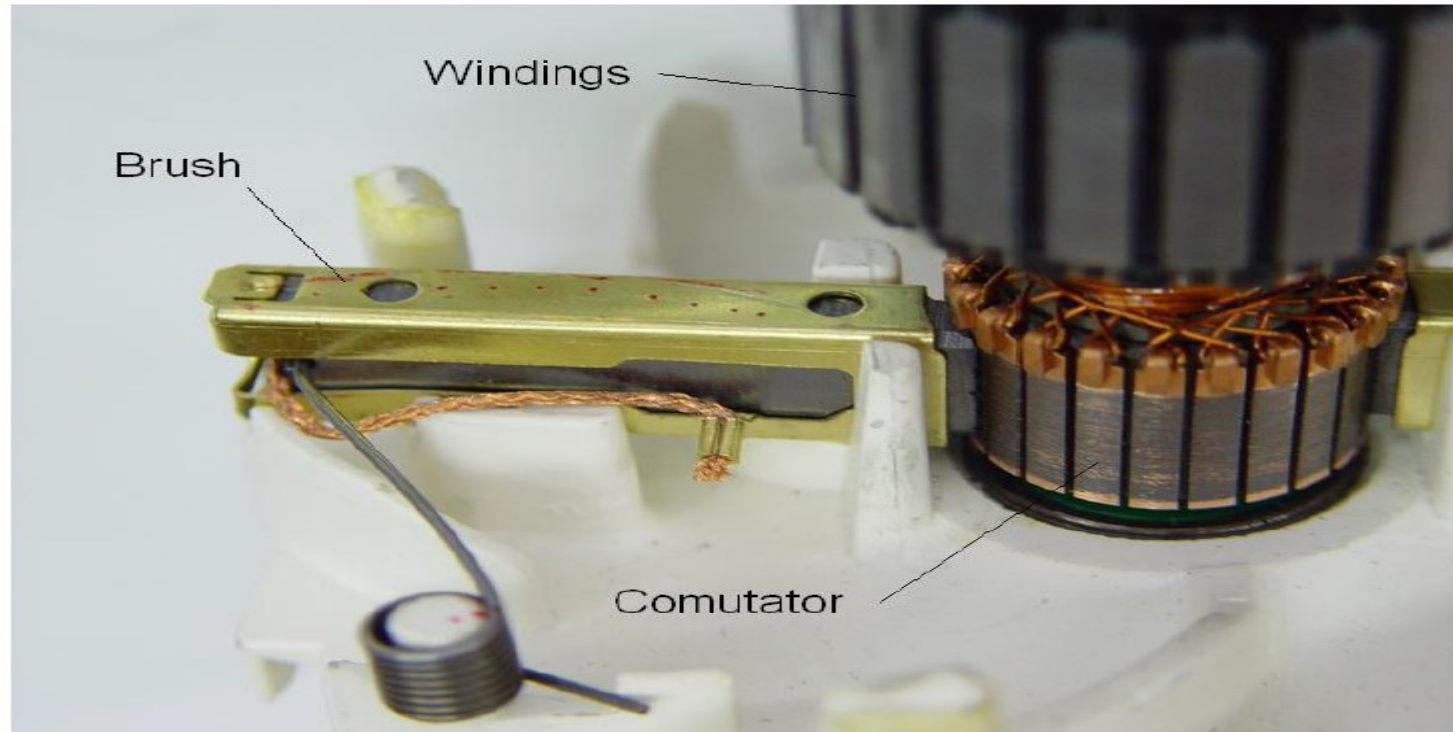


<https://www.indiamart.com/proddetail/dc-motor-carbon-brushes-8580964291.html>

<https://www.indiamart.com/proddetail/dc-motor-carbon-brush-18403148033.html>

DC motor working principle from Fleming's left hand rule

● Brush : mechanical terms



DC motor working principle from Fleming's left hand rule

- **Commutator and brushes : mechanical terms**

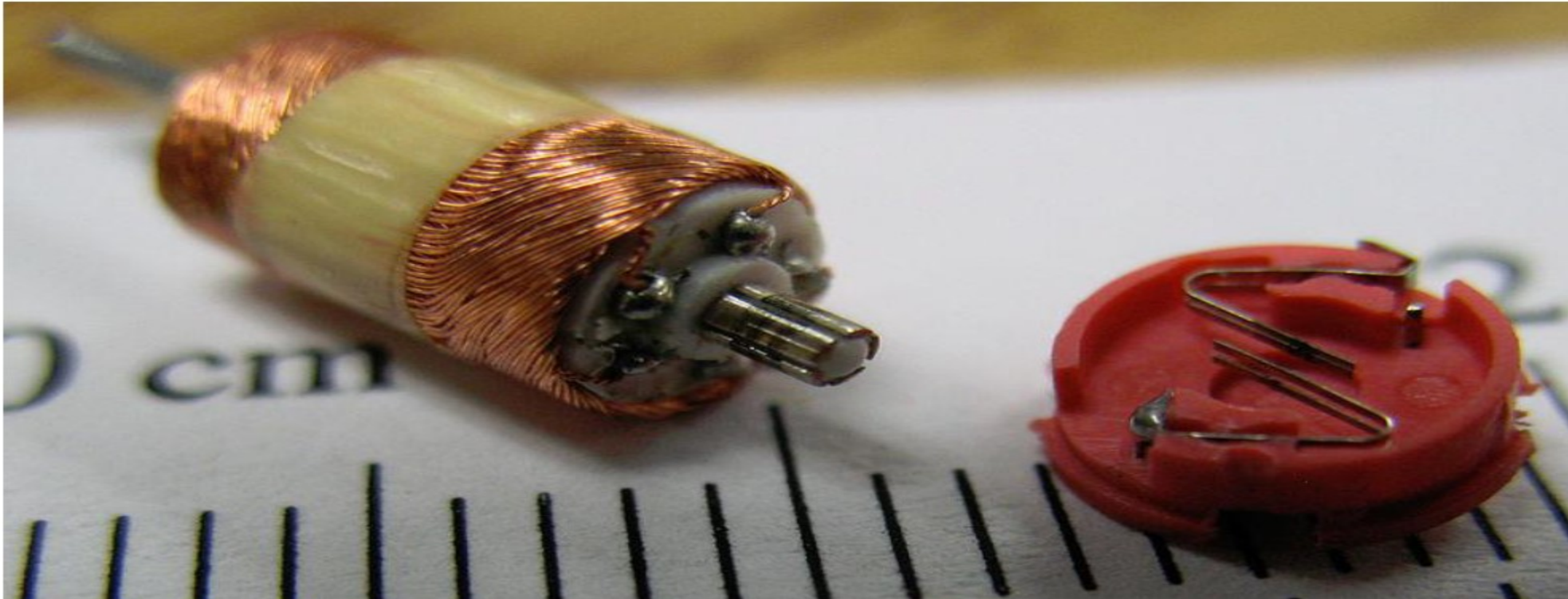


Image: https://en.wikipedia.org/wiki/File:Tiny_motor_windings_-_commutator_-_brushes_in_Zip_Zaps_toy_R-C_car.jpg

DC motor working principle from Fleming's left hand rule

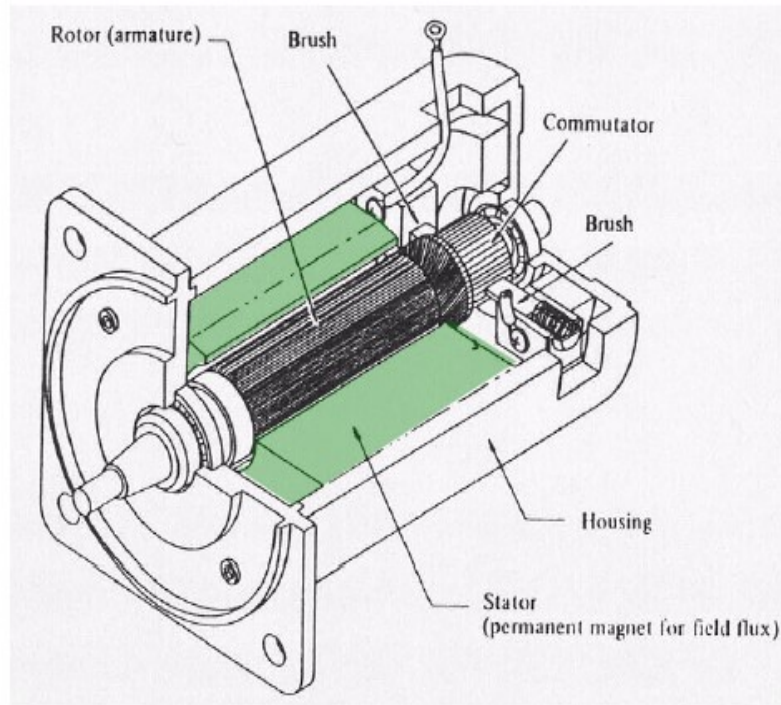
● Brush :weak point for brushed DC motors

Brushes tend to:

- Wear out
- Generate electrical (and acoustic) noise
 - Copper-graphite (cheaper, more current, more noise)
 - Precious metal (more expensive, less current, less noise)
- Limit maximum voltage

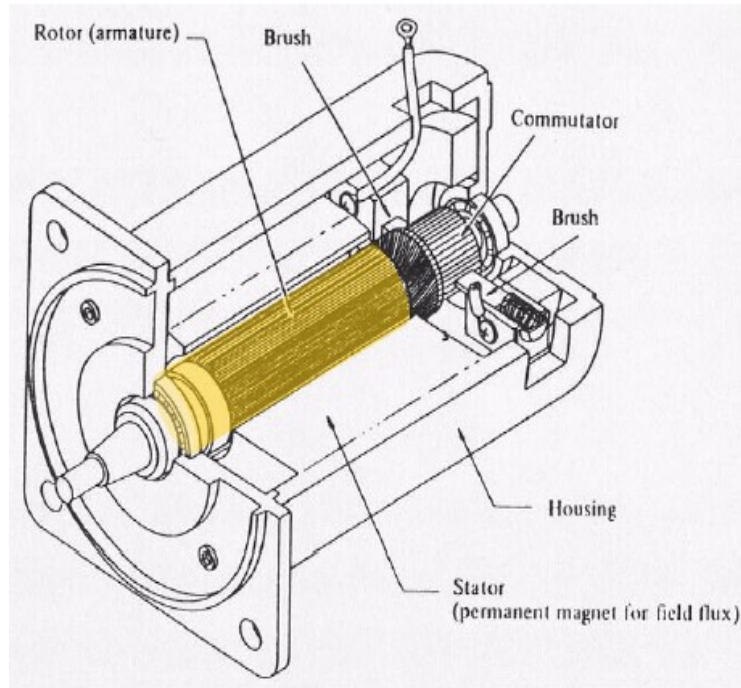
DC motor working principle from Fleming's left hand rule

- **Field system: electrical terms**



DC motor working principle from Fleming's left hand rule

- **Armature: electrical terms**



DC motor working principle from Fleming's left hand rule

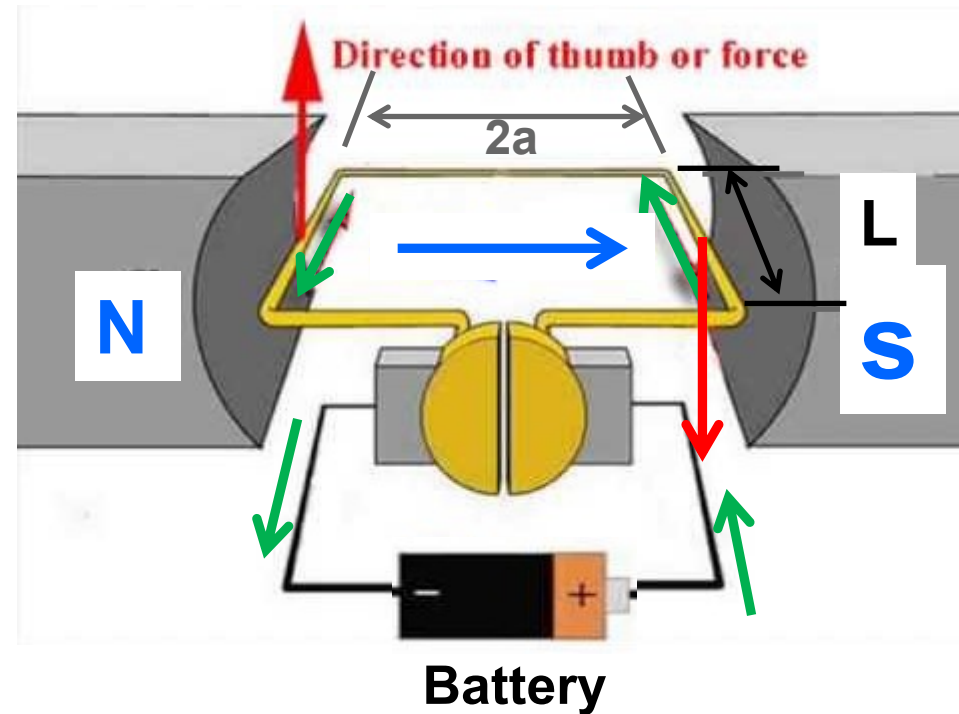
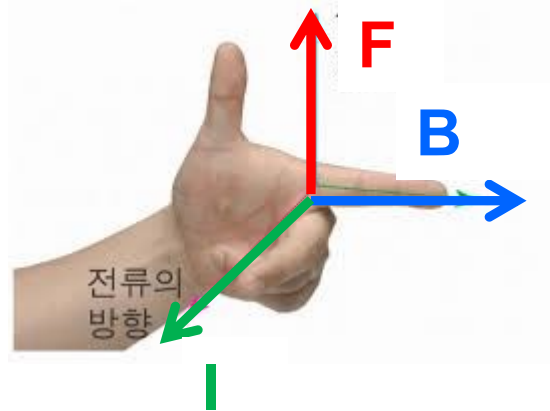
● Force and torque

-B magnetic field : from N to S

-I current direction in coil: from battery + to battery -

-F force in coil : $F=B*I*L$

-T torque = $2(\text{two coils})*F* a$



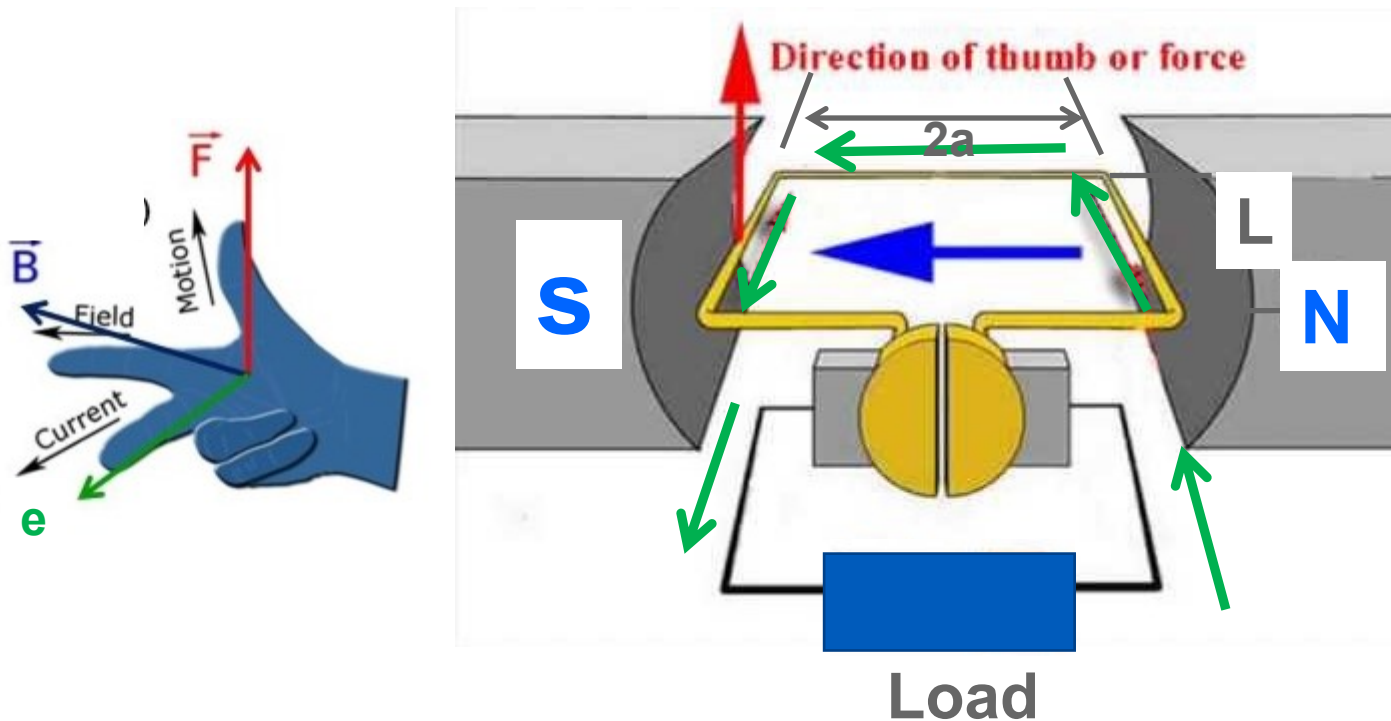
DC motor working principle from Fleming's right hand rule

- Fleming's right hand rule: generator

-B magnetic field : from N to S

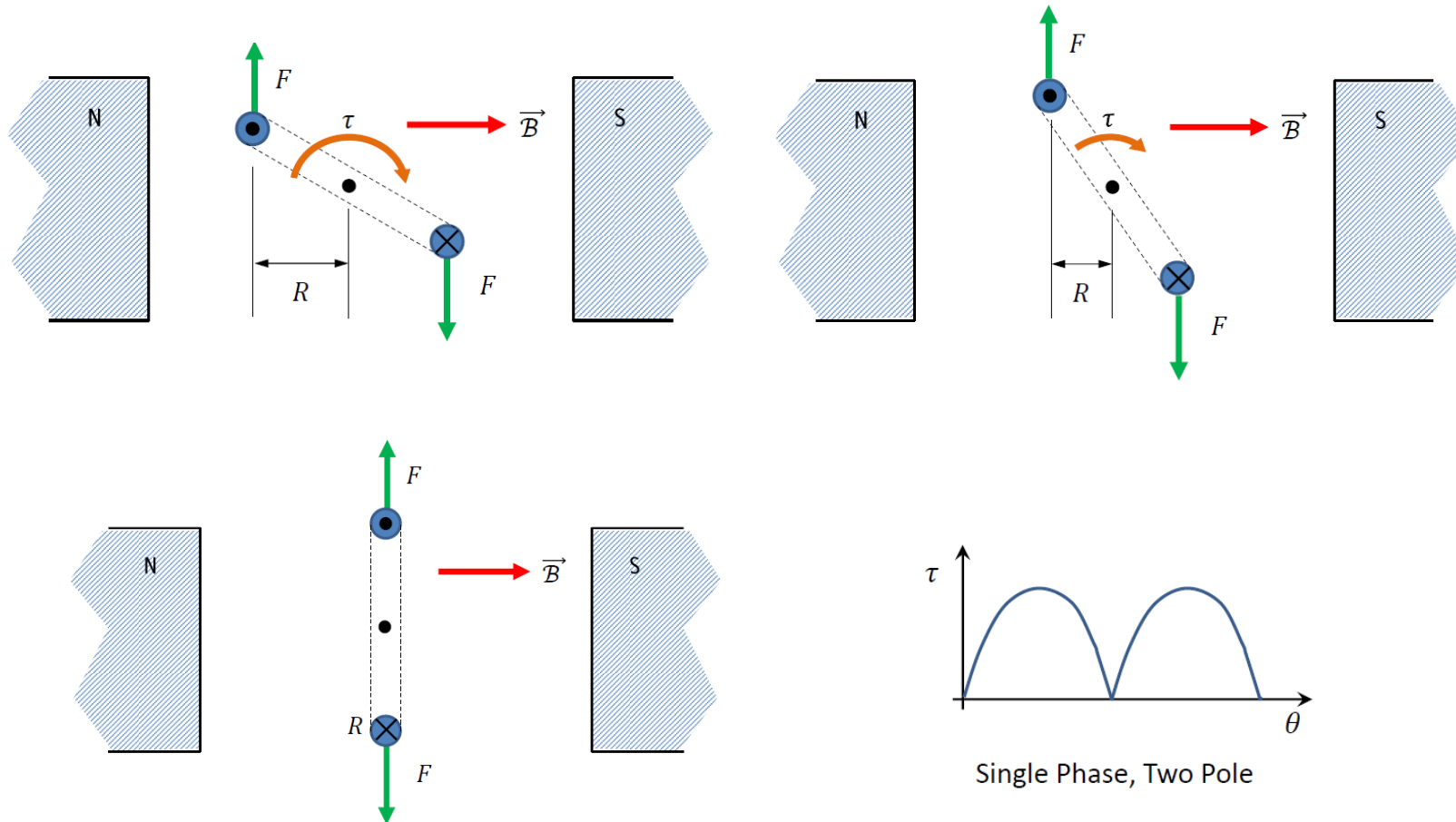
-F force in coil with speed v

-e Induced voltage: $e = B \cdot v \cdot L$



DC motor working principle from Fleming's left hand rule

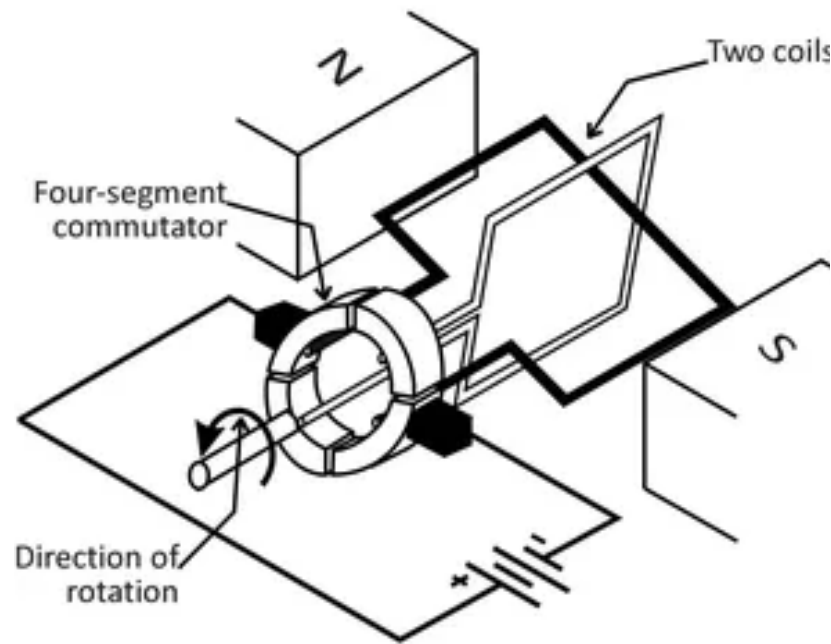
● Force and torque



No torque at all, what shall we do ???

DC motor working principle from Fleming's left hand rule

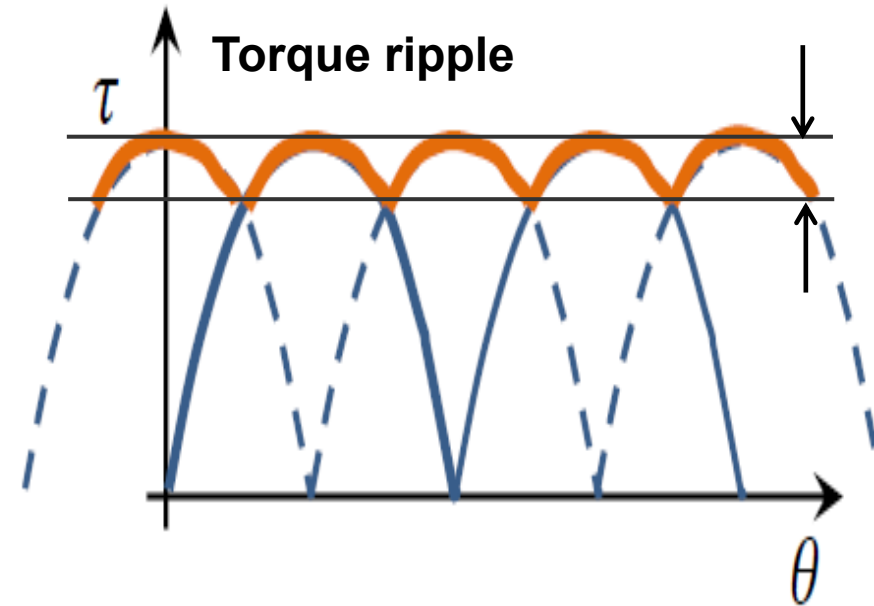
- Force and torque



(a): Simple 2-coil DC motor

4 segment commutator and two coi

<https://www.quora.com/I-could-not-understand-how-does-an-electric-motor-work-and-why-do-we-use-commutator-how-do-they-reverse-the-direction-of-the-current>

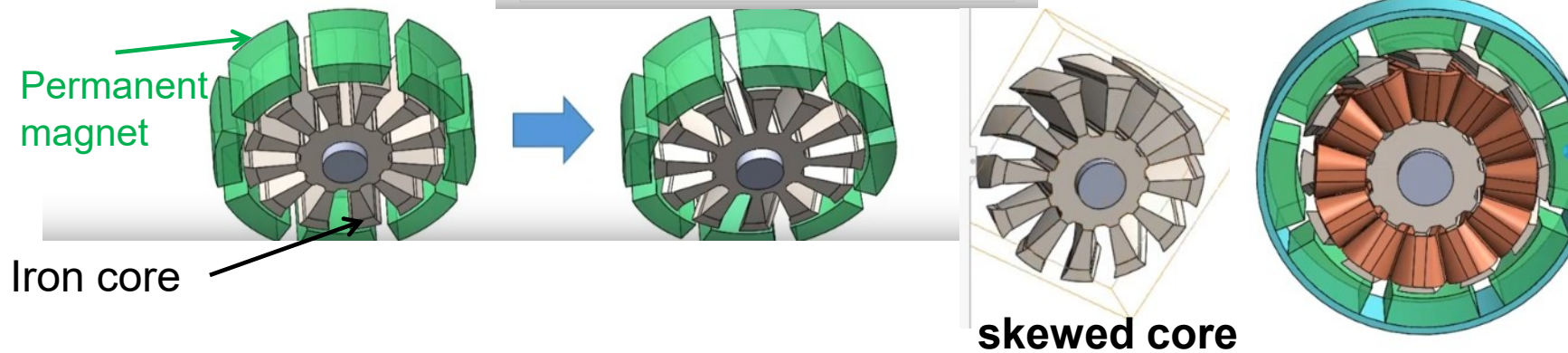
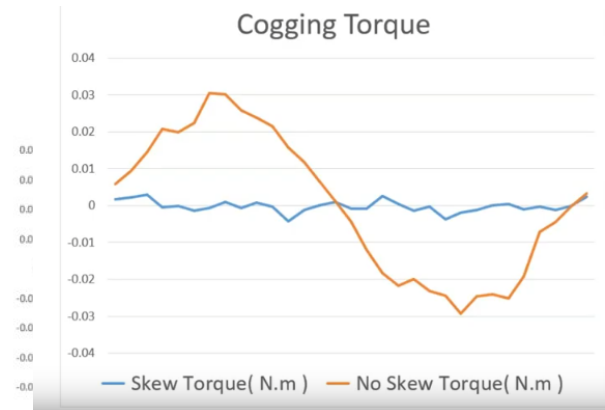


DC motor working principle from Fleming's left hand rule

● Force and torque

Cogging Torque

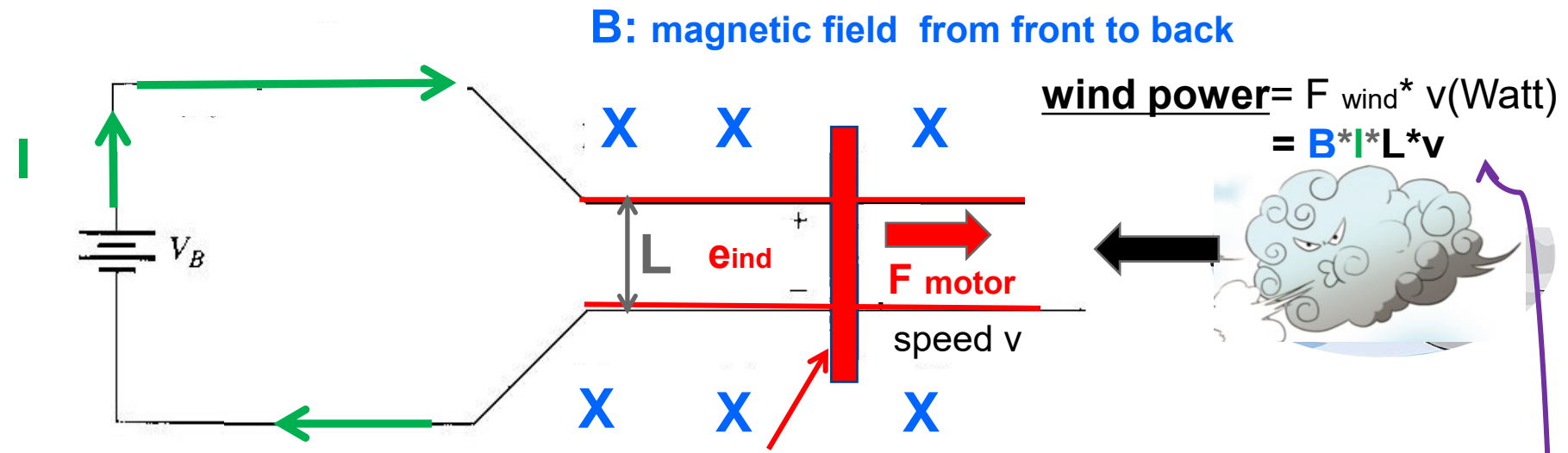
- Effects:
 - Vibration, Noise
 - Velocity variation
- Skewed stator slots:



<https://www.youtube.com/watch?v=O3MpiGL7CoE>

DC motor working principle from Fleming's left hand rule

- Energy conversion in dc motor: without coil resistance



I current direction in coil: Moving conductor bar: copper

-During working with speed v , $F_{motor} = F_{wind}$ means no acceleration

-Fleming's left hand rule: $F_{motor} = B * I * L$ → **motor power** = $F_{motor} * v = B * I * L * v$

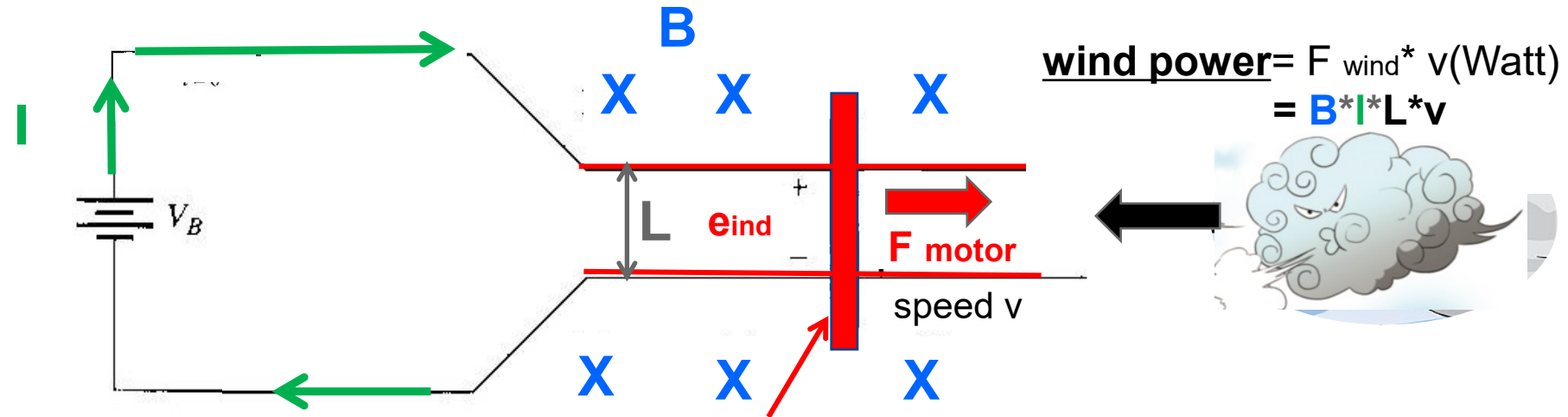
-Fleming's right hand rule: $e_{ind} = B * v * L$ is induced at moving conductor bar

-**Battery power** $V_B * I = e_{ind} * I = B * v * L * I$

All are same!! very important

DC motor working principle from Fleming's left hand rule

- Energy conversion in dc motor: without coil resistance



I current direction in coil:

Moving conductor bar: copper

-During working with speed v 4m/s, $F_{wind} = 15 \text{ N}$ \Rightarrow wind power = 60W

-Fleming's left hand rule: $F_{motor} = B \cdot I \cdot L \Rightarrow F_{motor} (15\text{N}) = B(1.5\text{T}) \cdot I \cdot L(0.2 \text{ m}) \Rightarrow I = 50 \text{ A}$

motor power = $F_{motor} (15\text{N}) \cdot v (4\text{m/s}) = 60\text{W}$

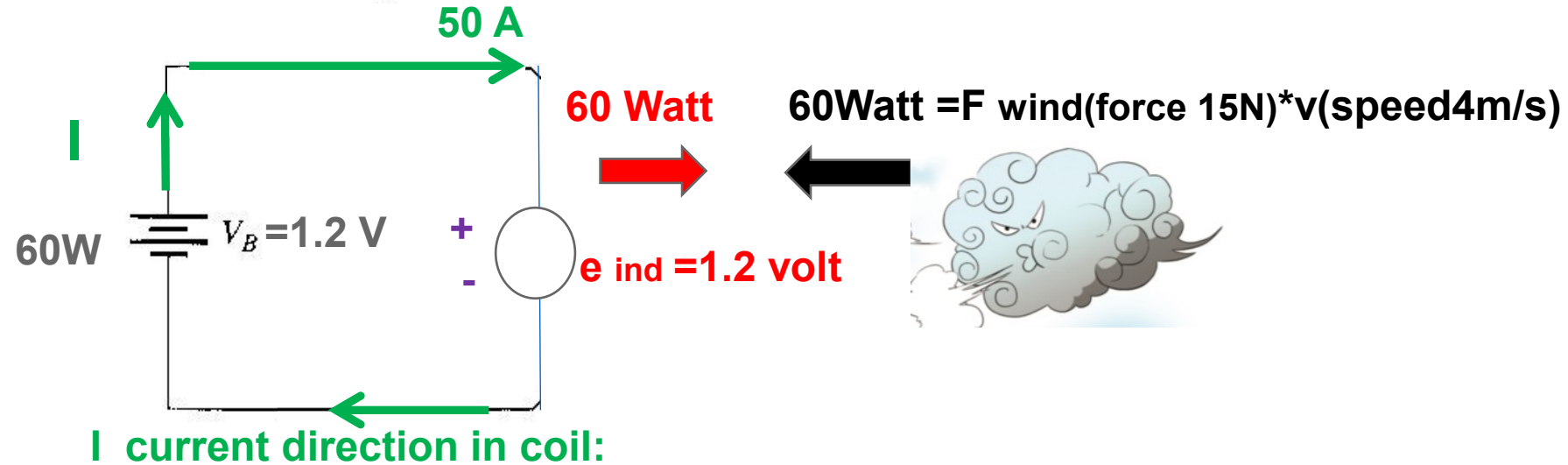
- Fleming's right hand rule: $e_{ind} = B(1.5) \cdot v(4) \cdot L(0.2) \Rightarrow e_{ind} = 1.2 \text{ V}$

-Battery power $V_B \cdot I = e_{ind} \cdot I = B \cdot v \cdot L(1.2\text{V}) \cdot I(50\text{A}) = 60\text{W}$

All are same!!

DC motor working principle from Fleming's left hand rule

- Energy conversion in dc motor: without coil resistance

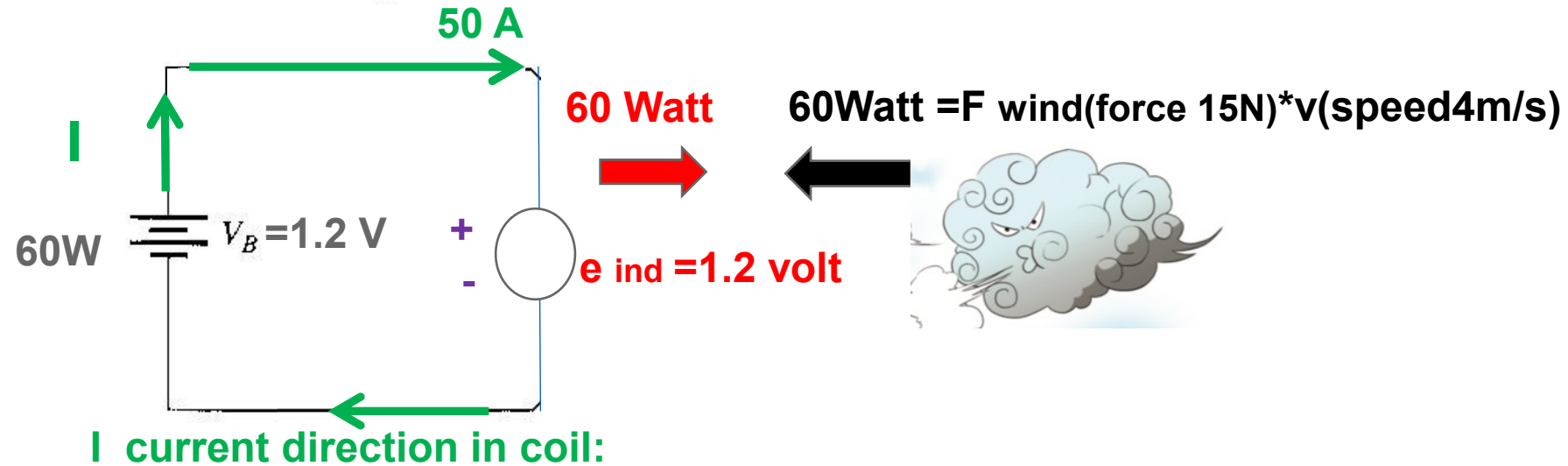


Mechanical load power :	wind power= $F_{wind} * v$ (Watt)	60W
Battery power:	$V_B * I$, $V_B = e_{ind}$	60 W
Motor power :	$e_{ind} * I$	60 W

Efficiency = motor out- put power / motor in put power (Battery out put power)
 $= 60/60 = 100\%$

DC motor working principle from Fleming's left hand rule

- Energy conversion in dc motor: without coil resistance



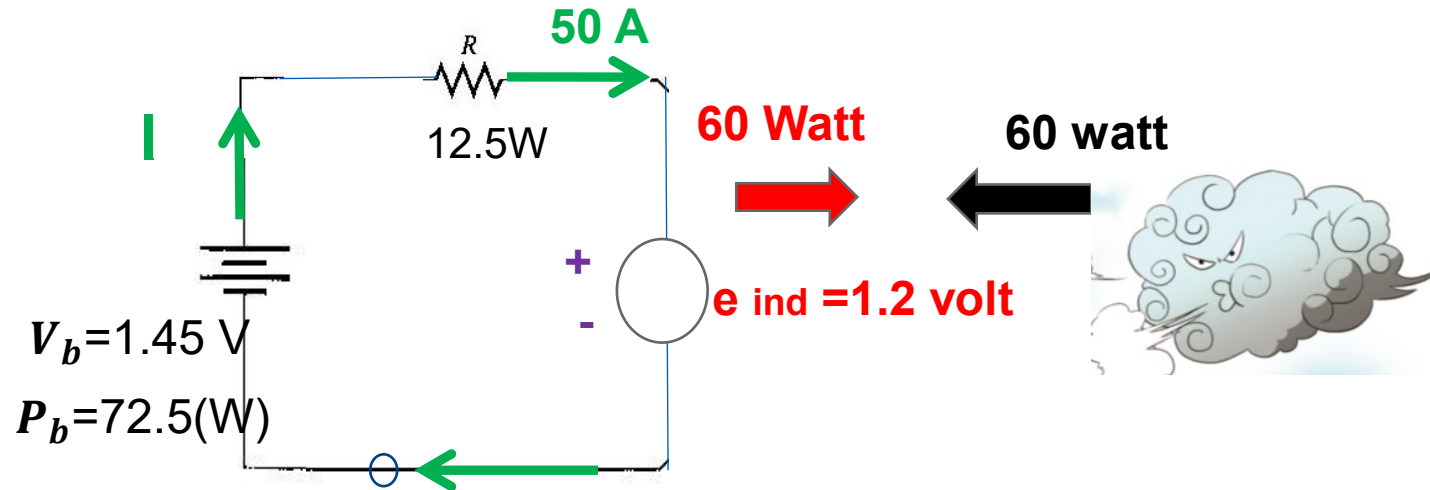
Mechanical load power :	wind power= $F_{wind} * v$ (Watt)	60W
Battery power:	$V_B * I$, $V_B = e_{ind}$	60 W
Motor power :	$e_{ind} * I$	60 W

Efficiency = motor out- put power / motor in put power (Battery out put power)
 = 60/60 = 100%

DC motor working principle from Fleming's left hand rule

- Energy conversion in dc motor with coil resistance

If there is $R=0.005$ ohm, $V_R = 0.005*50 = 0.25$ V



Battery power: $V_b = e_{ind} (1.2) + V_R (0.25) = 1.45$ V $\Rightarrow V_b (1.45) * I(50) = 72.5$ W

Motor output power: $e_{ind} * I = e_{ind} (1.2) * I(50) = 60$ W

Motor input power: power in coil resistance (12.5) + motor output power (60)
= 72.5 Watt

Motor efficiency = motor out put power/motor in put power = $60/72.5 = 82.75\%$

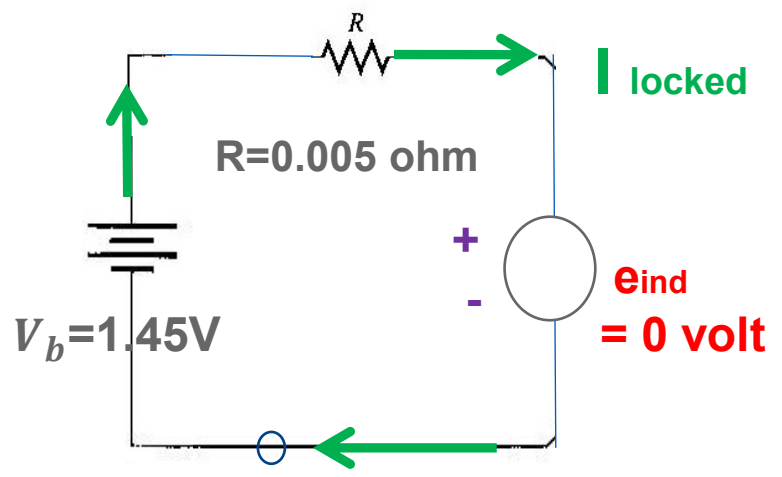
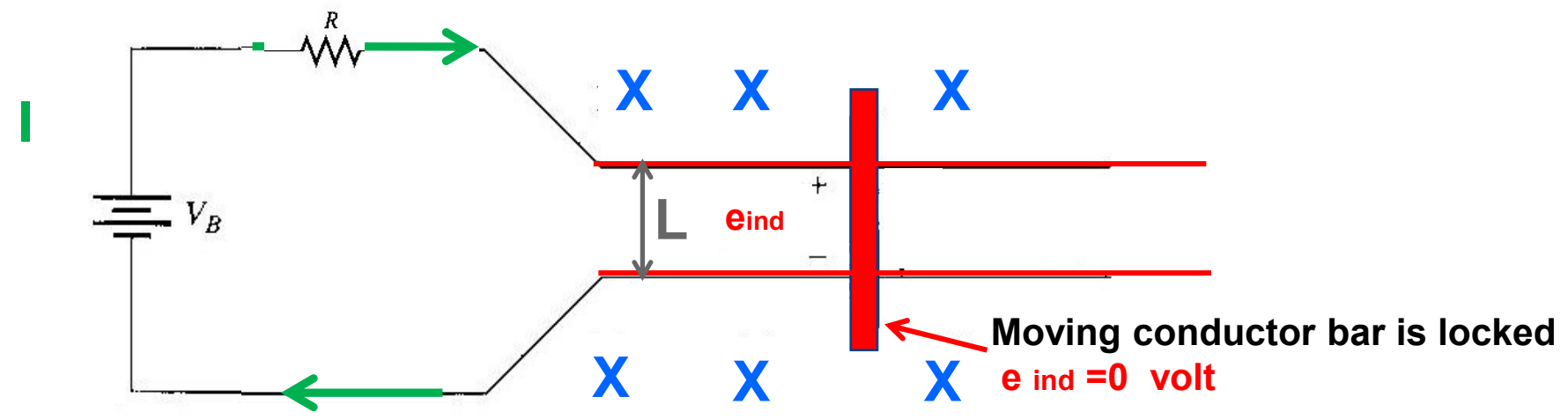
DC motor working principle from Fleming's left hand rule

- If motor mover or rotor is locked, what will be happened



DC motor working principle from Fleming's left hand rule

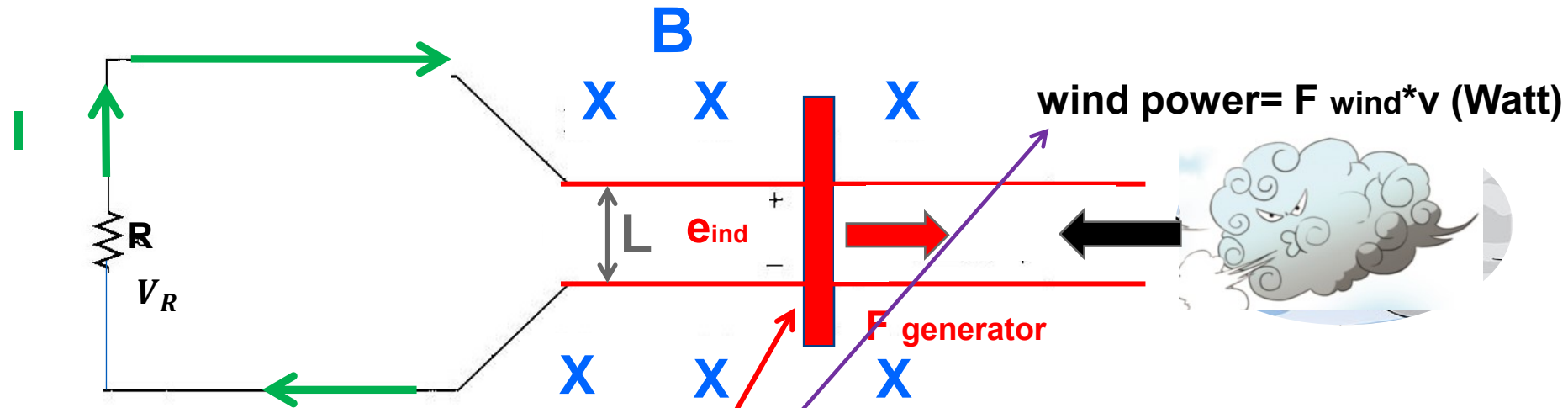
- If motor mover or rotor is locked, what will be happened



$I_{\text{locked}} = 1.45 / 0.005 = 290\text{A}$
 will burn motor winding
 (!!!!normal motor operation 50A)

- Immediately turn off motor
- remove the locking

DC generator working principle from Fleming's right hand rule



I current direction in coil: **Moving conductor bar: copper**

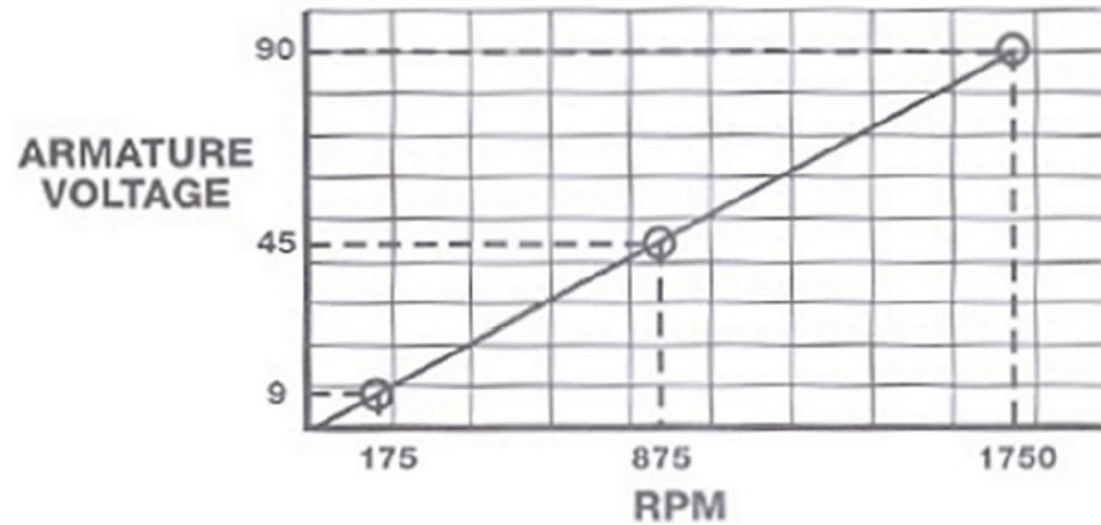
- During working with speed v , $F_{generator} = F_{wind}$ means no acceleration
- Fleming's right hand rule: **e induced voltage: $e_{ind} = B * v * L$** in moving conductor bar
- Fleming's left hand rule: **$F_{generator} = B * I * L \rightarrow I = F_{generator} / B * L$**
- Power in generator: **$e_{ind} = B * v * L * I = F_{generator} * v$**
- Power in load : **$V_R * I = e_{ind} * (F_{generator} / B * L) = B * v * L * (F_{generator} / B * L) = F_{generator} * v$**
- Power in wind = power in generator = power in load

DC generator working principle from Fleming's right hand rule

- 1) Fleming's left hand rule and Fleming's right hand rule are working together in energy conversion in motor or generator
- 2) If there is no losses in winding, efficiency=100%
 - motor: electrical power (in-put)= mechanical power (out put)
 - generator: mechanical power (in-put)= electrical power (out put)
- 3) In fact, efficiency will be 85% (depend on size and application)
 - motor: electrical power (in-put) > mechanical power (out put)
 - generator: mechanical power (in-put) > electrical power (out put)

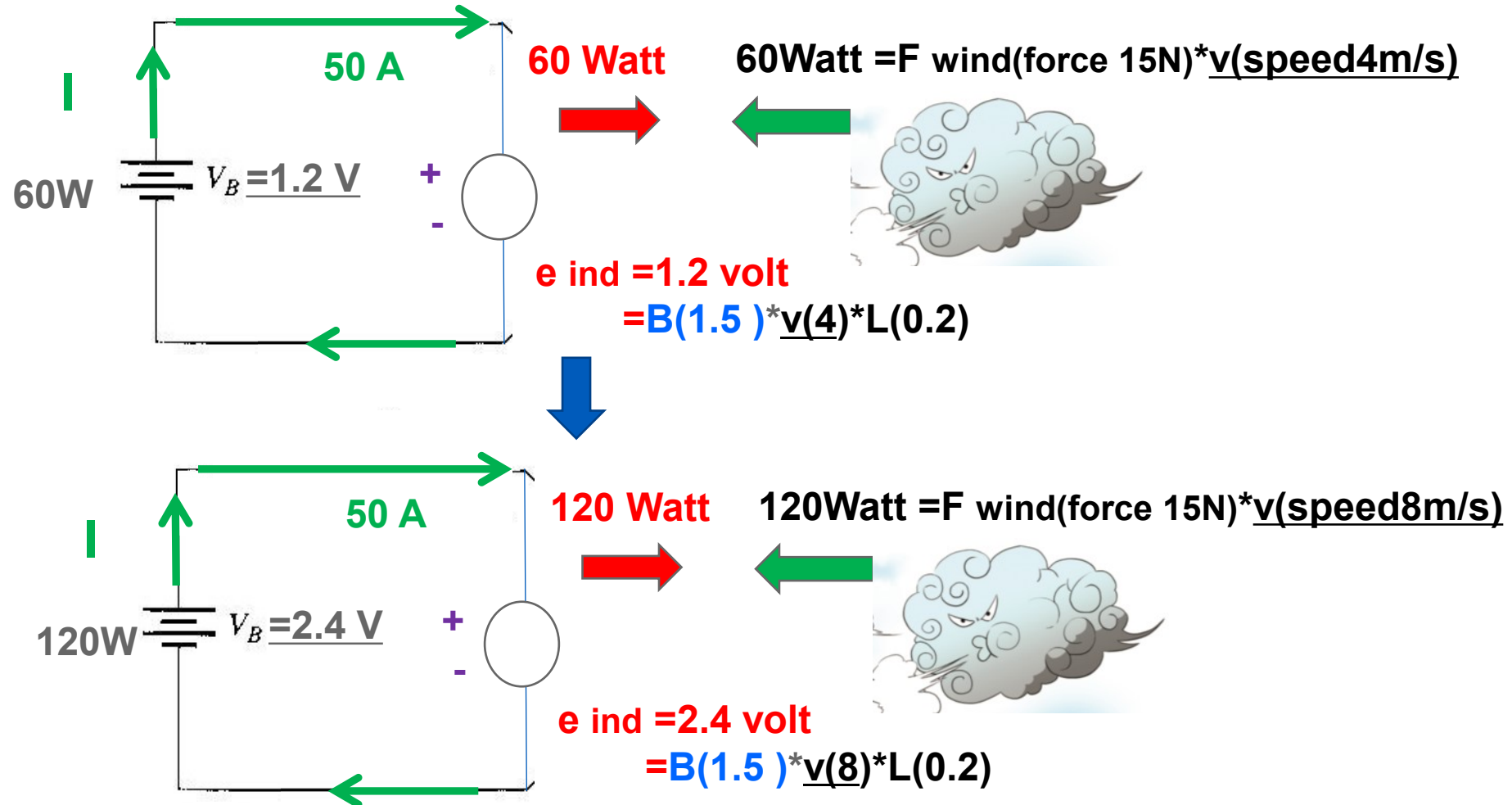
DC Motor control

- Increase voltage to increase speed
- Reverse voltage to reverse direction



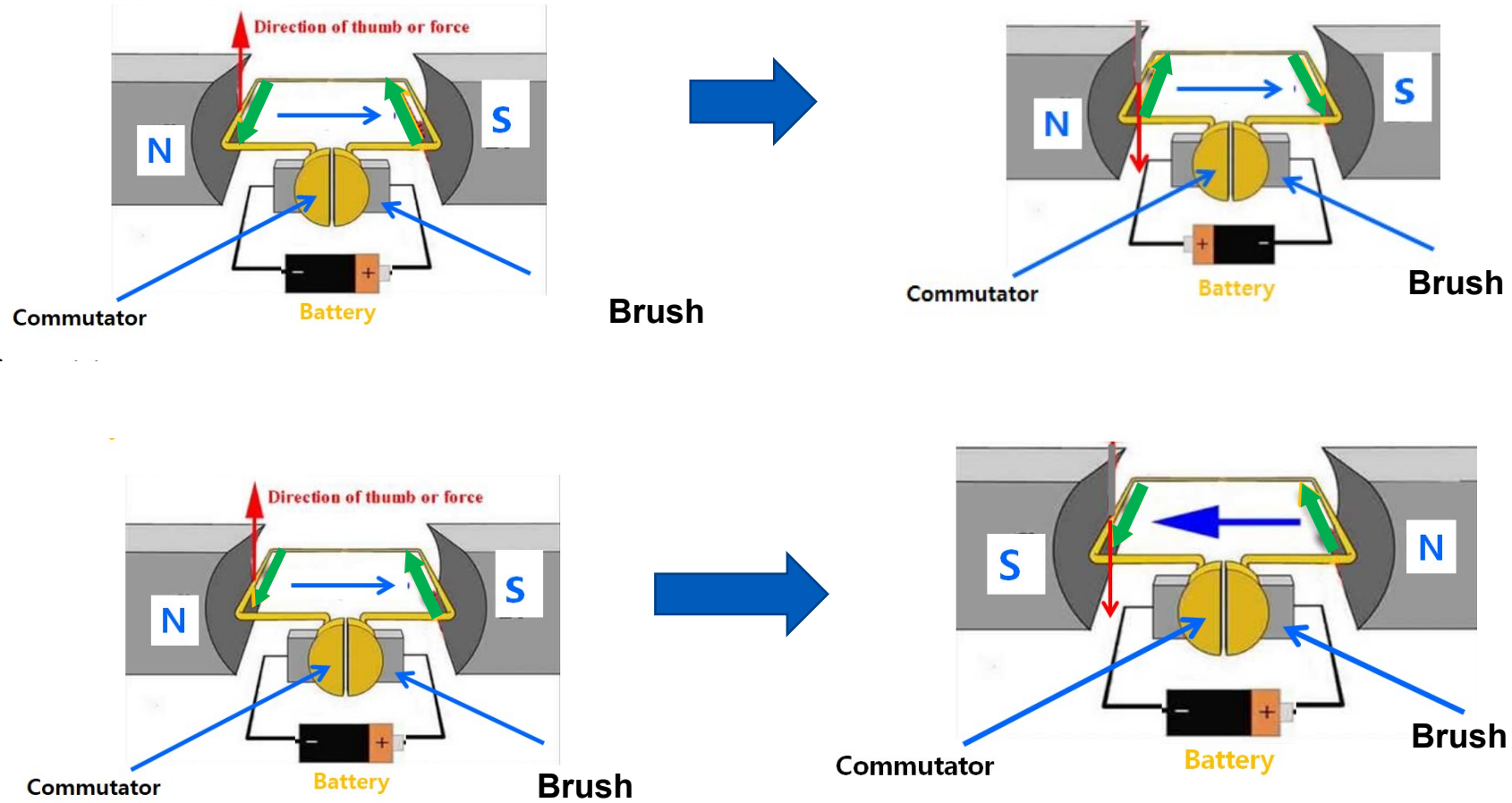
DC Motor control

- Increase voltage to increase speed



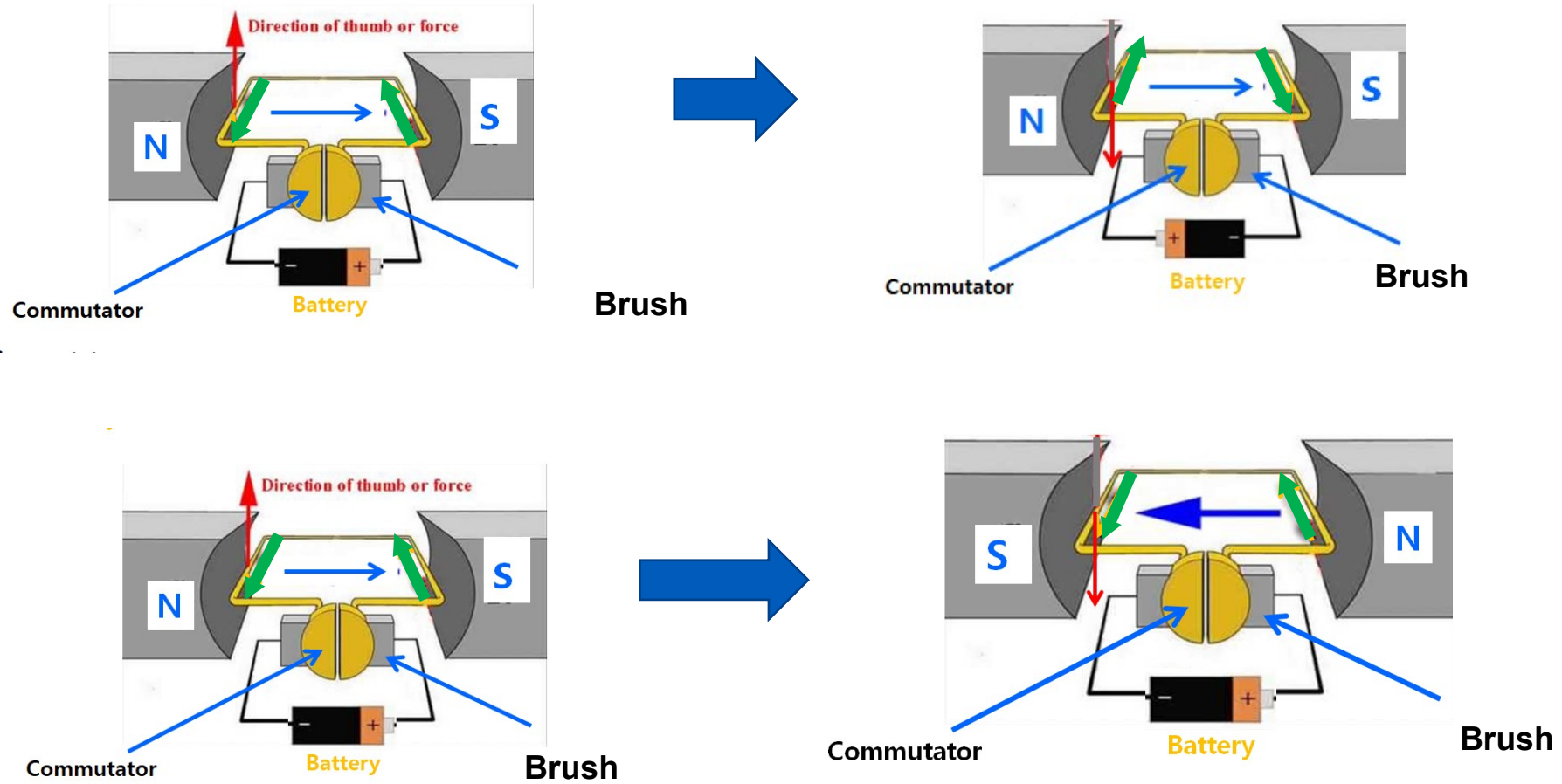
DC Motor control

- Reverse voltage to reverse direction



DC Motor control

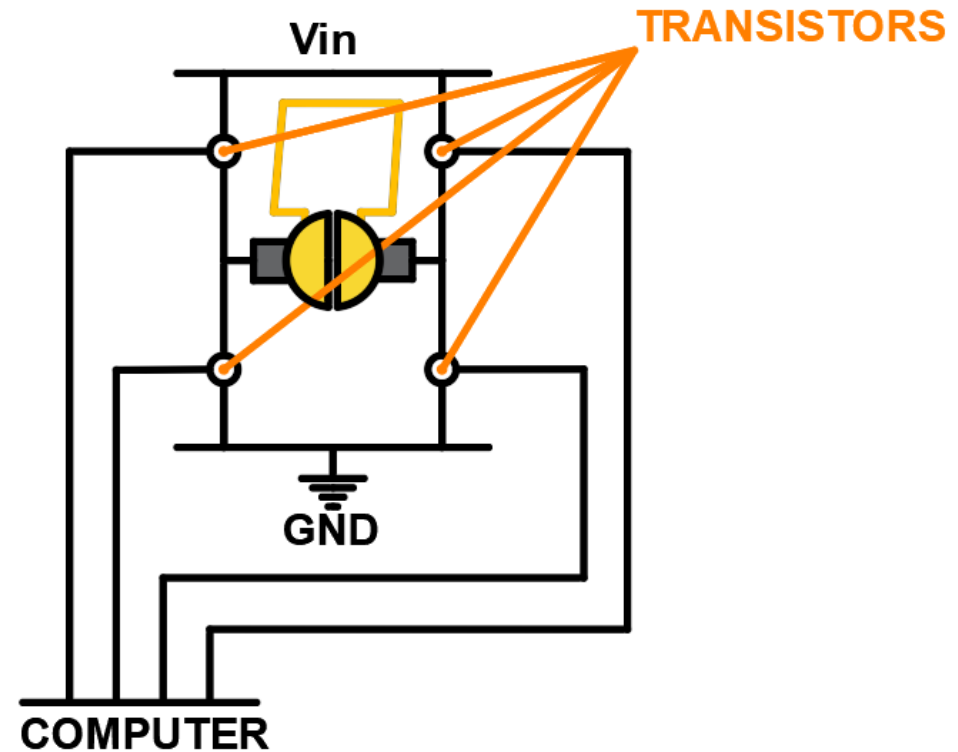
- Reverse voltage to reverse direction



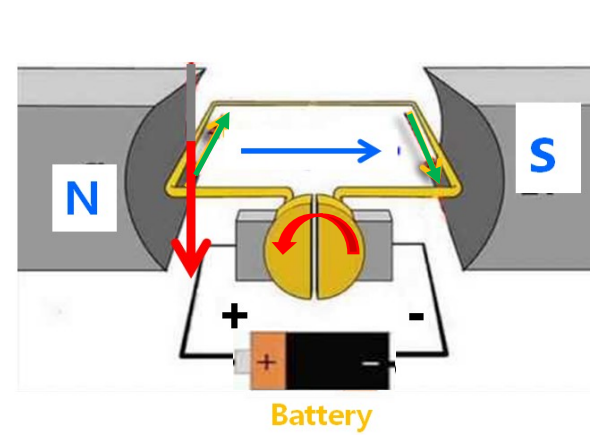
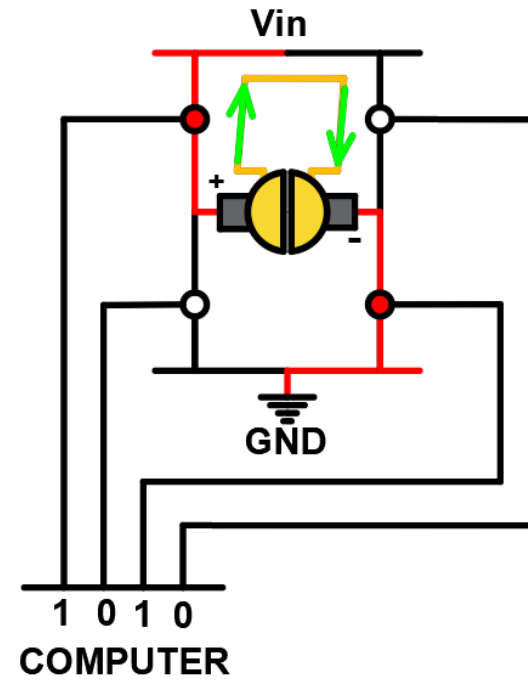
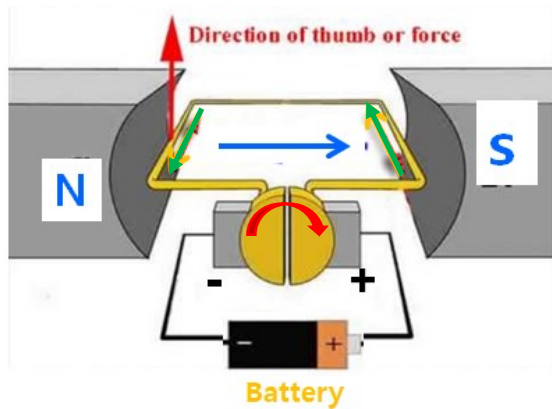
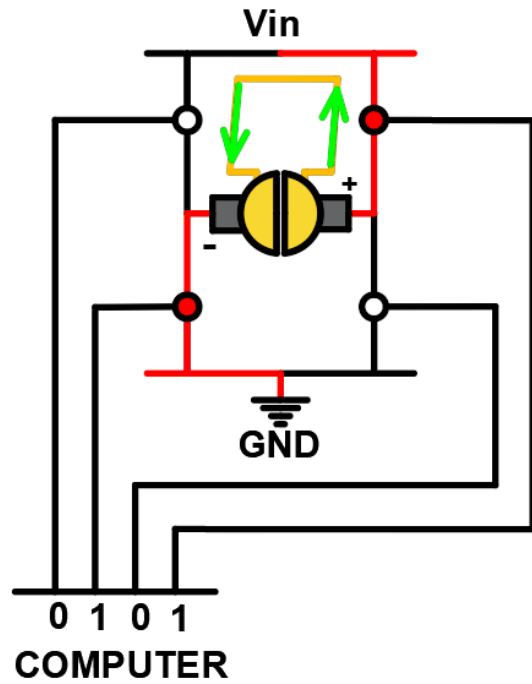
DC Motor control

● An H-bridge

- Name derived from shape of circuit
- Four switches (usually transistors) control circuit behavior
- Two switches turned on at a time
- Bipolar operation with unipolar supply voltage
- Speed is set by input voltage

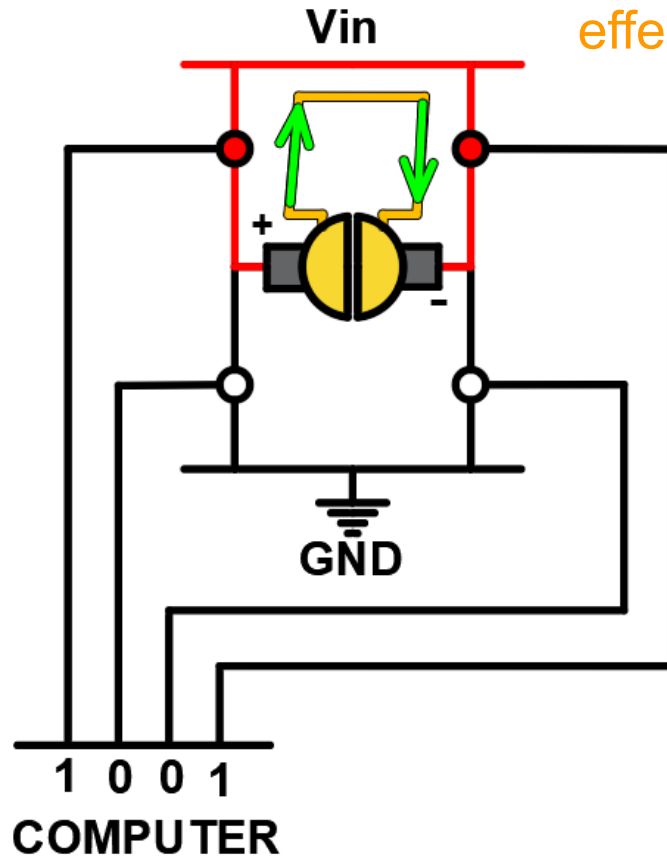


DC Motor control

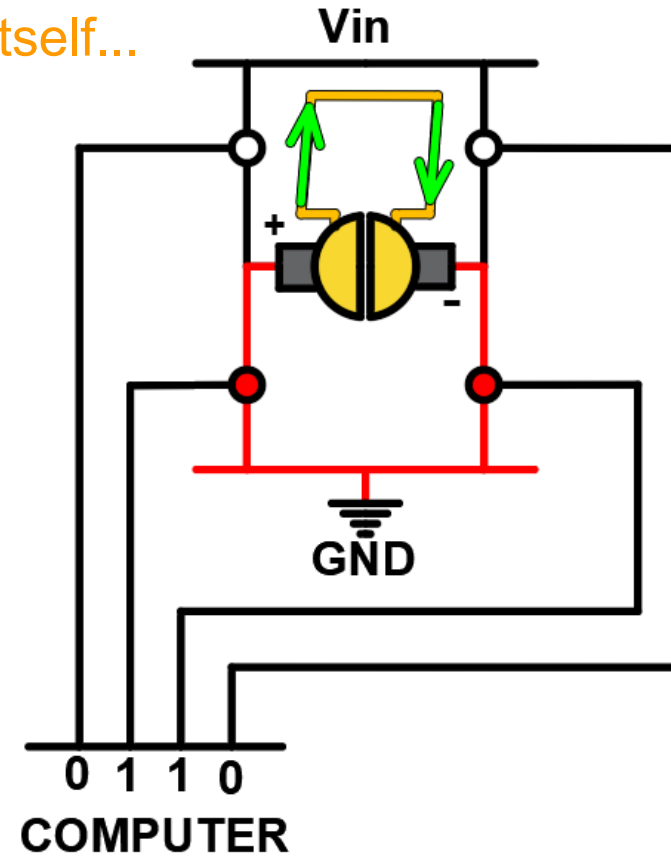


DC Motor control

Connecting motor leads causes the motor's generator effect to work against itself...

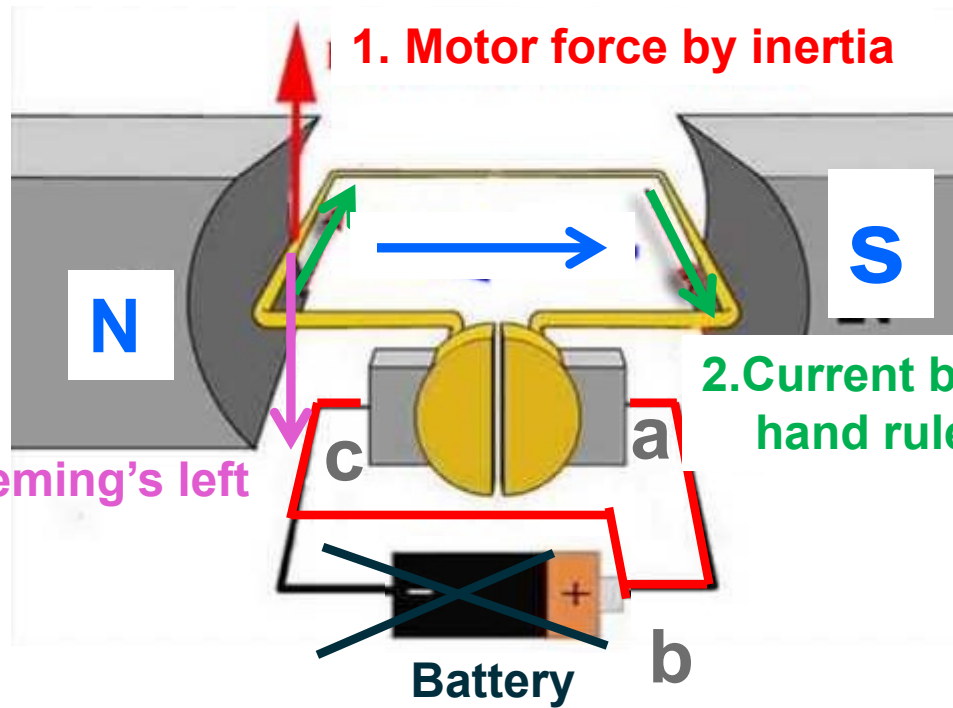
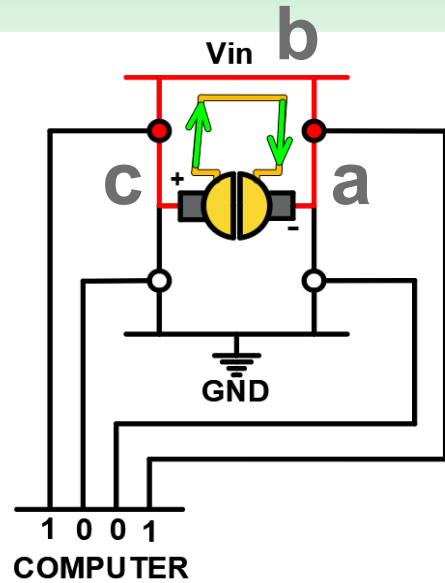


Braking Operation-1



Braking Operation-2

DC Motor control



3. Force by Fleming's left hand rule

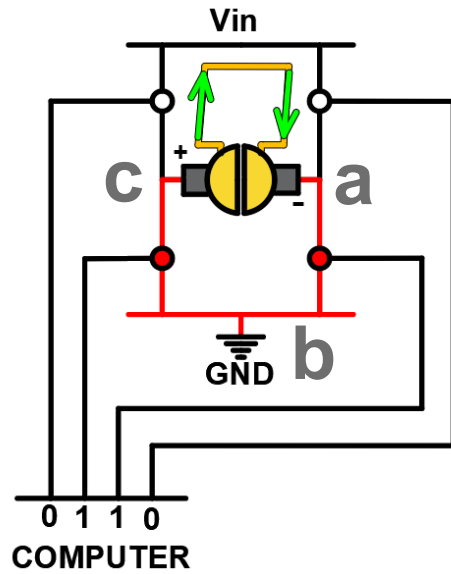
2. Current by Fleming's right hand rule: Generator

1. Motor force by inertia

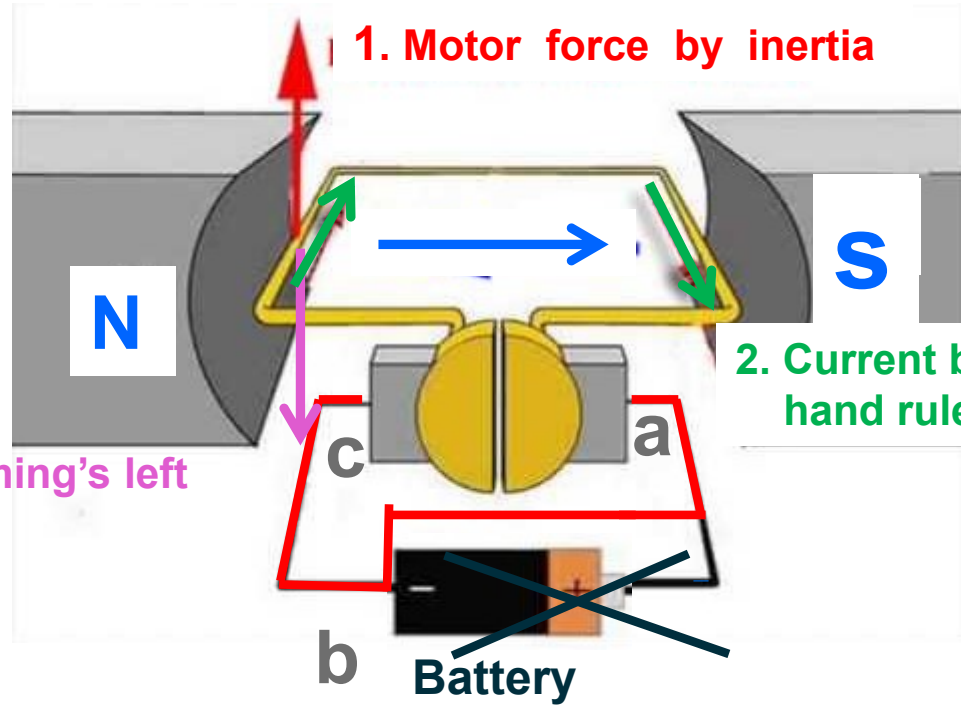
3. Force by Fleming's left hand rule in short circuit at generator

Braking force

DC Motor control



3. Force by Fleming's left hand rule



2. Current by Fleming's right hand rule: Generator

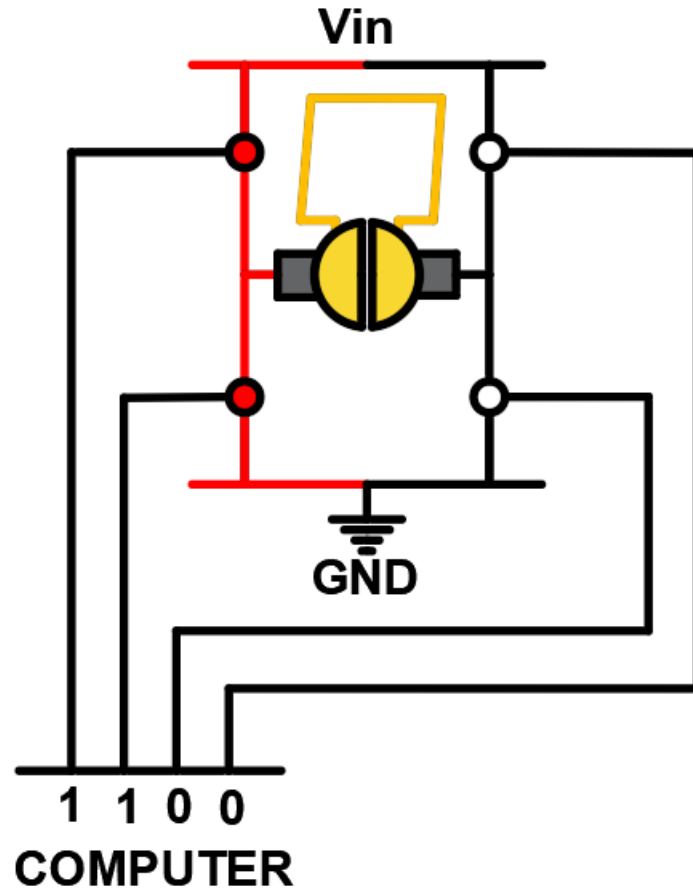
1. Motor force by inertia



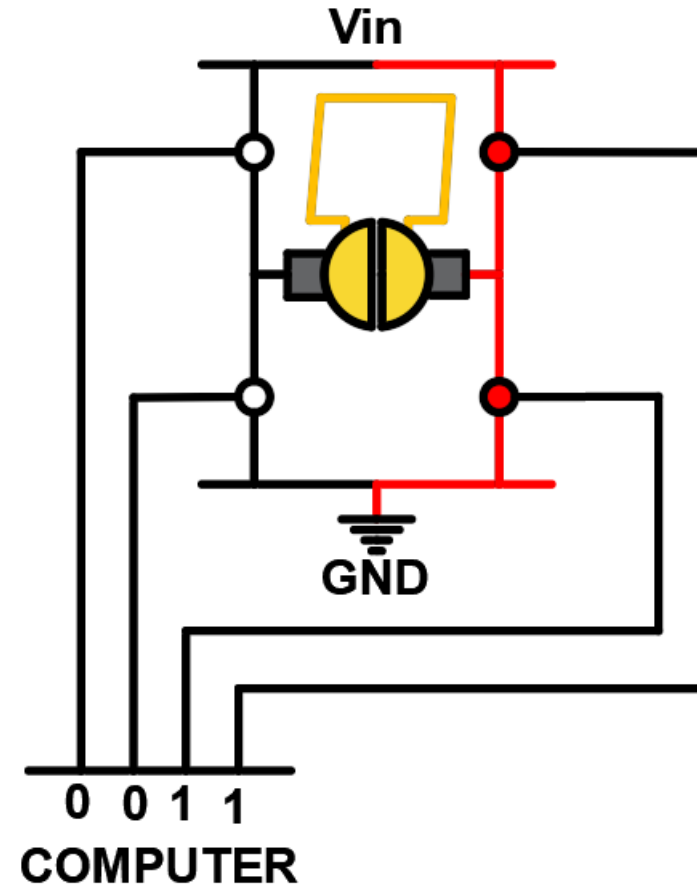
3. Force by Fleming's left hand rule in short circuit at generator

Braking force

DC Motor control

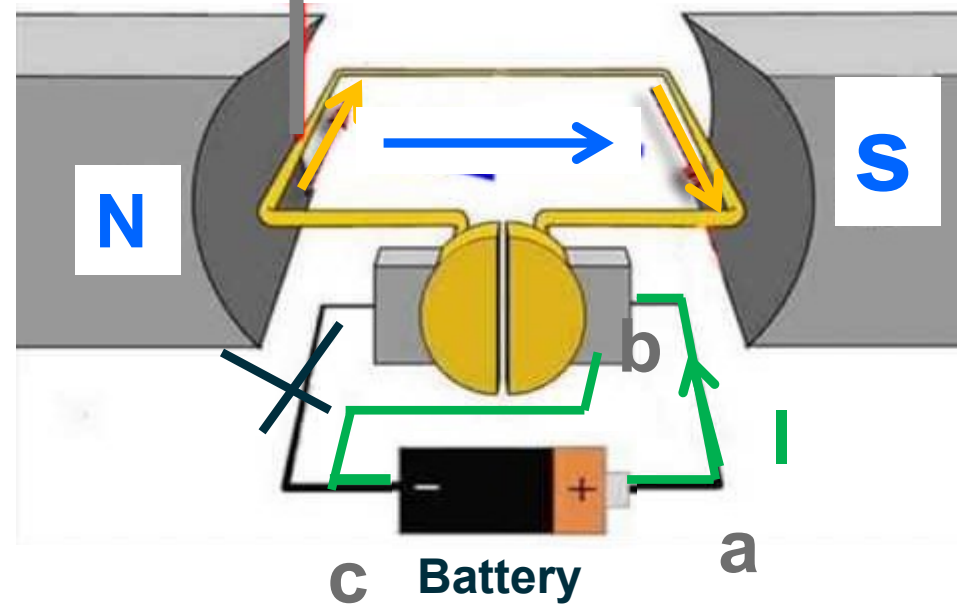
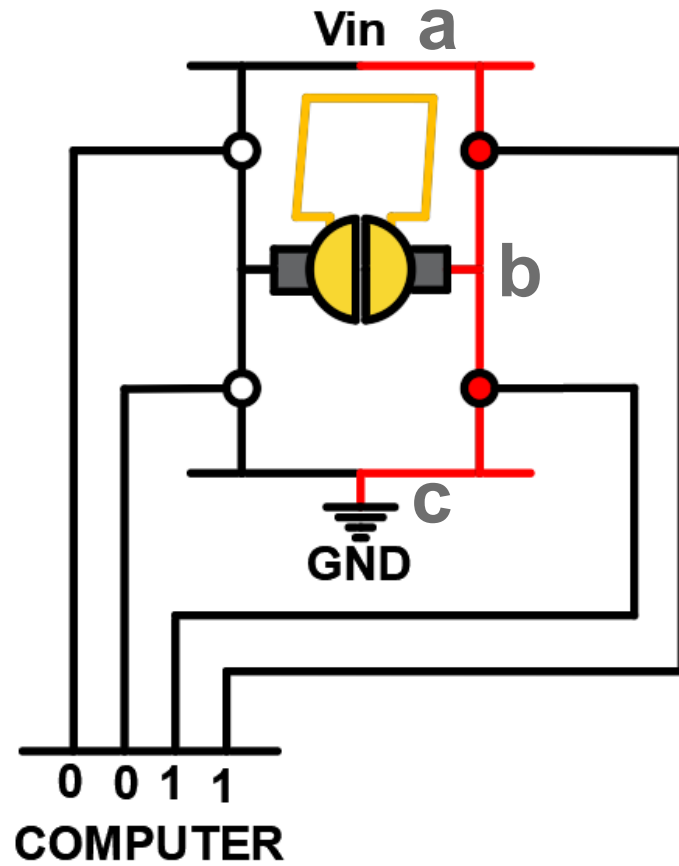


"Shoot thru" (not desirable)



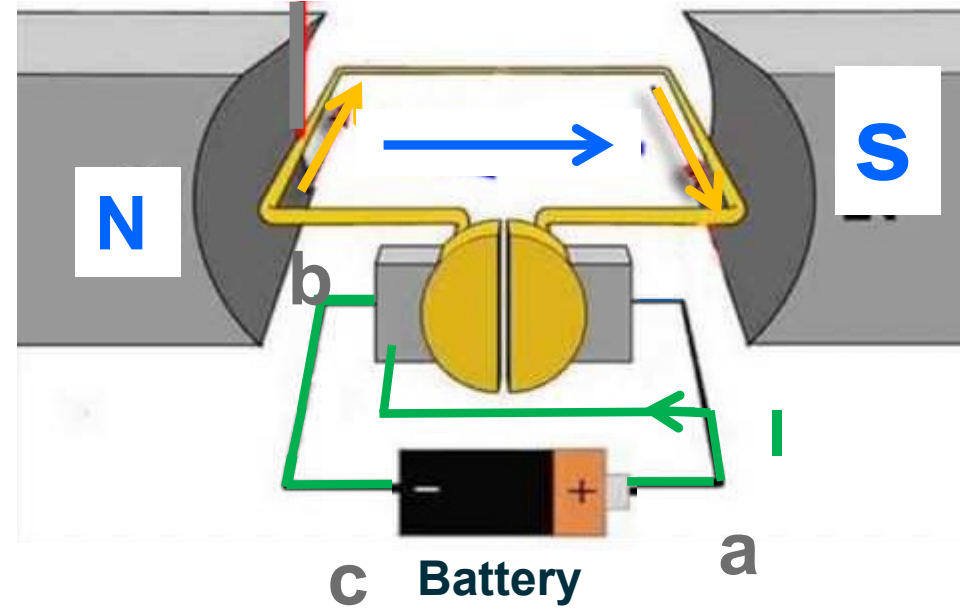
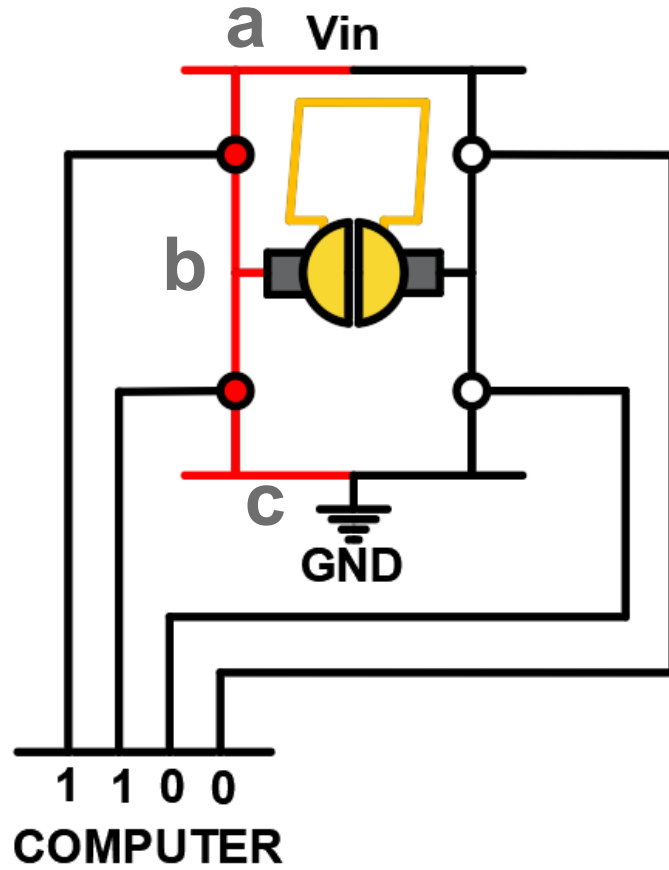
"Shoot thru" (not desirable)

DC Motor control



$$I = V_b / R \quad \Rightarrow \quad R = 0 \text{ Ohm} \quad \Rightarrow \quad I = \text{infinite}$$

DC Motor control



$$I = V_b / R \quad \Rightarrow \quad R = 0 \text{ Ohm} \quad \Rightarrow \quad I = \text{infinite}$$

DC Motor control

- **A DC motor can be driven using a PWM signal**
 - Can run PWM signal through an H-bridge to drive the DC motor
 - PWM behaves most linearly near 50% duty cycle; linearity drops off at the extremes.
 - Arduino Uno supplies 6 PWM output pins

DC Motor specification

Nominal voltage is the input voltage used to establish published specifications. You can apply higher and lower voltages, but watch out not to exceed max. current ratings!

	118749	118750	118751	118752	118753	118754	118755	118756	118757
Motor Data									
1 Assigned power rating				20					
2 Nominal voltage				24.0					
3 No load speed				9660					
4 Stall torque				240					
5 Speed / torque gradient				41.2					
6 No load current				37					
7 Starting current				10300					
8 Terminal resistance				2.32					
9 Max. permissible speed				11000					
10 Max. continuous current				1230					
11 Max. continuous torque				28.4					
12 Max. power output at nominal voltage				58400					
13 Max. efficiency				85					
14 Torque constant				23.2					
15 Speed constant				412					
16 Mechanical time constant				5					
17 Rotor inertia				10.3					
18 Terminal inductance				0.24					
19 Thermal resistance housing-ambient				14					
20 Thermal resistance rotor-housing				3.1					
21 Thermal time constant winding				12					

DC Motor specification

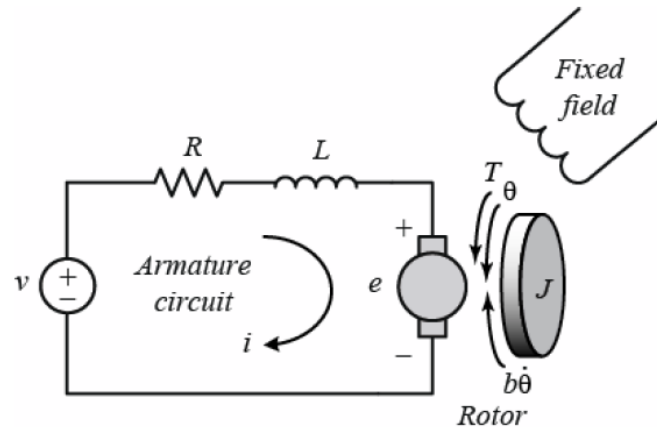
- **Factors to consider when selecting a motor**

While the nominal voltage is not an absolute definition of the operating voltage, it's a pretty good guideline:

- If you apply a voltage far above the nominal voltage, you risk overheating the motor (due to too much current).
- If you apply a voltage far below the nominal voltage, you may not overcome the motor's internal friction (too little current and, hence, too little torque).

DC Motor specification

- DC motors function using two fundamental principles



- **Torque Production:** current-carrying conductor in magnetic field will induce electro-magnetic force acting on the conductor
- **Back EMF:** electric potential will be generated across moving conductor in magnetic field

DC Motor specification

Torque in coil

- **F** force in coil : $F = B * I * L$

- Torque in coil

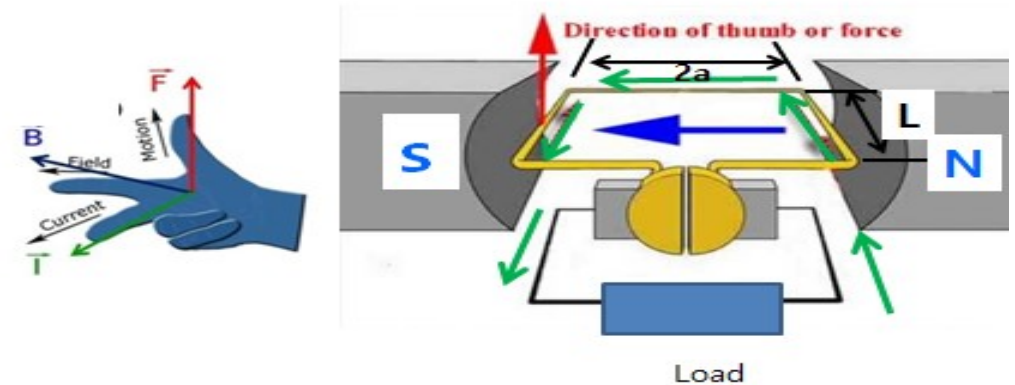
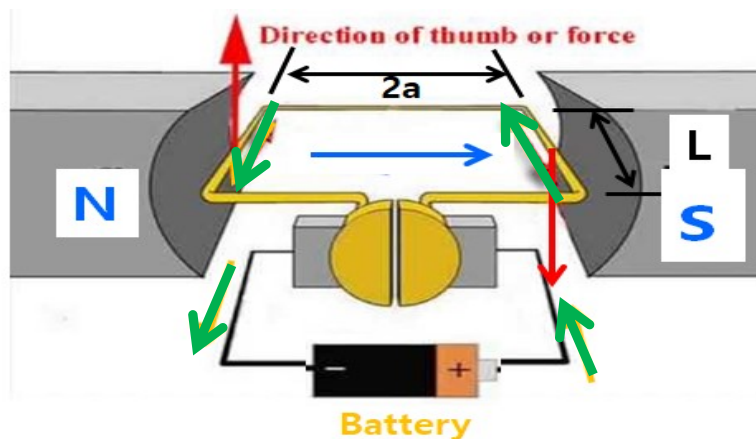
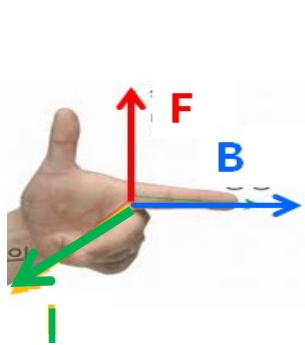
$$\begin{aligned} T &= 2F * a \\ &= 2 * B * I * L * a \\ &= \underline{2a * B * L * I} \\ &= K_T * I \end{aligned}$$

K_T: Torque constant

e Induced voltage:

$$\begin{aligned} e &= B * v * 2L \text{ (2 sides)} \\ &= B * 2a \pi * rps * 2L \\ &= (B * 2a * L) * 2\pi * rps \\ &= \underline{2a * B * L} * \omega \\ &= K_{EMF} * \omega \end{aligned}$$

K_{EMF}: Back-EMF constant



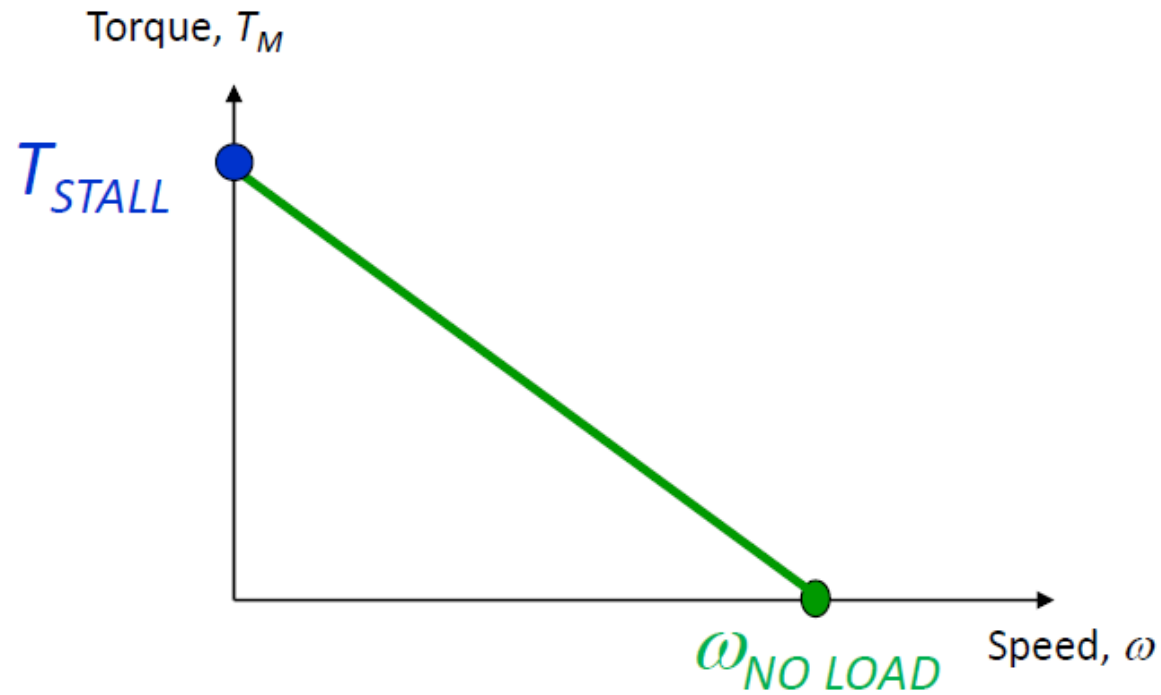
DC Motor specification

$$T_M = K_T \cdot i_a$$

	118749	118750	118751	118752	118753	118754	118755	118756	118757
Motor Data									
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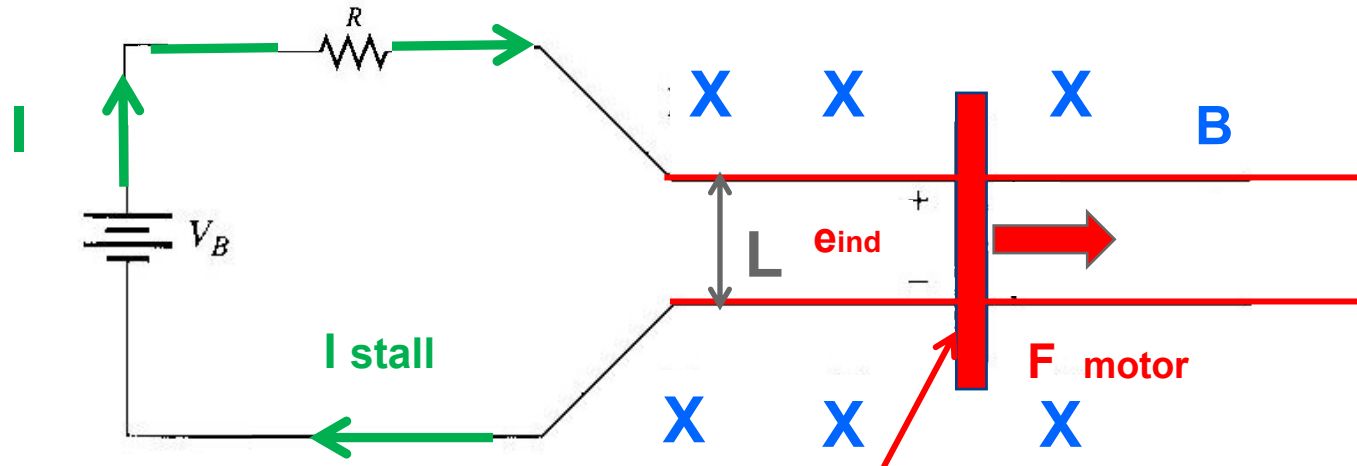
DC Motor specification

- Torque and speed are linearly related for DC motors



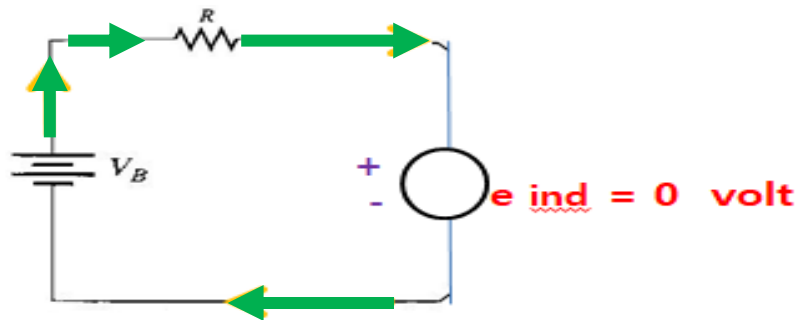
DC Motor specification

- Torque and speed are linearly related for DC motors

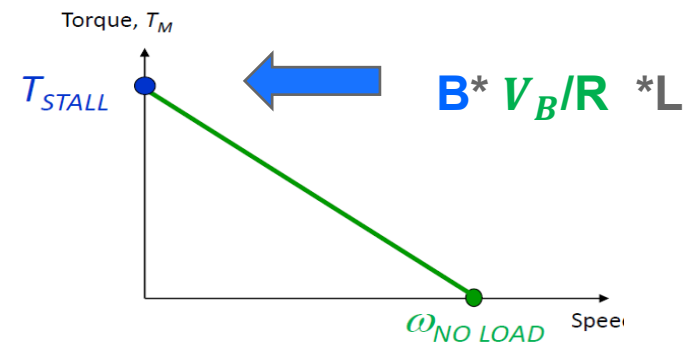


Moving conductor bar: stall (locked)

- Speed = 0 $e_{ind} = 0$ $I_{stall} = V_B / R$ \Rightarrow $F_{stall} = B * I_{stall} * L$

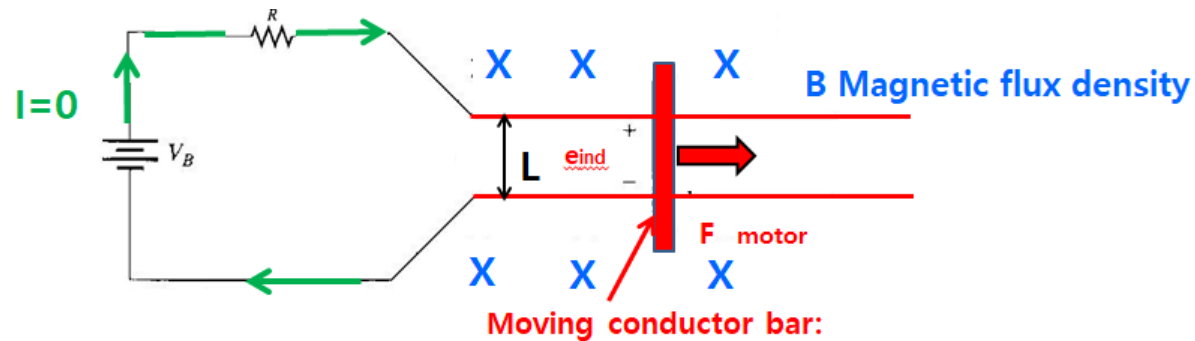


I_{stall} current direction in coil:



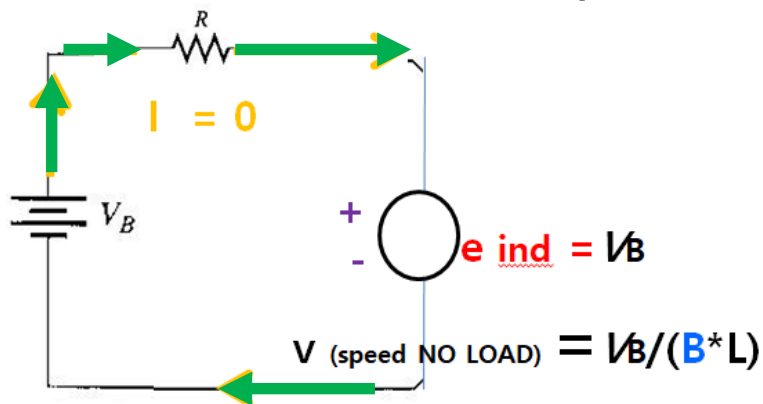
DC Motor specification

- Ω **NO LOAD** : motor speed at no load means no current



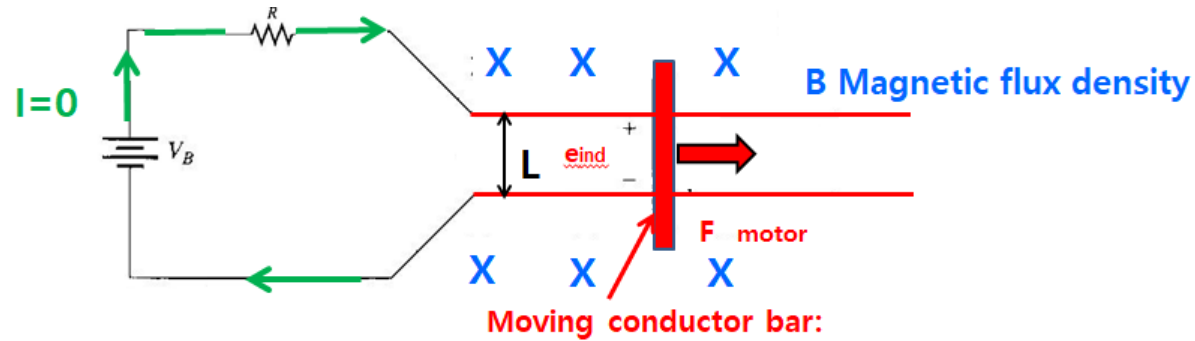
$-F_{\text{motor}}=0$ $I=0$ 이므로 $e_{\text{ind}} = B * v \text{ (speed NO LOAD)} * L = V_B$

$v \text{ (speed NO LOAD)} = V_B / (B * L)$



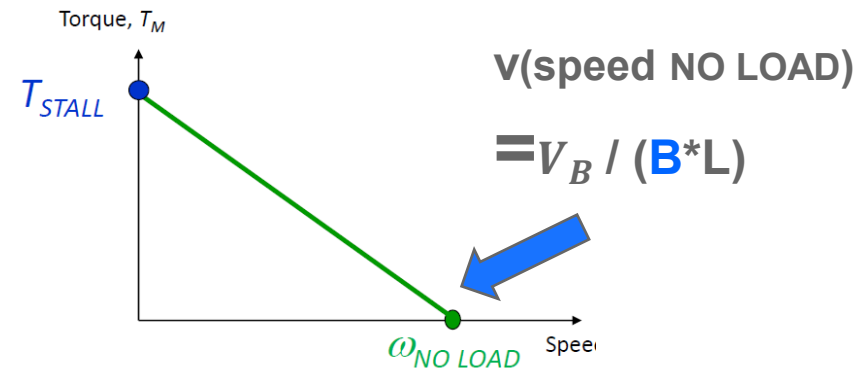
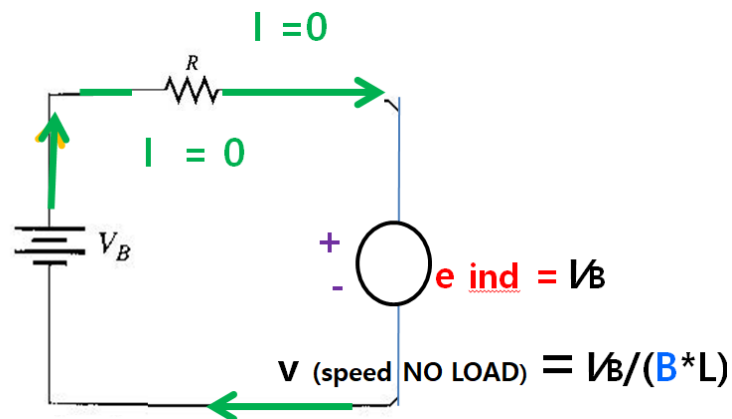
DC Motor specification

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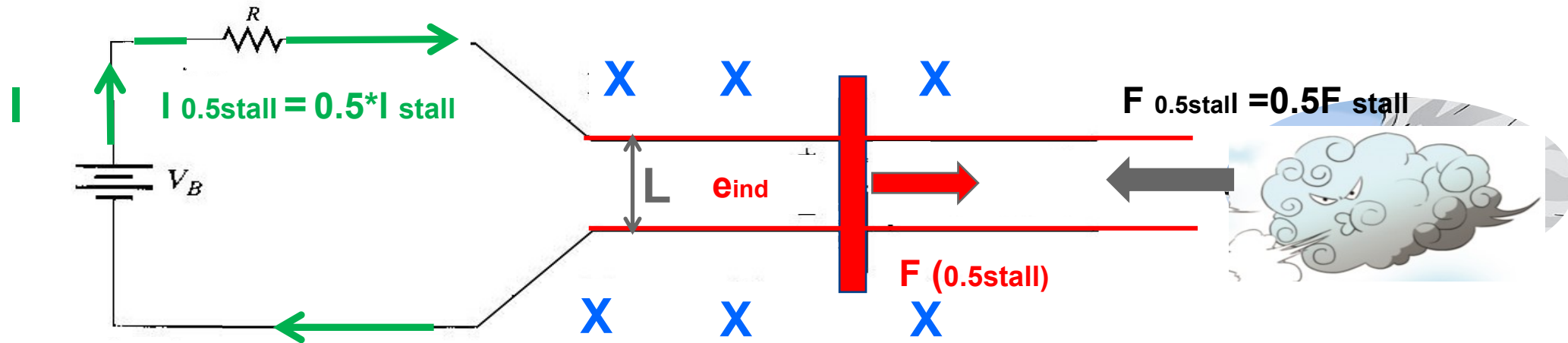
$-F_{motor}=0$ $I=0$ and $e_{ind} = B * v \text{ (speed NO LOAD) } * L = V_B$

$v \text{ (speed NO LOAD) } = V_B / (B * L)$



DC Motor specification

- Ω at $0.5 \cdot T$ stall



$$1) F(0.5stall) = B \cdot I_{0.5stall} \cdot L = B \cdot 0.5 \cdot I_{stall} \cdot L \text{ by Fleming's left hand rule}$$

$$F(0.5stall) = B \cdot 0.5 \cdot V_B / R \cdot L$$

$$2) V_B = R \cdot I_{0.5stall} + e_{ind} \text{ at } F_{0.5stall} = R \cdot 0.5 \cdot I_{stall} + e_{ind} \text{ at } F_{0.5stall}$$

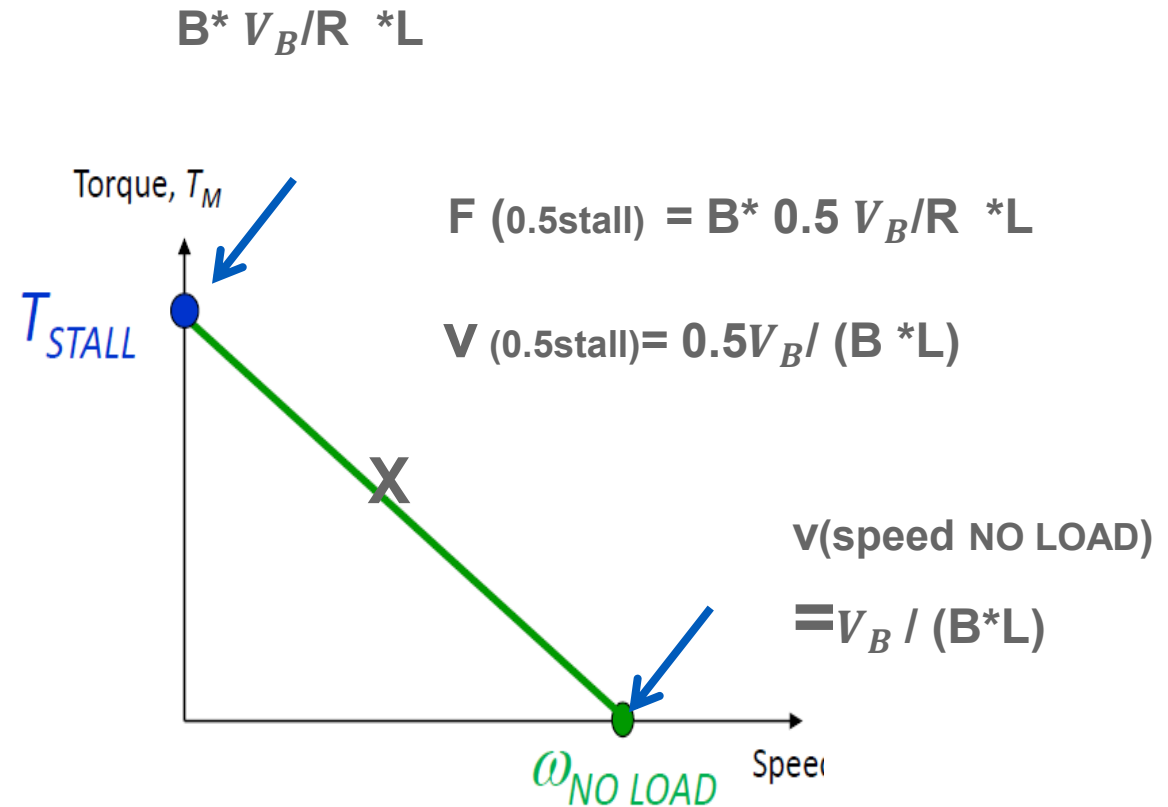
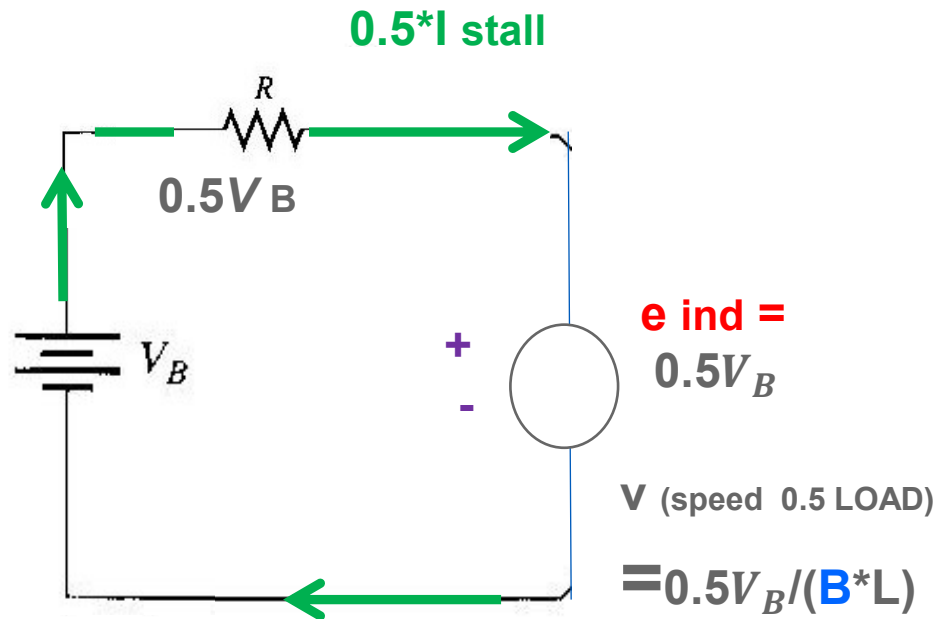
$$e_{ind} \text{ at } F_{0.5stall} = V_B - R \cdot 0.5 \cdot I_{stall} = V_B - R \cdot 0.5 \cdot V_B / R = 0.5 V_B$$

$$B \cdot v(0.5stall) \cdot L = 0.5 V_B \text{ by Fleming's right hand rule}$$

$$v(0.5stall) = 0.5 V_B / (B \cdot L)$$

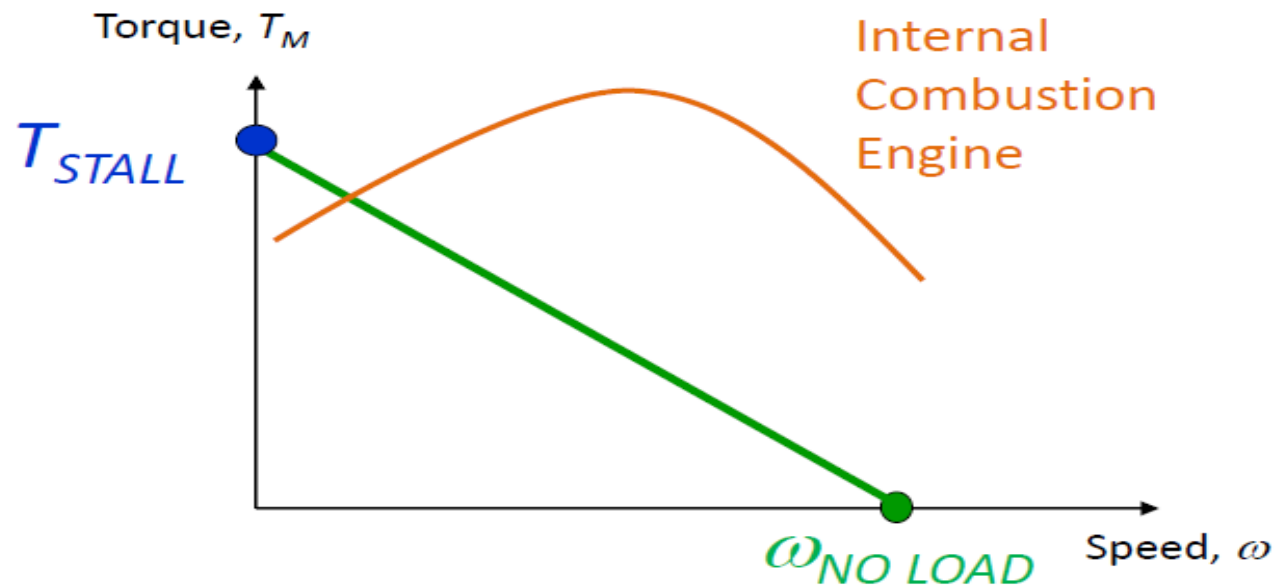
DC Motor specification

- Ω at $0.5 \cdot T$ stall

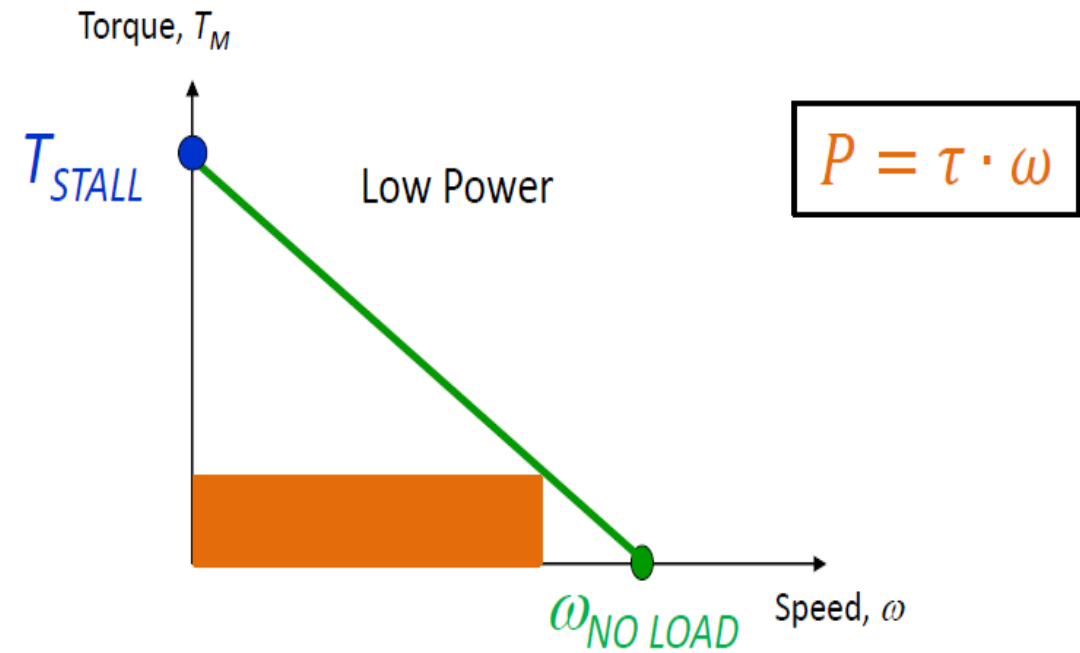
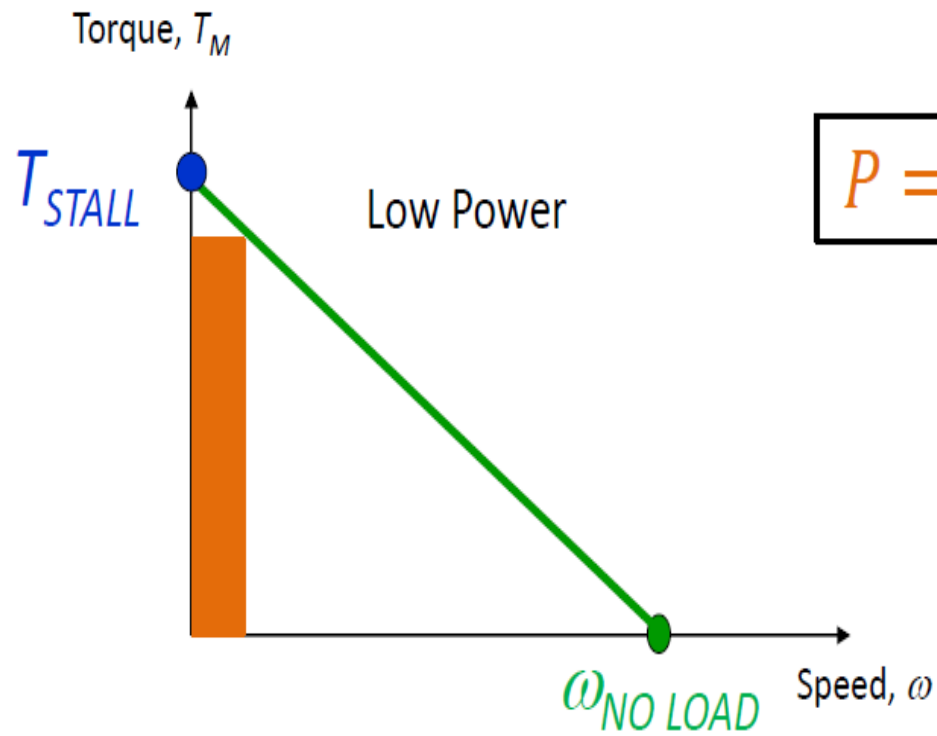


DC Motor specification

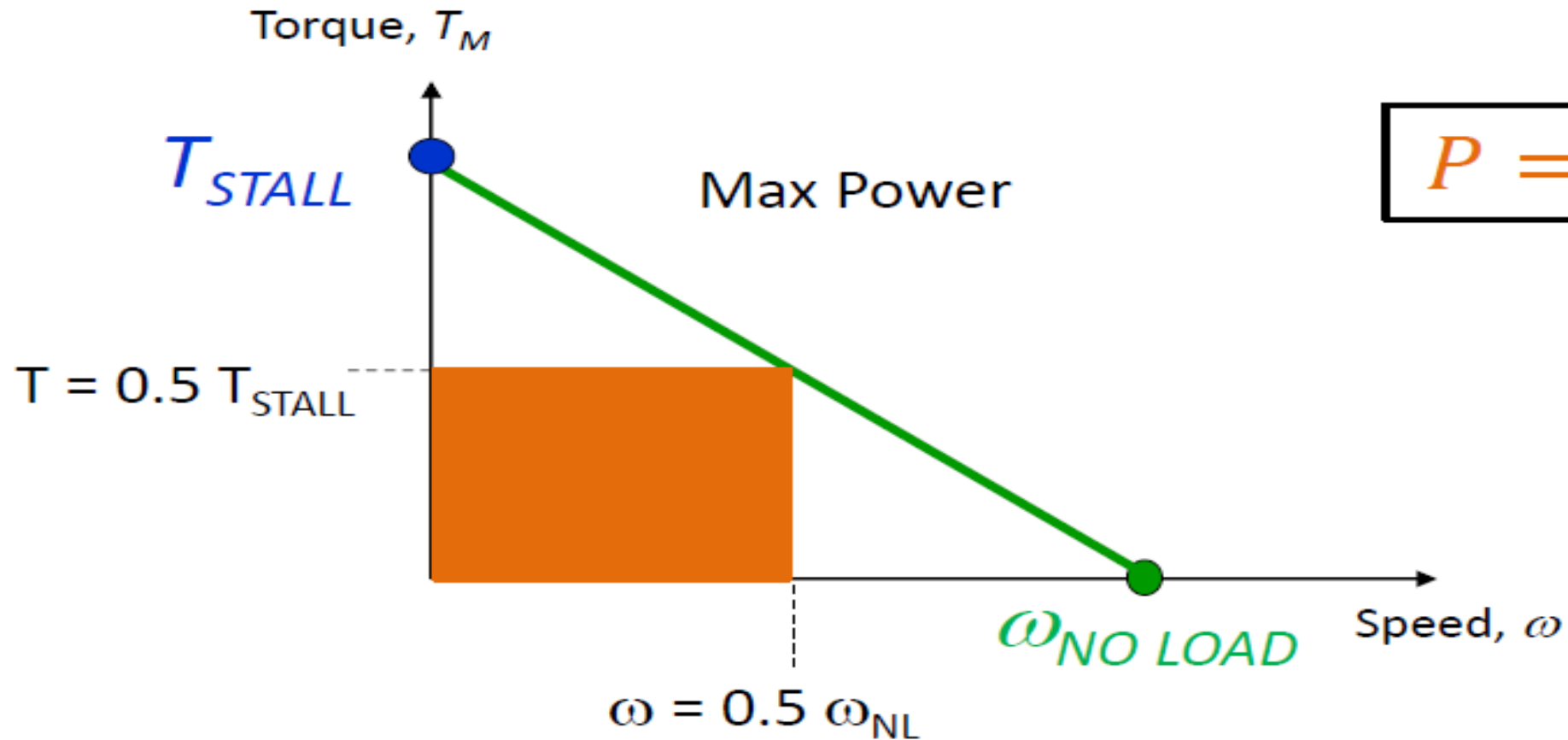
Other actuators have very different speed/torque curves



DC Motor specification

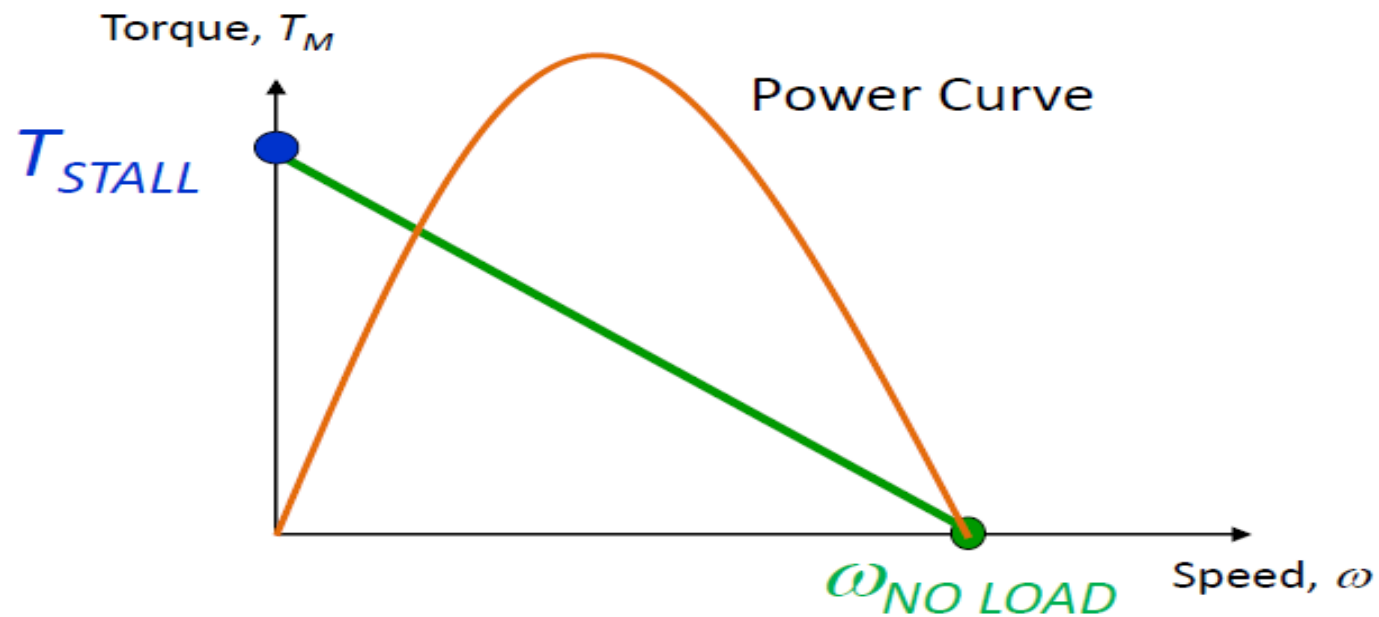


DC Motor specification

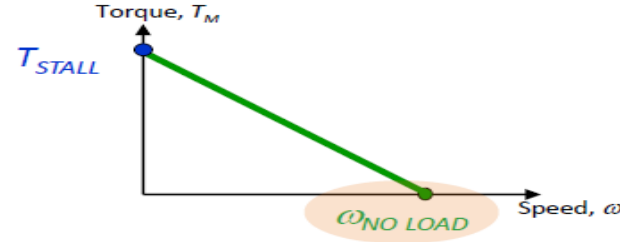


DC Motor specification

Important to remember if you want to optimize your vehicle's acceleration!



DC Motor specification



Motor Data	118749	118750	118751	118752	118753	118754	118755	118756	118757
1 Assigned power rating				20					
2 Nominal voltage				24.0					
3 No load speed				9660					
4 Stall torque				240					
5 Speed / torque gradient				41.2					
6 No load current				37					
7 Starting current				10300					
8 Terminal resistance				2.32					
9 Max. permissible speed				11000					
10 Max. continuous current				1230					
11 Max. continuous torque				28.4					
12 Max. power output at nominal voltage				58400					
13 Max. efficiency				85					
14 Torque constant				23.2					
15 Speed constant				412					
16 Mechanical time constant				5					
17 Rotor inertia				10.3					
18 Terminal inductance				0.24					
19 Thermal resistance housing-ambient				14					
20 Thermal resistance rotor-housing				3.1					
21 Thermal time constant winding				12					

The difference from 9660rpm is mechanical friction and wind load

$$412 * 24(\text{volt}) = 9888 \text{ rpm}$$

DC Motor specification

$$T_M = K_T \cdot i_a$$

Stall torque is a test parameter, not an upper bound on the torque you should expect from your DC motor during continuous operation!

Motor Data	118749	118750	118751	118752	118753	118754	118755	118756	118757
1 Assigned power rating				20					
2 Nominal voltage				24.0					
3 No load speed				9660					
4 Stall torque				240					
5 Speed / torque gradient				41.2					
6 No load current				37					
7 Starting current				10300					
8 Terminal resistance				2.32					
9 Max. permissible speed				11000					
10 Max. continuous current				1230					
11 Max. continuous torque				28.4					
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20 Thermal resistance rotor-housing				3.1					
21 Thermal time constant winding				12					

$$I_{\text{stall}} = V_B / R = 24 / 2.32 = 10.3 \text{ A}$$

How long can you run with a stalled out motor?

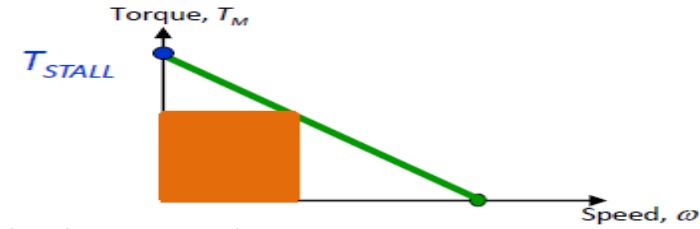
Not long if you're running applying a high load torque!

$$10.3 \text{ A} * 23.2 = 239 \text{ mNm}$$

DC Motor specification

Our theoretical peak power output is:

$$P = \omega T = 2 \pi * \text{rps} * T = 2 \pi * ((9660/2) * 1/60) * (0.24/2) = 60.7W$$



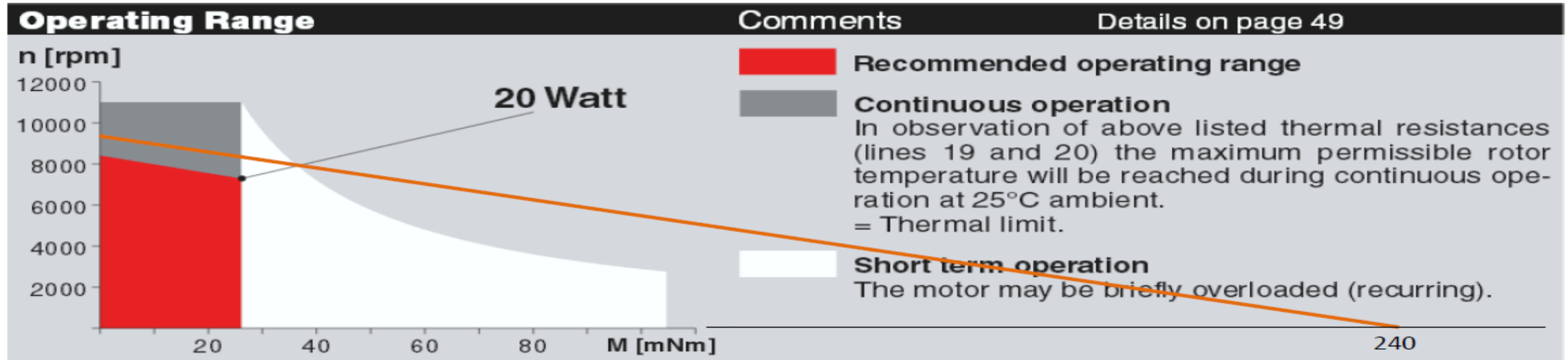
Motor Data	118749	118750	118751	118752	118753	118754	118755	118756	118757
1 Assigned power rating				20					
2 Nominal voltage				24.0					
3 No load speed				9660					
4 Stall torque				240					
5 Speed / torque gradient				41.2					
6 No load current				37					
7 Starting current				10300					
8 Terminal resistance				2.32					
9 Max. permissible speed				11000					
10 Max. continuous current				1230					
11 Max. continuous torque				28.4					
12 Max. power output at nominal voltage				58400					
13 Max. efficiency				85					

The manufacturer is being conservative in assigning a power level for **continuous** operation.

Note that the max. power output listed here is closer to our theoretical calculation

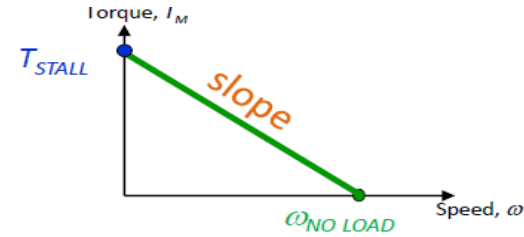
DC Motor specification

This manufacturer is conservative in its recommendations...



This manufacturer recommends keeping the torque at about 1/8th of stall torque for continuous operation! A more common rule of thumb is limiting continuous torque from 1/3 to 1/2 the stall torque. The higher the continuous torque, the closer you need to watch the motor temperature!

DC Motor specification



Motor Data	118749	118750	118751	118752	118753	118754	118755	118756	118757
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16 Mechanical time constant				5					
17 Rotor inertia				10.3					
18 Terminal inductance				0.24					
19 Thermal resistance housing-ambient				14					
20 Thermal resistance rotor-housing				3.1					
21 Thermal time constant winding				12					

Slope = $9660 / 240$
= 40.25

DC Motor specification

How can the motor speed be greater than no load speed?

	118749	118750	118751	118752	118753	118754	118755	118756	118757
Motor Data									
1 Assigned power rating				20					
2 Nominal voltage				24.0					
3 No load speed				9660					
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18 Terminal inductance				0.24					
19 Thermal resistance housing-ambient				14					
20 Thermal resistance rotor-housing				3.1					
21 Thermal time constant winding				12					

If the input voltage is greater than 24V, the speed can be greater than no load speed.
But, do not exceed Max. permissible speed because the commutator and brushes wear more rapidly

DC Motor specification

Torque in coil

- **F** force in coil : $F = B * I * L$

- Torque in coil

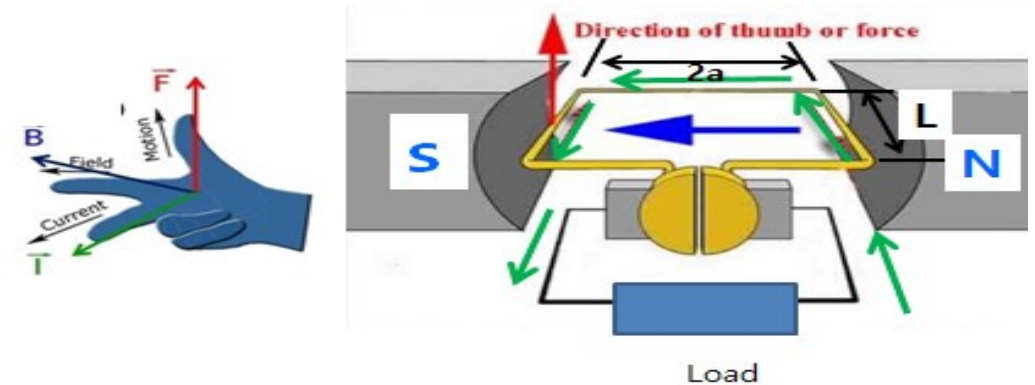
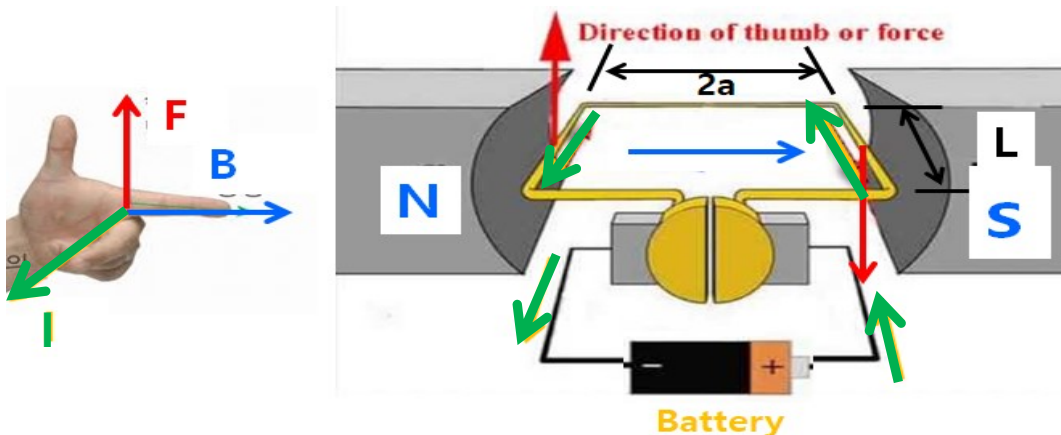
$$\begin{aligned} T &= 2F * a \\ &= 2 * B * I * L * a \\ &= \underline{2a * B * L * I} \\ &= K_T * I \end{aligned}$$

K_T: Torque constant

e Induced voltage:

$$\begin{aligned} e &= B * v * 2L \text{ (2 sides)} \\ &= B * 2a \pi * rps * 2L \\ &= (B * 2a * L) * 2\pi * rps \\ &= \underline{2a * B * L} * \omega \\ &= K_{EMF} * \omega \end{aligned}$$

K_{EMF}: Back-EMF constant



DC Motor specification

This spec sheet gives the inverse of K_{EMF}

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2 Nominal voltage									
3 No load speed									
4 Stall torque									
5 Speed / torque gradient									
6 No load current									
7 Starting current									
8 Terminal resistance									
9 Max. permissible speed									
10 Max. continuous current									
11 Max. continuous torque									
12 Max. power output at nominal voltage									
13 Max. efficiency									
14 Torque constant									
15 Speed constant									
16 Mechanical time constant									
17 Rotor inertia									
18 Terminal inductance									
19 Thermal resistance housing-ambient									
20 Thermal resistance rotor-housing									
21 Thermal time constant winding									

Speed constant

$$-412 = \text{rpm/V}$$

$$-412/60 = \text{rps/V} \quad (1\text{rpm} = 1/60 \text{ rps})$$

Back-EMF constant

$$60/412 = \text{V/rps}$$

$$(60/412) / 2\pi = \text{V}/(\text{rad/s}) \quad (1\text{rps} = 2\pi \text{ rad/s})$$

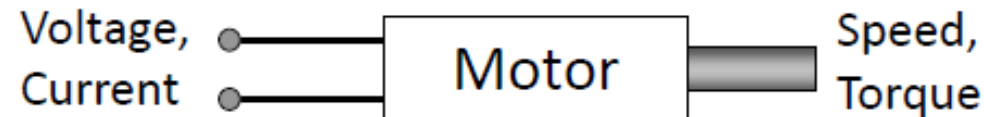
$$23(\text{mV}/\omega)$$

Torque constant = Back-EMF constant

DC Motor operating characteristics

From a *control* view of a DC motor

- We treat the “motor” as a box that is lossless and stores no energy. In reality, power losses exist due to internal resistance and friction.

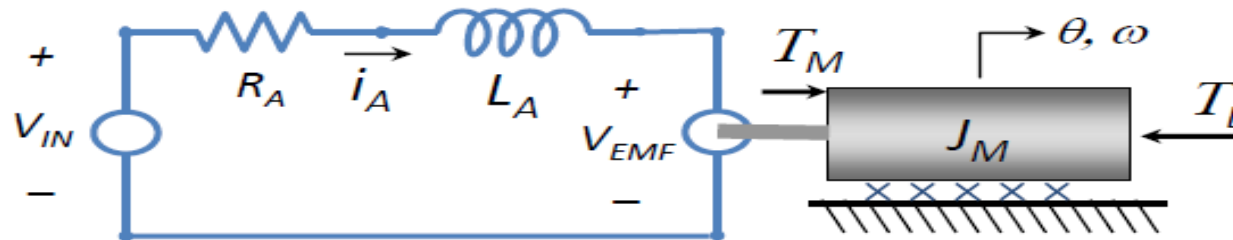


DC Motor operating characteristics

- At steady state, power flow on the mechanical and electrical sides instantaneously match (why?)

$$P = \underbrace{V_{IN} \cdot i}_{\text{Electrical power}} = \underbrace{T \cdot \omega}_{\text{Mechanical power}}$$

$$P = K_{EMF} \cdot \omega \cdot \frac{T}{K_T} = T \cdot \omega$$

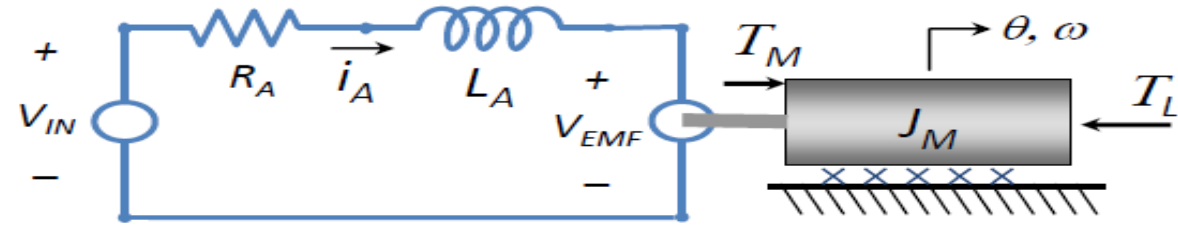


During constant speed operation, the input voltage is equal to the back-EMF generated by the motor, since $T = K_T \cdot i$ and $K_{EMF} = K_T$. Hence, by maintaining a constant supply voltage of $V_{IN} = K_{EMF} \cdot \omega$, we achieve a constant output speed

DC Motor operating characteristics

Equivalent circuit:

$$V_{IN} = i_A \cdot R_A + V_{EMF} + L_A \frac{d}{dt} i_A$$



At steady-state:

$$V_{IN} = i_A \cdot R_A + V_{EMF} = \frac{T_M}{K_T} \cdot R_A + K_{EMF} \cdot \omega$$

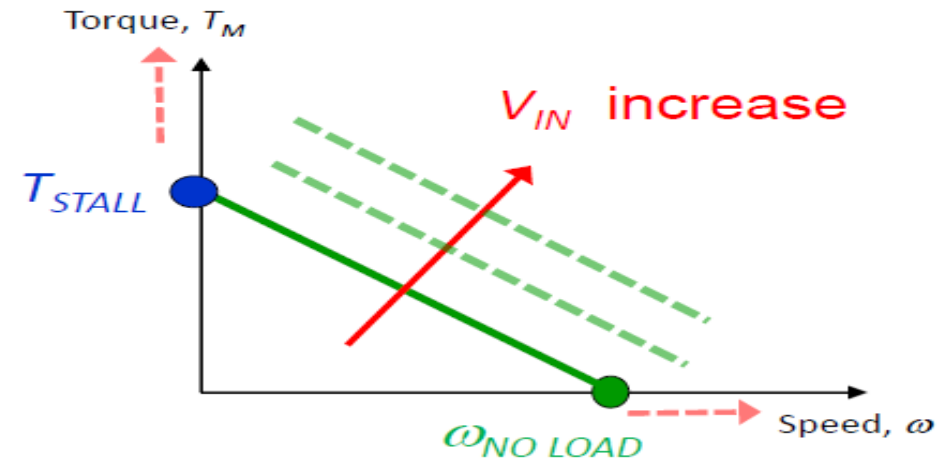
$$\Rightarrow T_M = \frac{K_T}{R_A} (V_{IN} - K_{EMF} \omega)$$

- Stall Torque ($\omega = 0$):

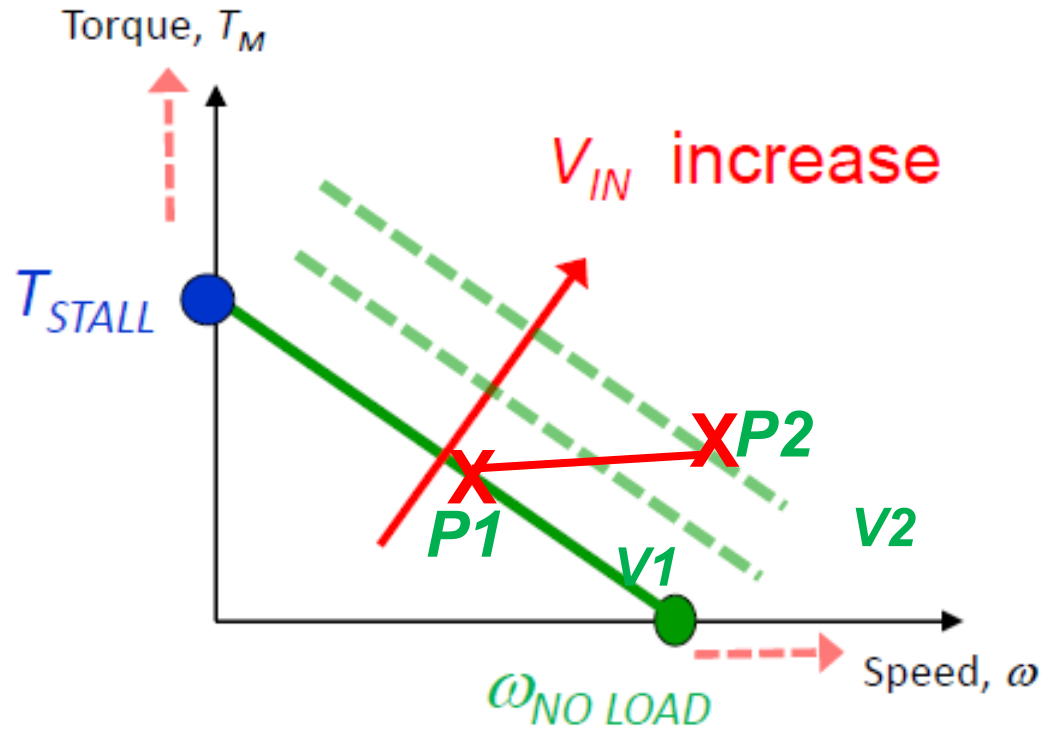
$$T_{STALL} = \frac{K_T}{R_A} \cdot V_{IN}$$

- No-Load Speed ($T_M = 0$):

$$\omega_{NO\ LOAD} = \frac{V_{IN}}{K_{EMF}}$$



DC Motor operating characteristics



93

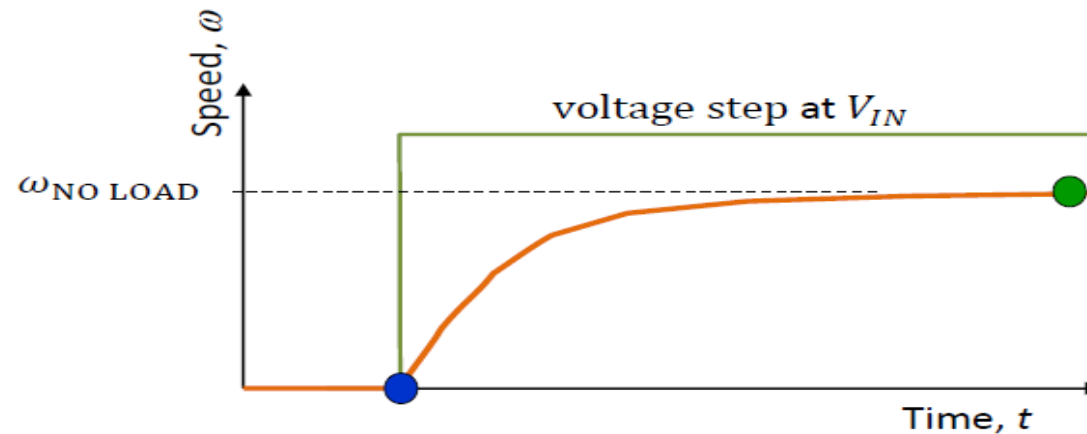
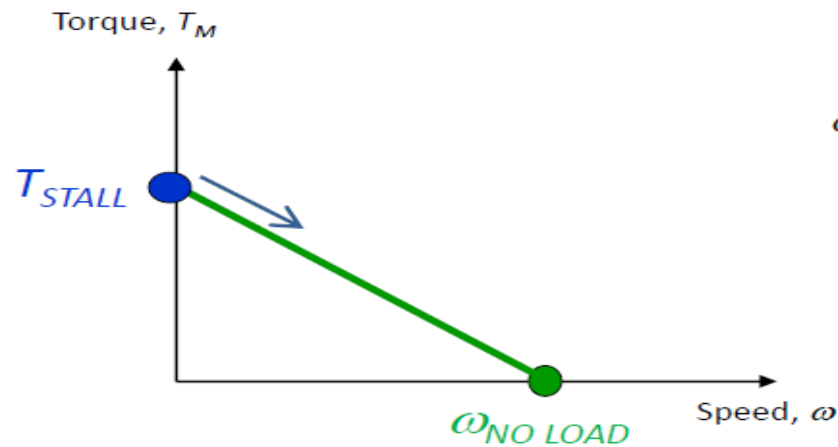
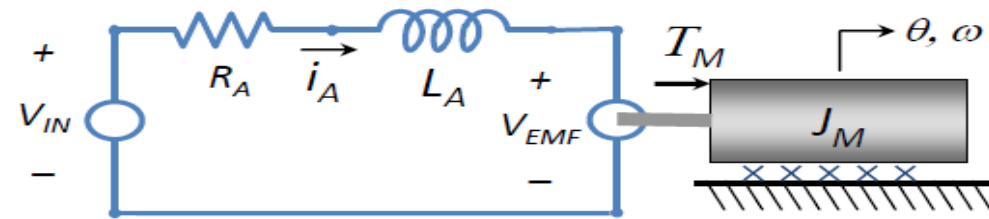
$V_1 \rightarrow V_2$ \rightarrow $P_1 \rightarrow P_2$

means same torque (same current/same winding loss)
with higher speed (more power with same current)

DC Motor operating characteristics

- No load

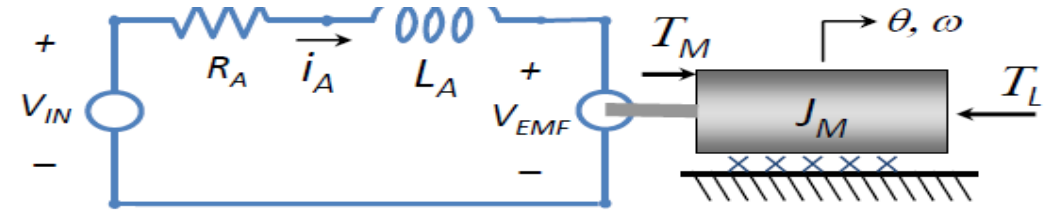
- For a step voltage input, rapid acceleration occurs as motor starts from a standstill. As more and more back EMF is generated, the motor torque decreases, and acceleration slows, with the speed eventually settling at $\omega_{NO\ LOAD}$.



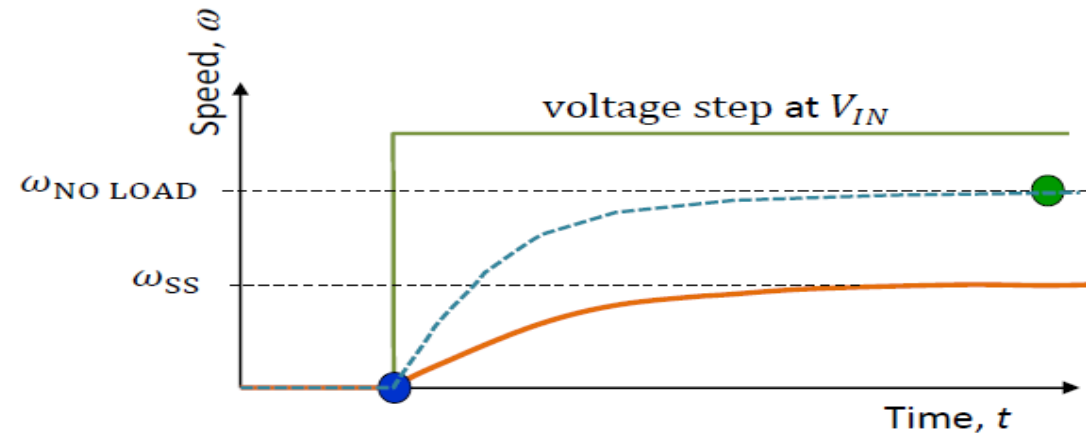
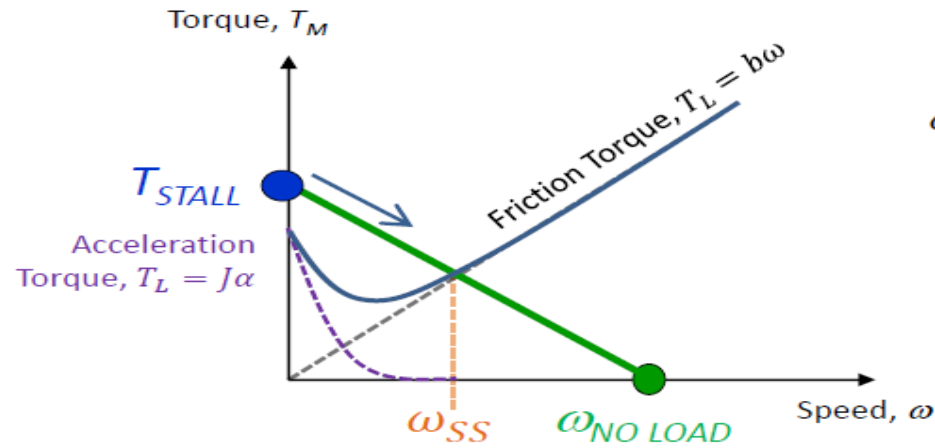
DC Motor operating characteristics

- With load

Q: Does the load on the mechanical side affect the steady-state speed?



$$T_L = J\alpha + b\omega$$



DC Motor operating characteristics

The mechanical time constant tells us the time it takes an unloaded motor to reach 63% of its no-load speed under a constant voltage, when starting from rest

	118749	118750	118751	118752	118753	118754	118755	118756	118757
Motor Data									
1 Assigned power rating				20					
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18 Terminal inductance				0.24					
19 Thermal resistance housing-ambient				14					
20 Thermal resistance rotor-housing				3.1					
21 Thermal time constant winding				12					

DC Motor operating characteristics

Why doesn't the no load current go to zero?

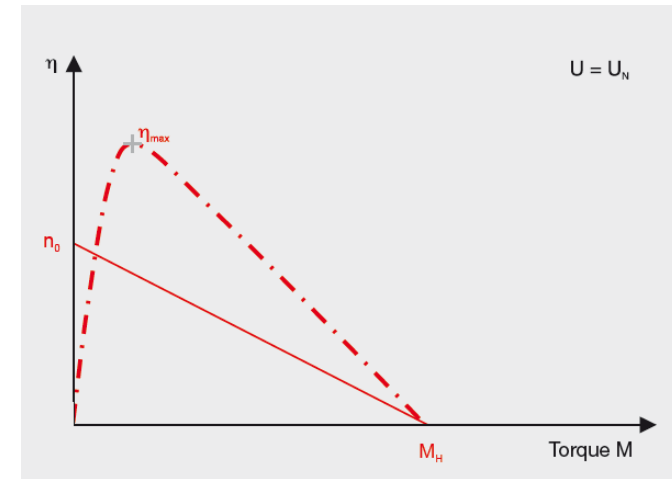
	118749	118750	118751	118752	11
Motor Data					
1 Assigned power rating				20	
2 Nominal voltage				24.0	
3 No load speed				9660	
4 Stall torque				240	
5 Speed / torque gradient				41.2	
6 No load current				37	
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21 Thermal time constant winding				12	

**Because of
mechanical friction loss
and wind loss load**

DC Motor operating characteristics

Maximum efficiency in converting electrical power to mechanical power usually occurs at high speeds and low torques

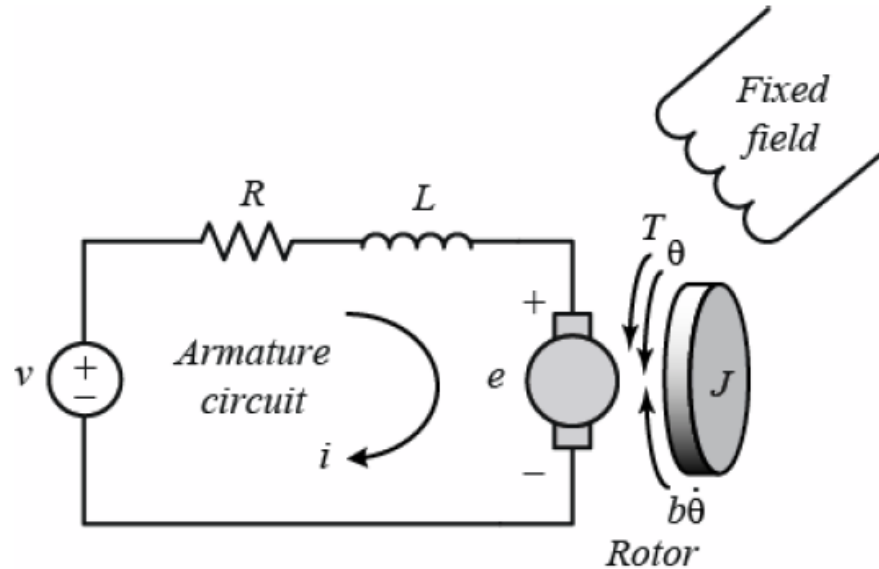
Motor Data	118749	118750	118751	118752	118753
1 Assigned power rating				20	
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15 Speed constant				412	
16 Mechanical time constant				5	



Because major losses of motor is copper winding loss by current
Less torque → less current

But mechanical loss will be increase by higher higher speed

DC Motor operating characteristics



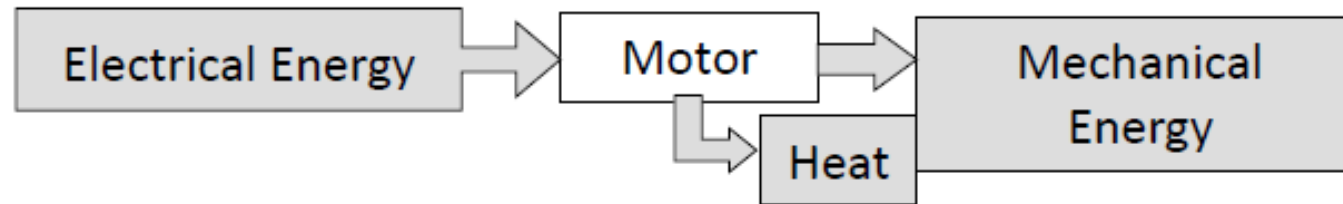
$$V_{EMF} = K_{EMF} \cdot \omega$$

$$T_M = K_T \cdot i_A$$

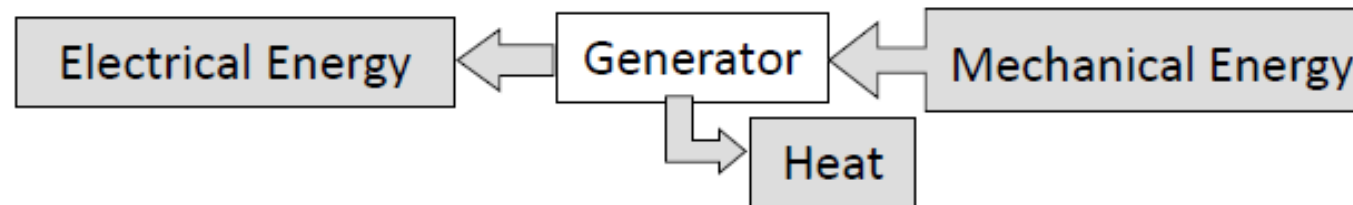
- Voltage (velocity) mode: control voltage across winding
- Current (torque) mode: control current through winding

DC Motor operating characteristics

- Motor – Electrical power in → mechanical power out.



- Generator – Mechanical power in → electrical power out.
 - ❖ When operated for its output power, it is called a generator.



DC Motor operating characteristics

- **Factors to consider when selecting a motor**

We often want more torque, but we can't increase torque without increasing current. However, *too much current will destroy the motor windings!* Thus, we must take a look at the following constraints when selecting a DC motor:

- Torque limits
- Current limits
- Rotational speed limits

DC Motor operating characteristics

- **Factors to consider when selecting a motor**

Even if we don't burn out the windings, we can overheat the motor:

- Heat is primary performance limitation for DC motors
- Sources:
 - Electrical losses in windings
 - Eddy current
 - Hysteresis
 - Friction
 - Brush contact resistance
- Transient temperature limit is very different from steady-state limits (what is on the specifications)

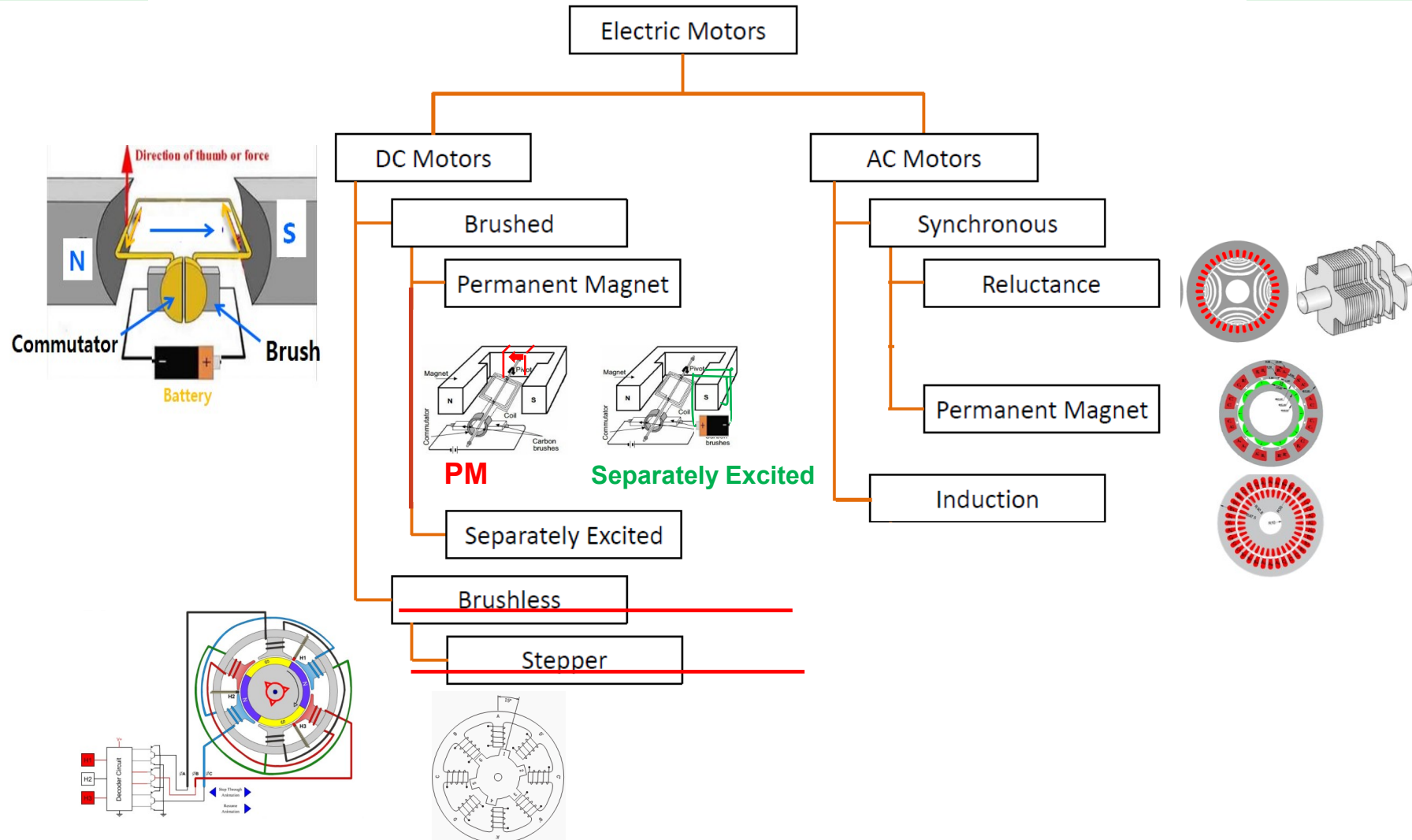
DC Motor operating characteristics

- **Factors to consider when selecting a motor**

If you need more torque, however, do not fear...

As we will see shortly, you can trade speed for torque using a gearbox!

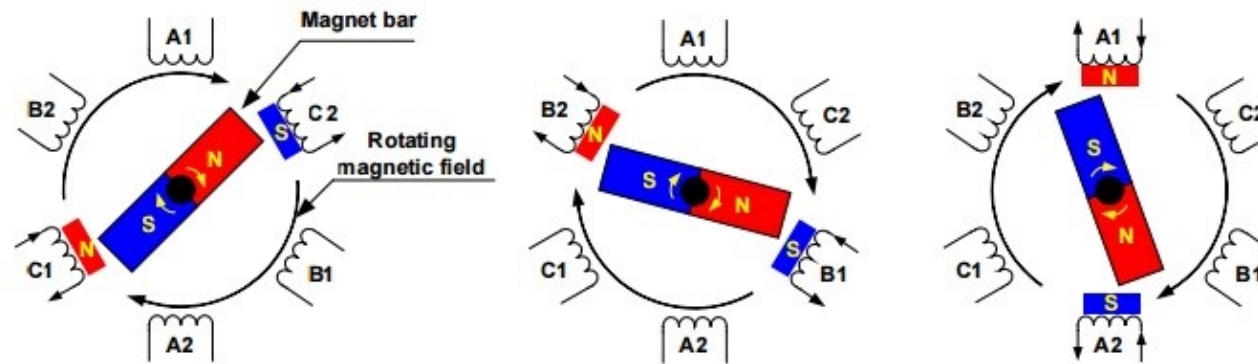
Classification of motors



<https://electricalbaba.com/brushless-dc-bldc-motor/>

Classification of motors

- BLDC (brushless DC) motor



http://4.bp.blogspot.com/-9q50-d2NK_M/VztxoGsaBbl/AAAAAAAAA4o/vG_S193LnB0YFYt3OgUijUons63QD-0oACK4B/s1600/BLDC-brushless-dc-motor-animation.gif

Compared with a brushed DC motor, the has many advantages:

Higher efficiency and reliability

Lower acoustic noise

Smaller and lighter

Greater dynamic response

Better speed versus torque characteristics

Higher speed range

Longer life

Classification of motors

- Stepper motor

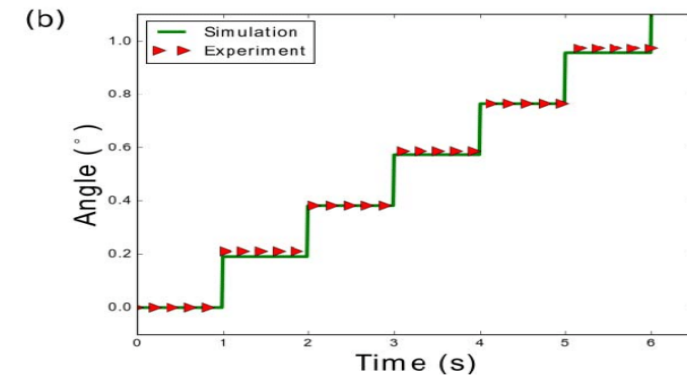
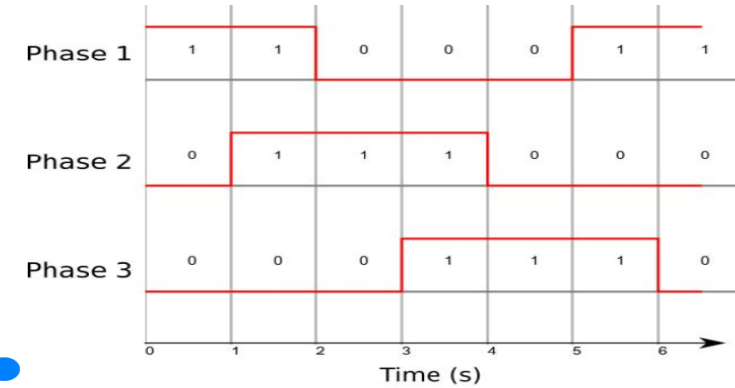
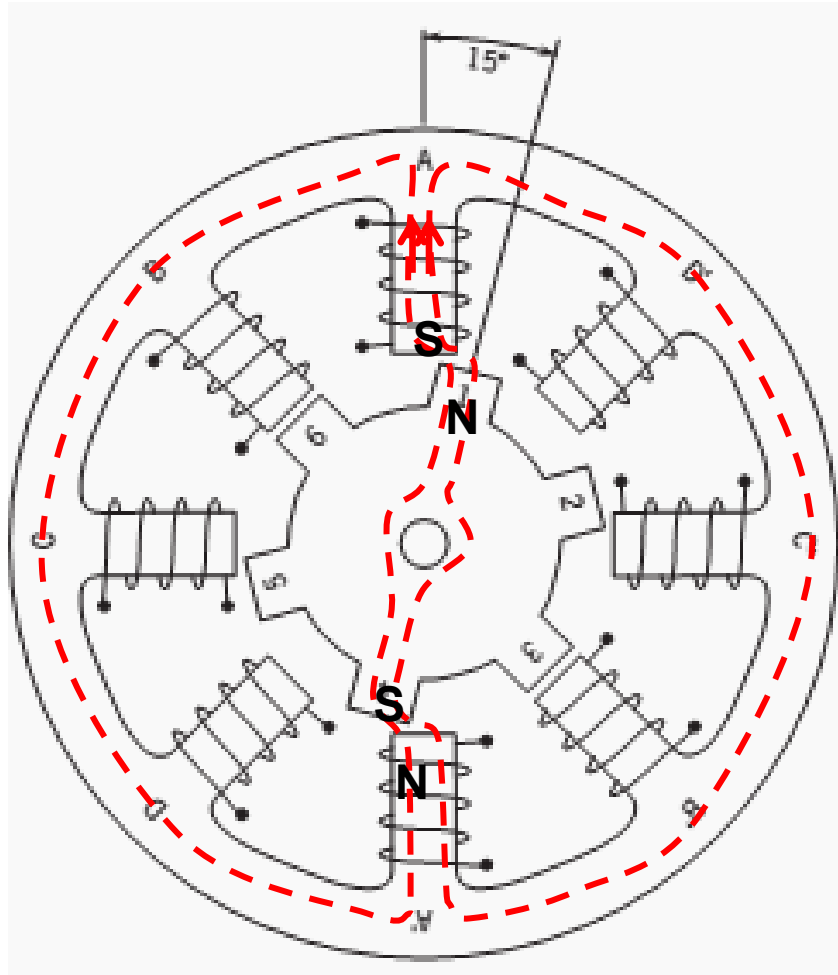


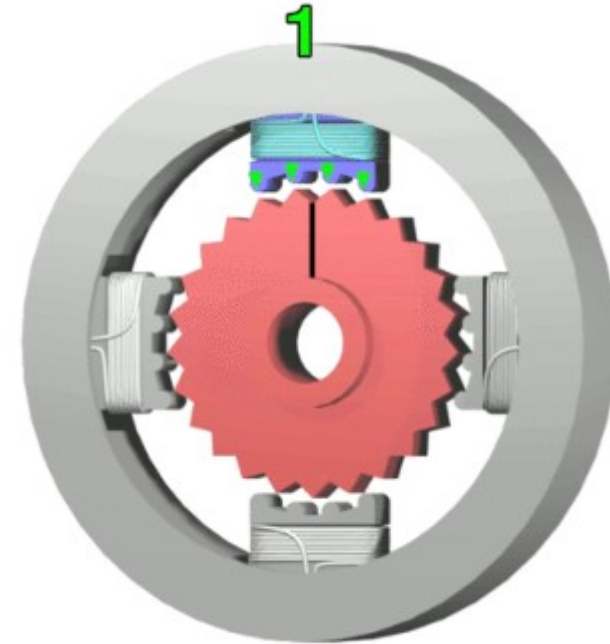
Illustration of stepper motor driving principle: (a) Driving half-stepping voltage waveform for driving rotary actuator, and (b) experimental plots showing the rotational stepping motion of the motor with an angle of 0.2° per step.

Classification of motors

- Stepper motor

A stepper motor, also known as step motor or stepping motor, is a brushless DC electric motor that divides a full rotation into a number of equal steps. The motor's position can then be commanded to move and hold at one of these steps without any position sensor for feedback (an open-loop controller), as long as the motor is carefully sized to the application in respect to torque and speed.

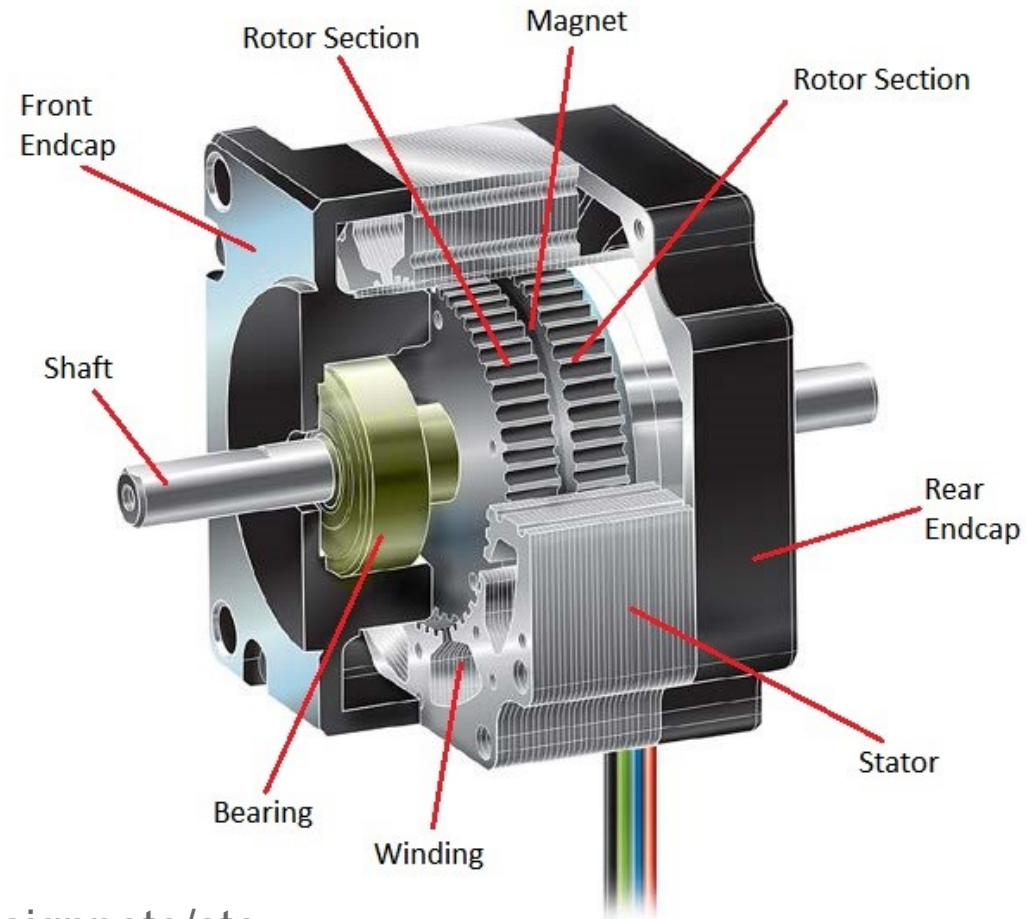
Switched reluctance motors are very large stepping motors with a reduced pole count, and generally are closed-loop commutated.



https://en.wikipedia.org/wiki/Stepper_motor#/media/File:StepperMotor.gif

Classification of motors

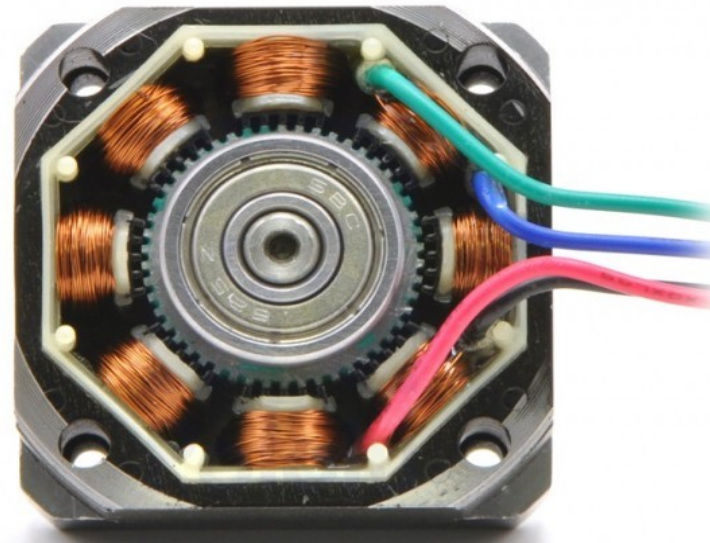
- Stepper motor



<https://www.islproducts.com/designnote/stepper-motor-fundamentals/>

Classification of motors

- Stepper motor



www.pololu.com

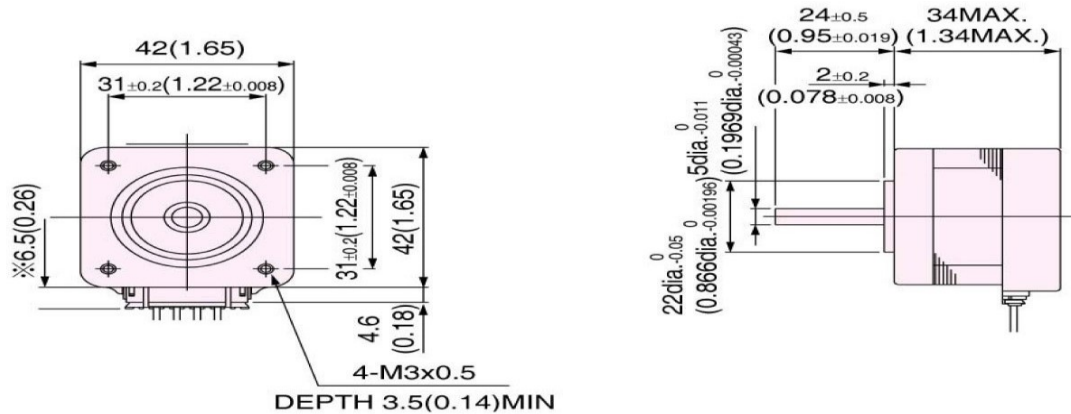
<https://www.youtube.com/watch?v=eyqwLiowZiU>

<https://www.youtube.com/watch?v=bkqoKWP4Oy4>

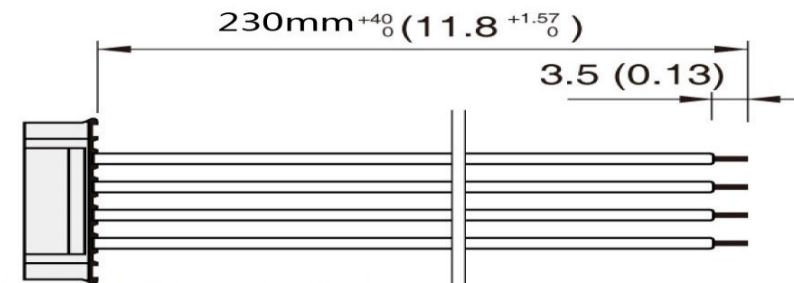
Classification of motors

- Stepper motor : specification

MODEL	SINGLE SHAFT	-951
DRIVE METHOD		BI-POLAR
NUMBER OF PHASES		2
STEP ANGLE	deg./step	1.8
VOLTAGE	V	12
CURRENT	A/PHASE	0.35
WINDING RESISTANCE	/PHASE	34
INDUCTANCE	mH/PHASE	4.3
HOLDING TORQUE	mN • m	200
	oz • in	28
DETENT TORQUE	mN • m	11.8
	oz • in	2.1
ROTOR INERTIA	g • cm ²	38
	oz • in ²	0.21
WEIGHTS	g	200
	lb	0.57
INSULATION CLASS		JIS Class E (120°C 248°F) (UL VALUE : CLASS B-130°C 266°F)
INSULATION RESISTANCE		500VDC 100MΩmin.
DIELECTRIC STRENGTH		500VAC 50HZ 1min.
OPERATING TEMP. RANGE	°C	0 to 50
ALLOWABLE TEMP. RISE	deg.	70

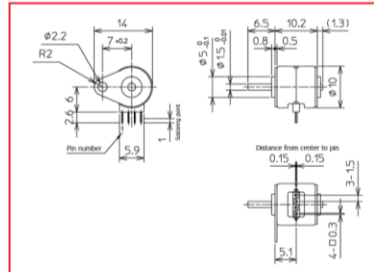


BI-POLAR



DC Motor operating characteristics

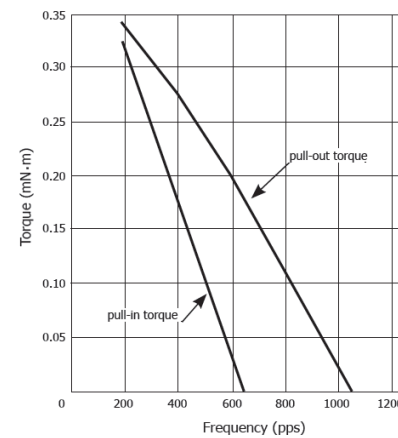
- Stepper motor : specification



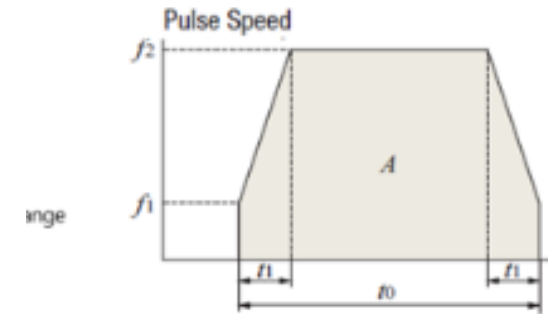
Specifications

Specification	Unit	PFC10-20R6
Type of Winding		Bipolar
Excitation Mode*		Full step (2-2)
Steps/Revolution		20
Step Angle	°	18
Holding Torque	mN·m	1.0
Rated Voltage	V	2.7
Rated Current	mA/phase	135
Resistance	Ω / ϕ	20
Inductance	mH / ϕ	3.2
Coil		R
Starting Pulse Rate	pps	960
Slewing Pulse Rate	pps	1600
Rotor Inertia	kg·m ²	0.03×10^{-7}
Operating Temp. Range	°C	-10 to +50
Storage Temp. Range	°C	-30 to +80
Insulation Class		E
Temperature Rise	K	70
RoHS Compliant		Yes
Weight	g	5

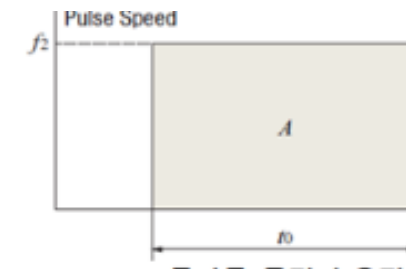
Torque Curve Characteristics



Pin	Coil Phase
1	4 ϕ B
2	1 ϕ A

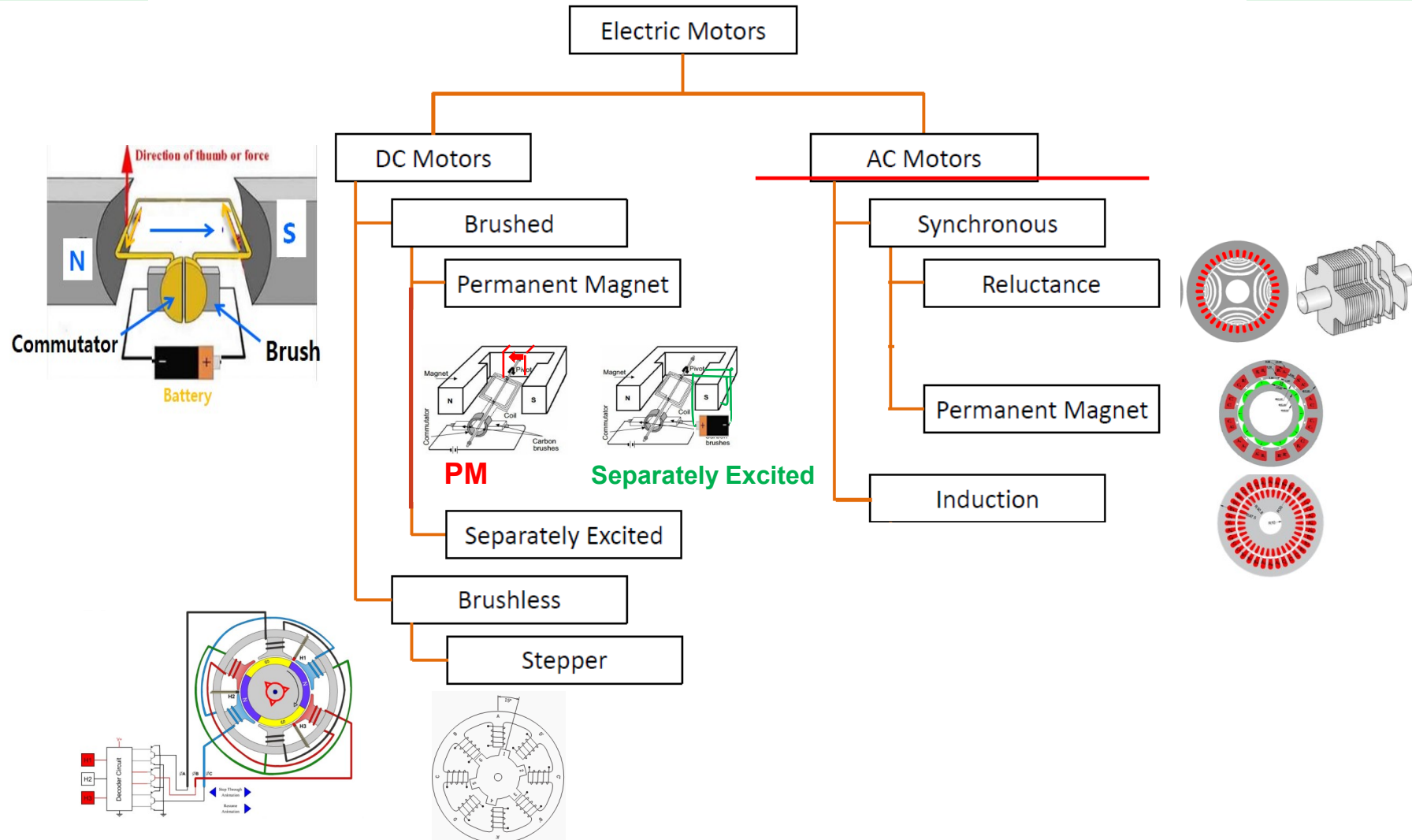


Operation for pull-out torque



Operation for pull-in torque

Classification of motors



<https://electricalbaba.com/brushless-dc-bldc-motor/>

Classification of motors

▪ AC motors: Generation of 3 phase AC current

When these windings are kept stationary, and the magnetic field is rotated as shown in the figure A below or when the windings are kept stationary, and the magnetic field is rotated as shown below in figure B, an emf is induced in each winding. The magnitude and frequency of these EMFs are same but are displaced apart from one another by an angle of 120 degrees.

In a 3 phase system, there are three equal voltages or EMFs of the same frequency having a phase difference of 120 degrees.

These voltages can be produced by a three-phase AC generator having three identical windings displaced apart from each other by 120 degrees electrical.

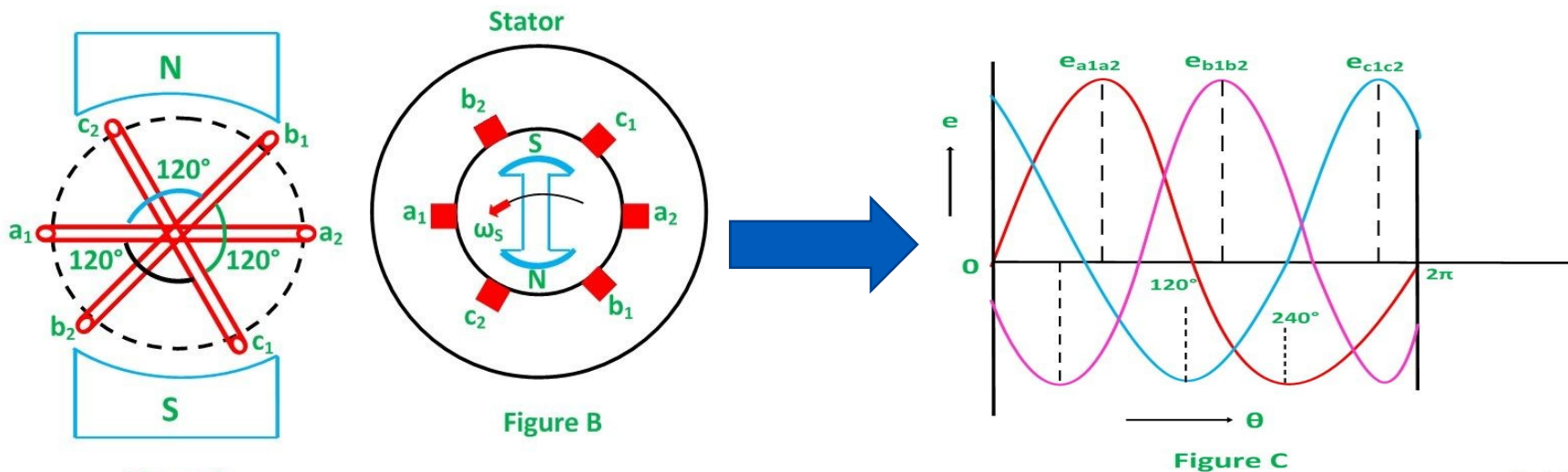


Figure A

Circuit Globe

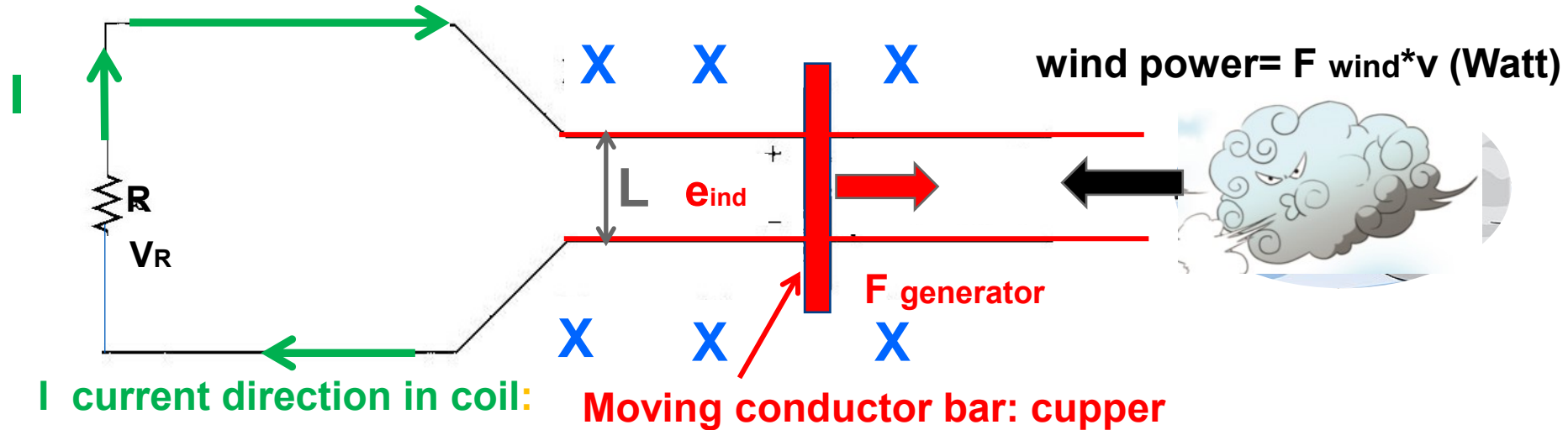
<https://circuitglobe.com/generation-of-3-phase-power-in-3-phase-circuits.html>

Circuit Globe

Classification of motors

- Induced voltage and magnetic flux

B: magnetix flux density



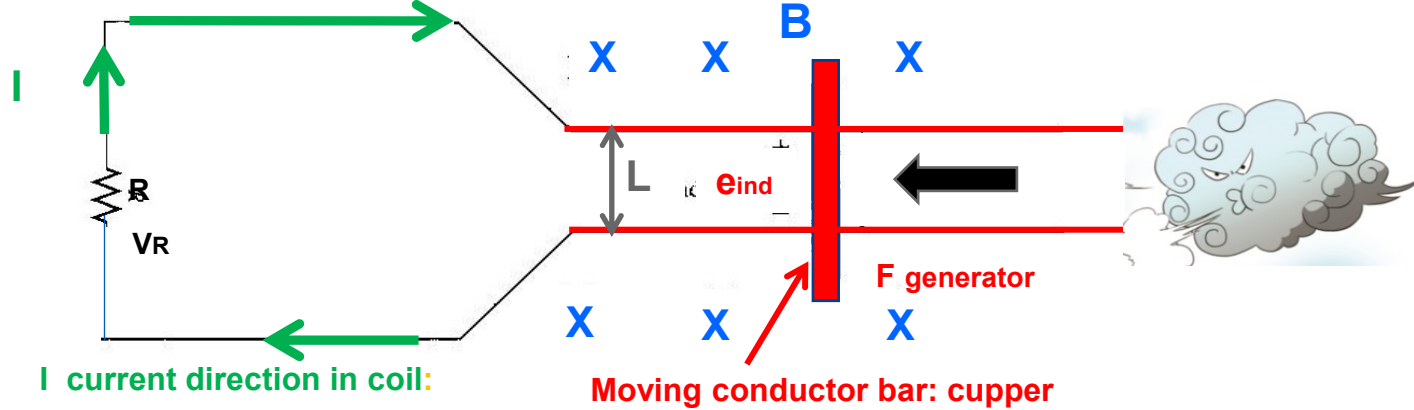
- Fleming's right hand rule: **e induced voltage: $e_{ind} = B \cdot v \cdot L$** in moving conductor bar
- $v(\text{speed}) = dx / dt$ **$e_{ind} = B \cdot (dx / dt) \cdot L = B \cdot (dx) \cdot L / dt = d\Phi / dt$**
- Here Φ is magnetic flux in coil loop

!!! Remember $e_{ind} = B \cdot v \cdot L$ (Fleming's right hand rule) = $d\Phi / dt$

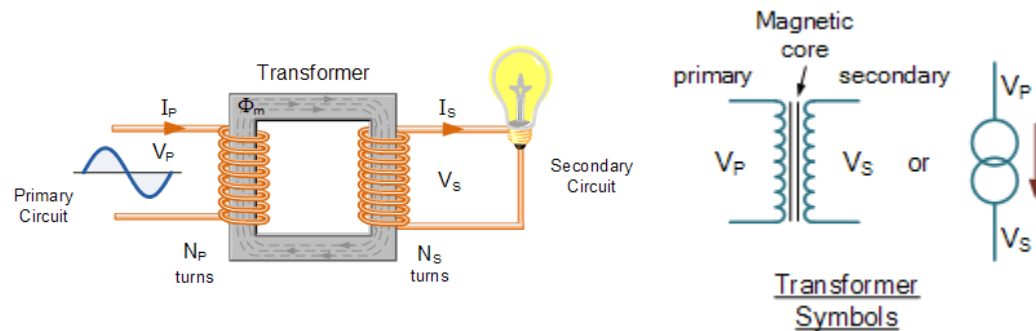
Classification of motors

- Induced voltage by magnetic flux change

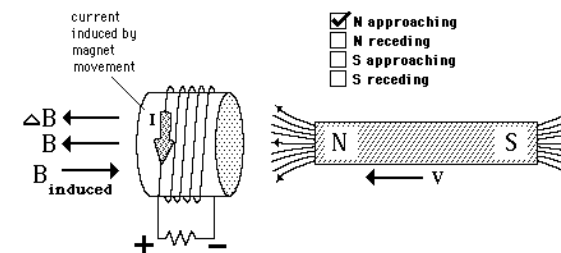
- Induced voltage 1: by speed



- Induced voltage 2: by AC

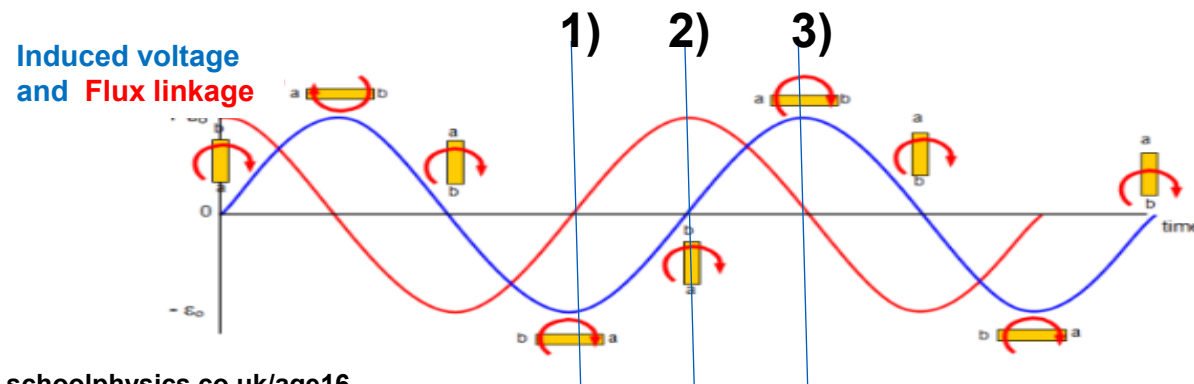
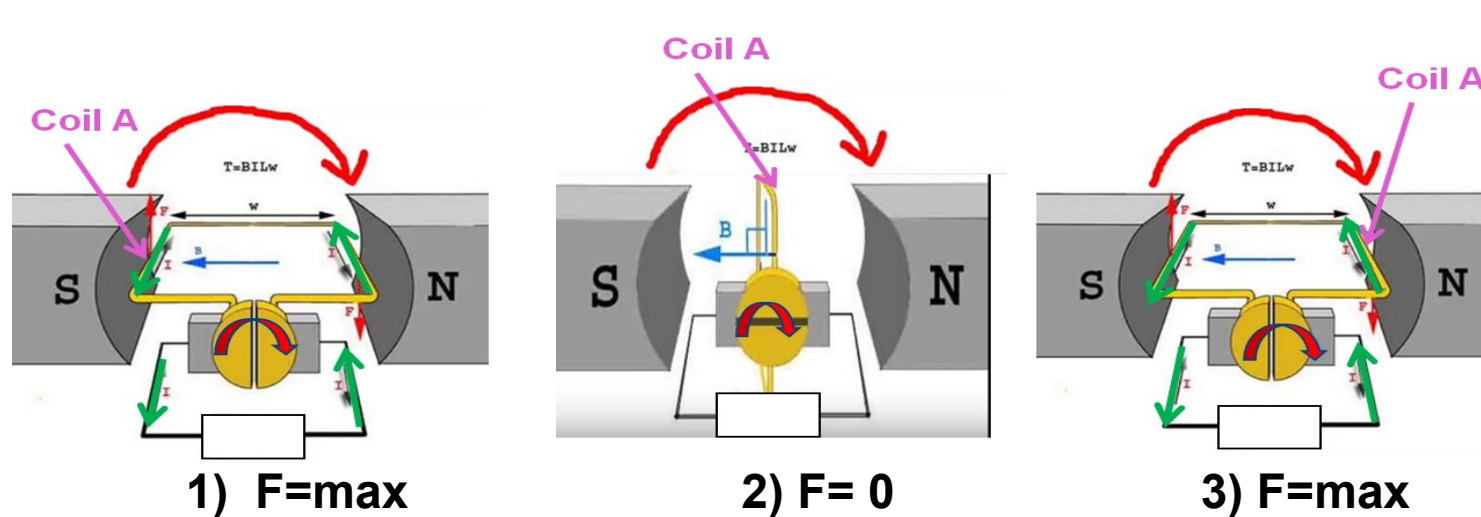


- Induced voltage 3: by speed

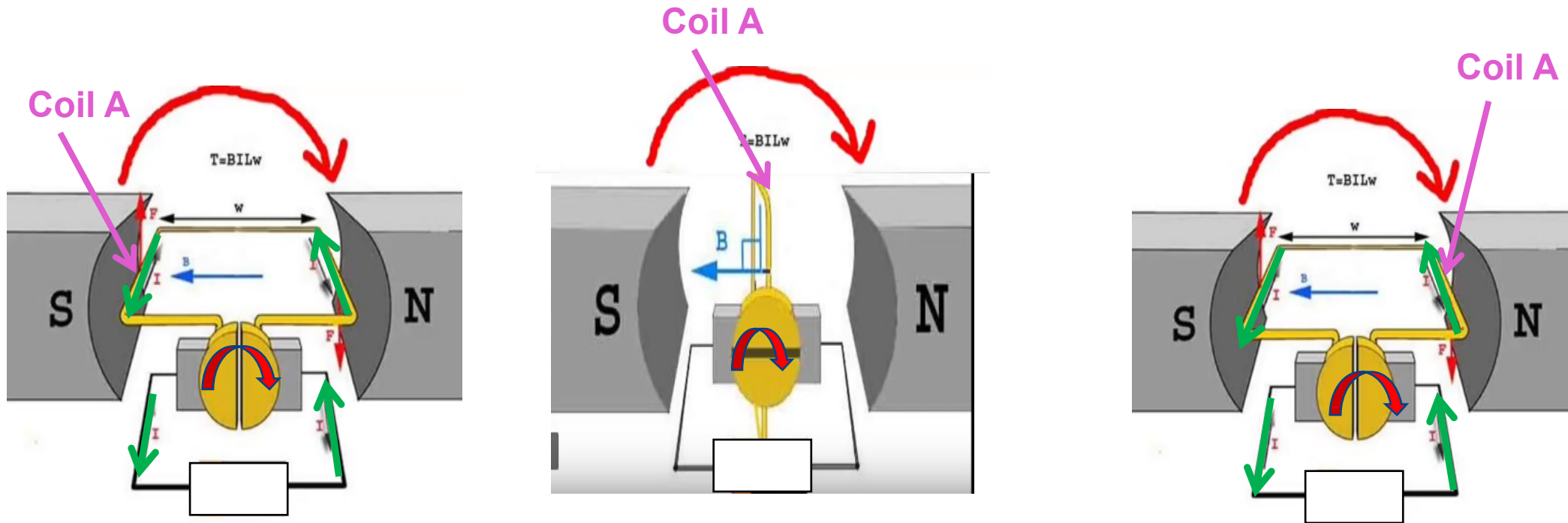


Classification of motors

- Induced voltage by magnetic flux change
 - Induced voltage 4: by speed

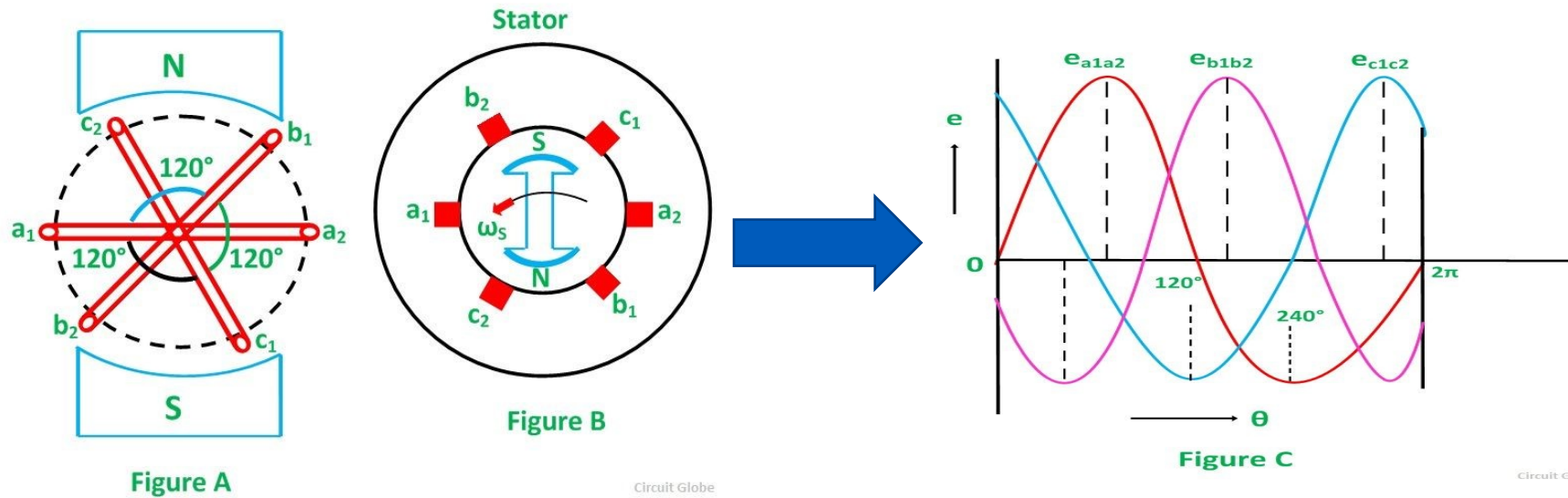


Classification of motors



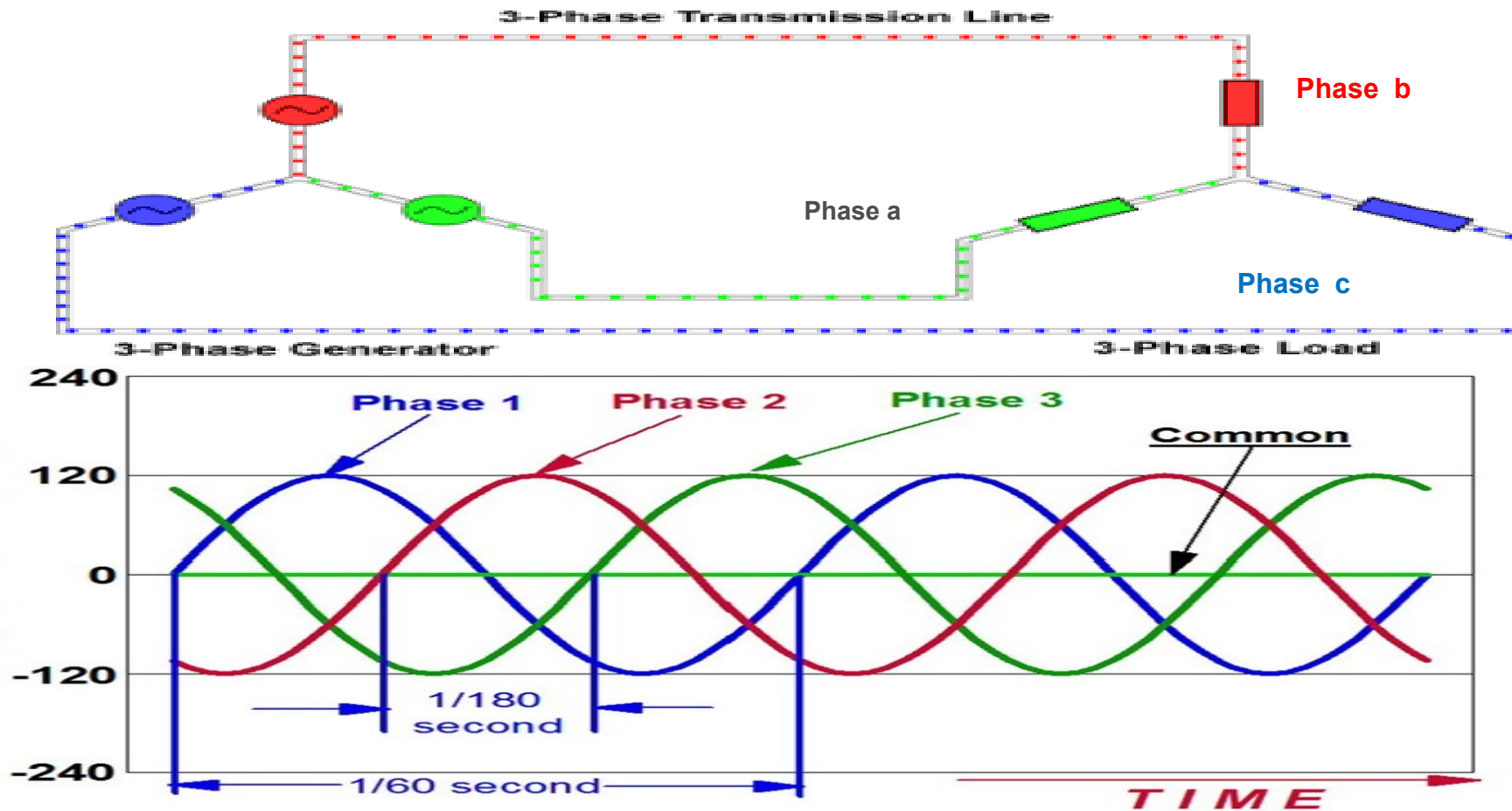
Classification of motors

- AC motors: Generation of 3 phase AC current
- 3 phase voltage is generated by $d\Phi / dt$ in the coil loop



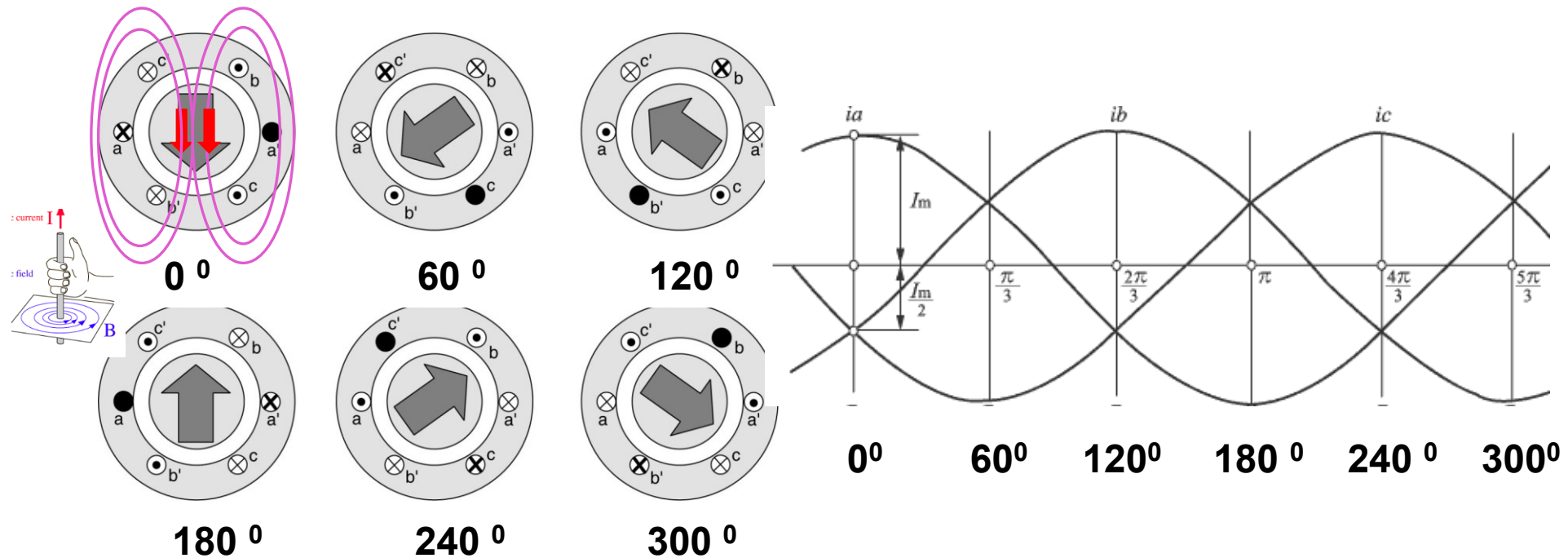
Classification of motors

- AC motors: 3 phase AC current and load at 60Hz



Classification of motors

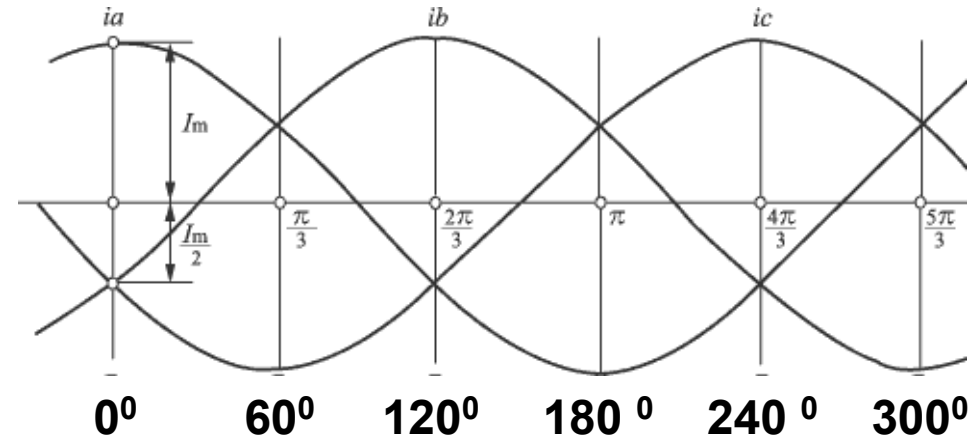
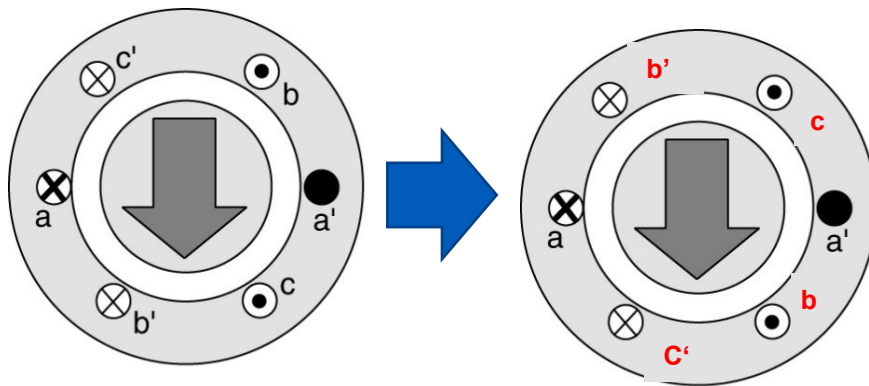
- AC motors: rotating magnetic field by 3 phase AC current
- **Remember !!!!!!!**
- **Invented by Nikola Tesla: great great invention**



<http://electricalacademia.com/synchronous-machines/synchronous-machine-construction-working/attachment/rotating-magnetic-field-created-by-a-three-phase-winding/>

Classification of motors

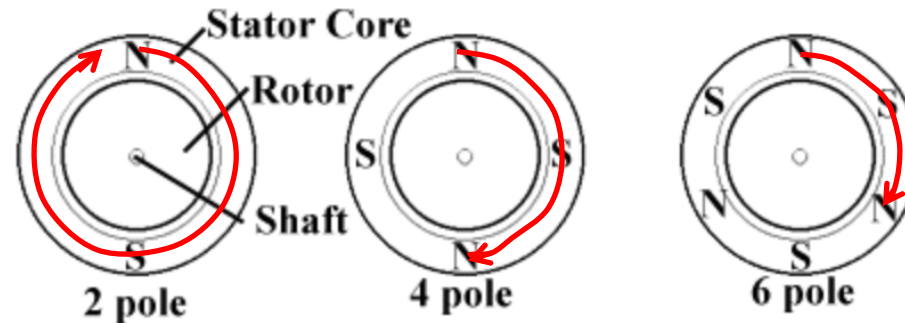
- If coil b and c is changed each other, what will be happened ???
- Home work
- rotating magnetic field is rotating to reverse direction.
- motor is rotating reversely



Classification of motors

- **Speed of rotating magnetic field**

- 2 pole 1 Hz = 1 rps
2 pole 2 Hz = 2 rps
2 pole 60 Hz = 60 rps
- 4 pole 1 Hz = 1/2 rps
4 pole 2 Hz = 1 rps
4 pole 60 Hz = 30 rps
- 6 pole 1 Hz = 1/3 rps
6 pole 2 Hz = 2/3 rps
6 pole 60 Hz = 20 rps

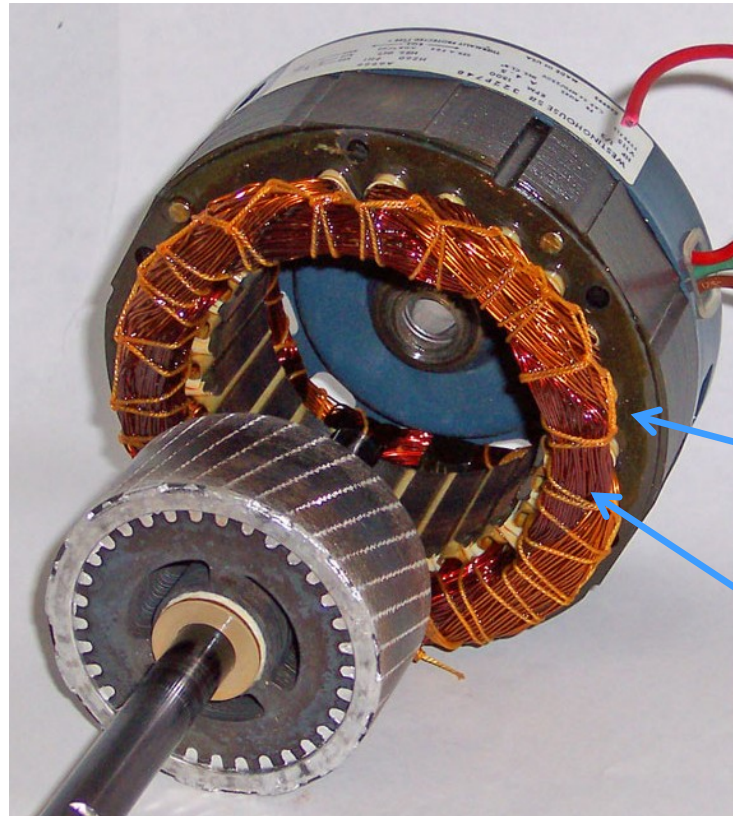


Rotation by 1 Hz

motor speed = $120f$ (frequency) / p (poles) rpm !!!

Classification of motors

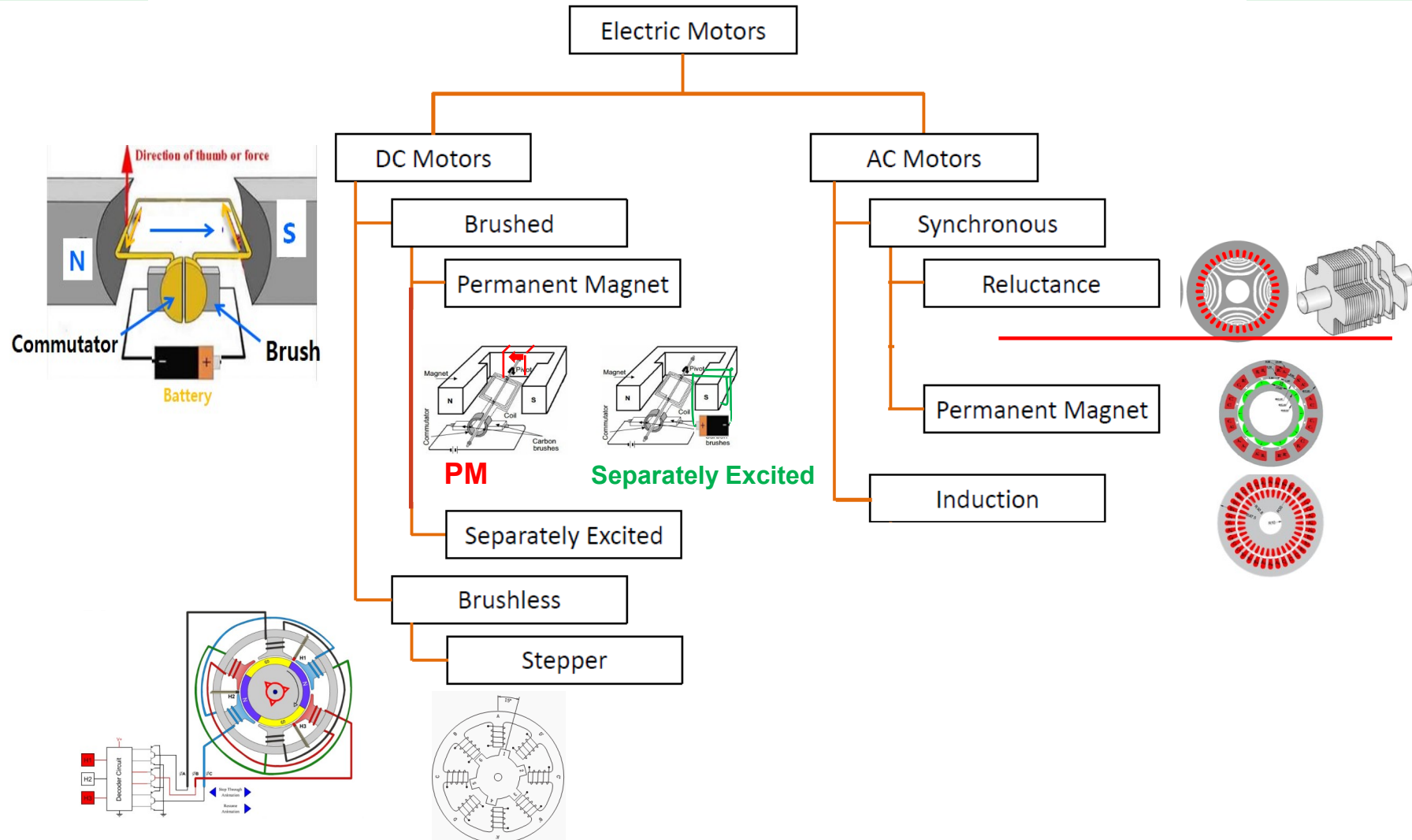
- AC motor stator for rotating magnetic field



Stator core

Stator winding (copper)

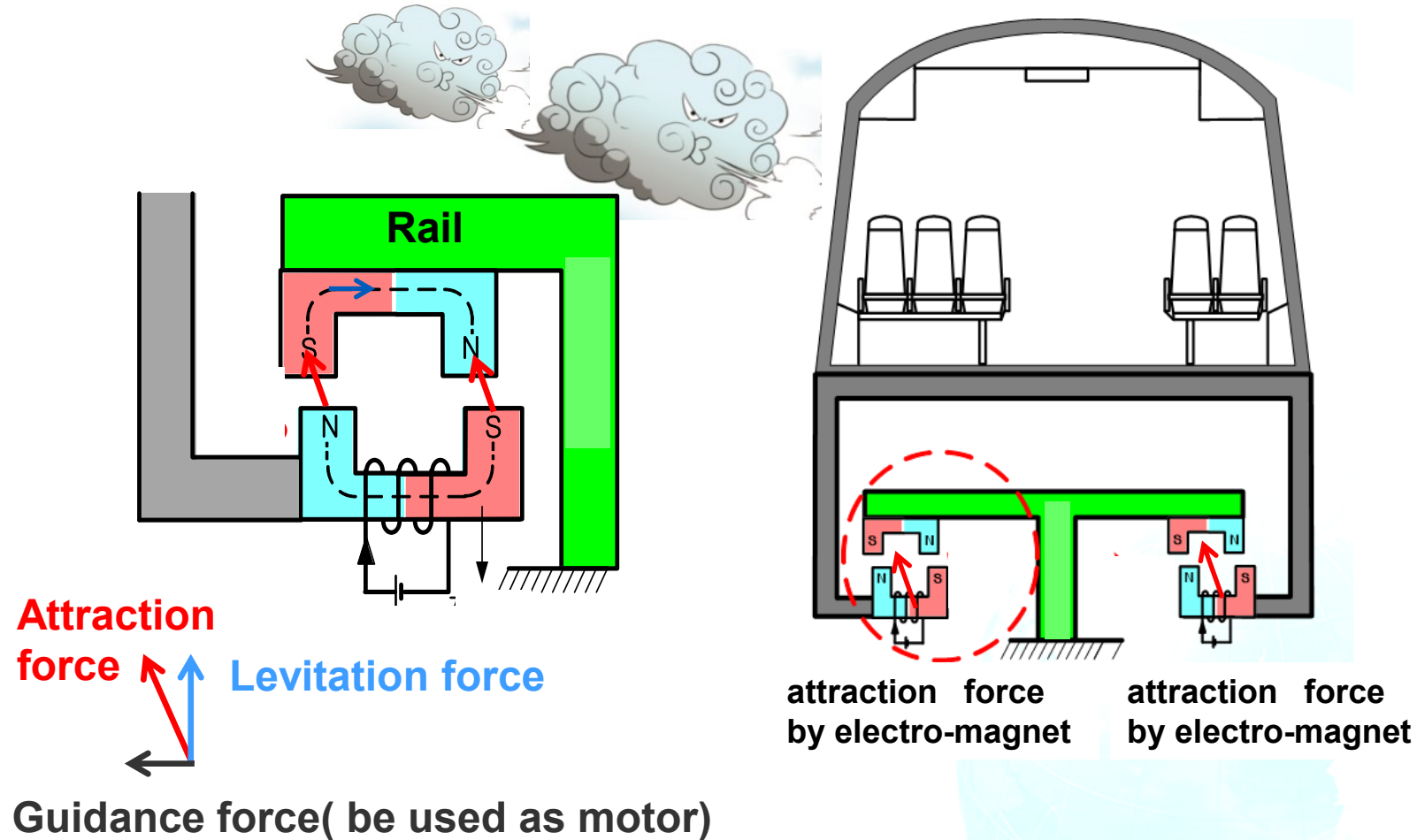
Classification of motors



<https://electricalbaba.com/brushless-dc-bldc-motor/>

Classification of motors

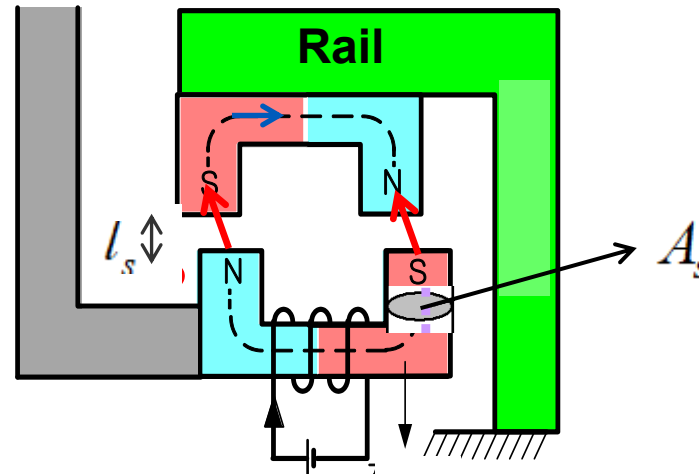
- Synchronous motor: reluctance motor
-magnetic levitation



Classification of motors

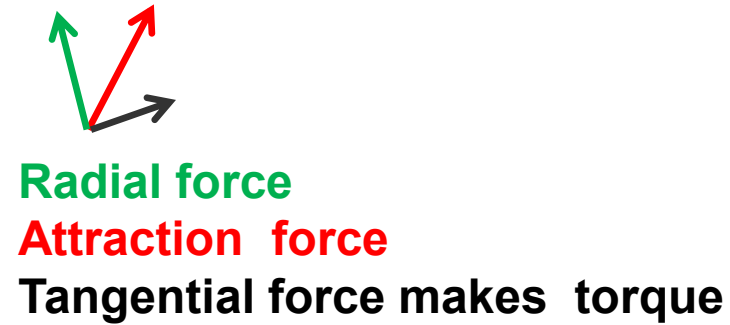
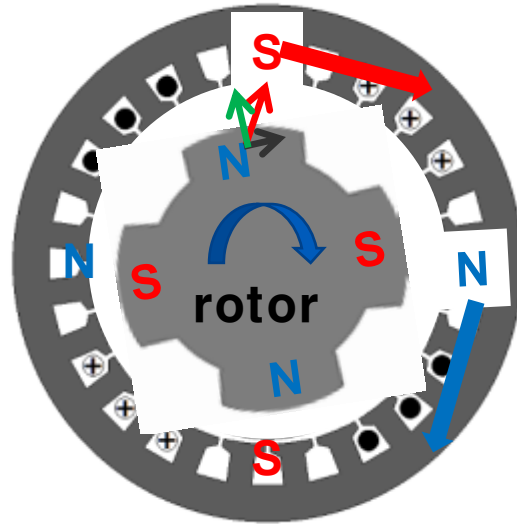
- Synchronous motor: reluctance motor
- Reluctance=inverse of magnetic resistance= $1/R_m$
- Core(motor) is moving to be minimum magnetic resistance
- Core(motor) is moving to be maximum magnetic reluctance
- Reluctance motor is named after magnetic reluctance

$$- R_m = \frac{l_s}{\mu_s A_s}$$




Classification of motors

- Synchronous reluctance motor:
 - rotating magnetic field is rotating by 3 phase AC current
 - rotor is rotating according to rotating magnetic field

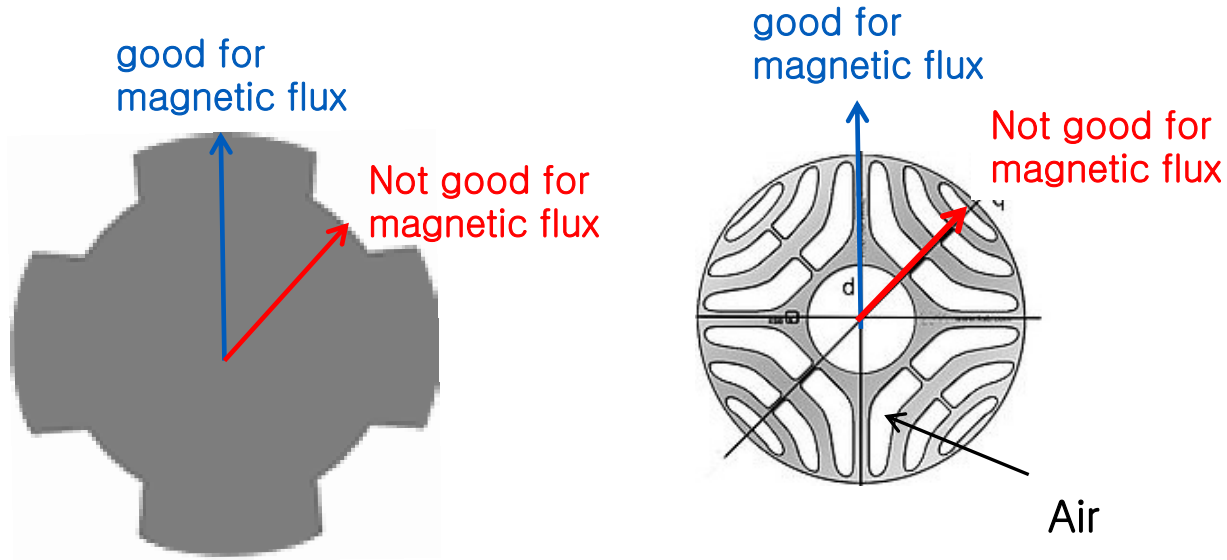


Radial force
Attraction force
Tangential force makes torque

- If rotor is , there is no force
- Radial force is 4 -6 times higher than tangential force.
- If air-gap length is not equal, more noise and vibration by unsymmetric radial force

Classification of motors

- Synchronous reluctance motor:
 - Shape of rotor

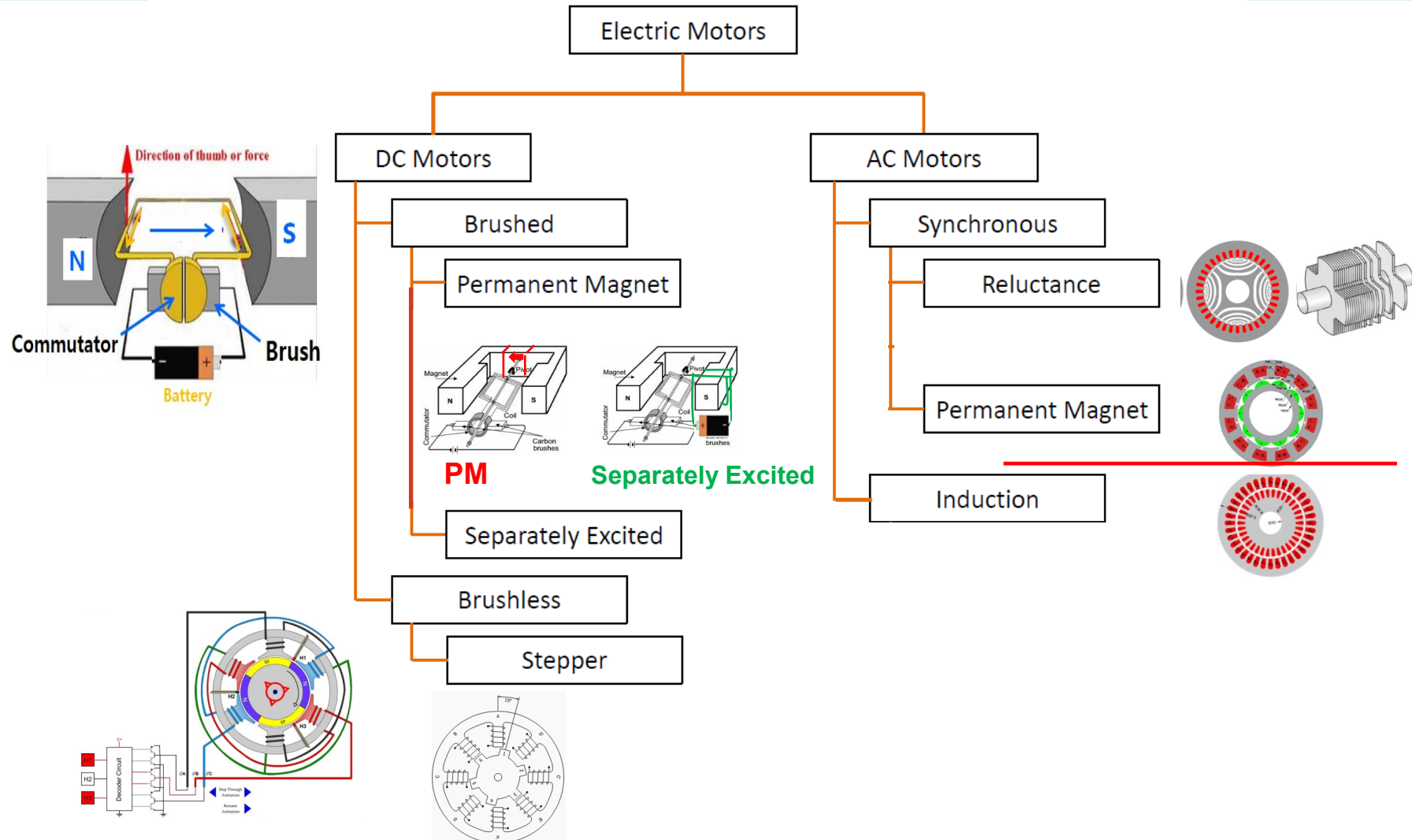


reluctance motor
rotor

- Advantage : no magnet or no copper in rotor
- Disadvantage: bigger motor

<https://new.abb.com/motors-generators/iec-low-voltage-motors/process-performance-motors/synchronous-reluctance-motors>

Classification of motors



<https://electricalbaba.com/brushless-dc-bldc-motor/>

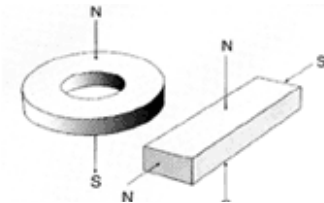
Classification of motors

- Permanent magnet motor:

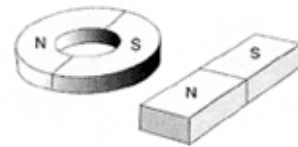
- A **permanent magnet** is an object made from a material that is magnetized by high impulse current and creates its own persistent magnetic field

- The magnetic state (or magnetic phase) of a material depends on temperature and other variables such as the reversely applied magnetic field.

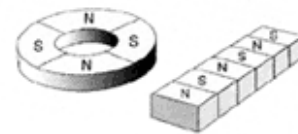
- Magnetized Magnet



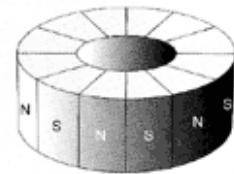
1 face/1 pole



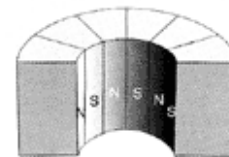
1 face/2 pole



1 face/multi pole



Inner side/outer side pole

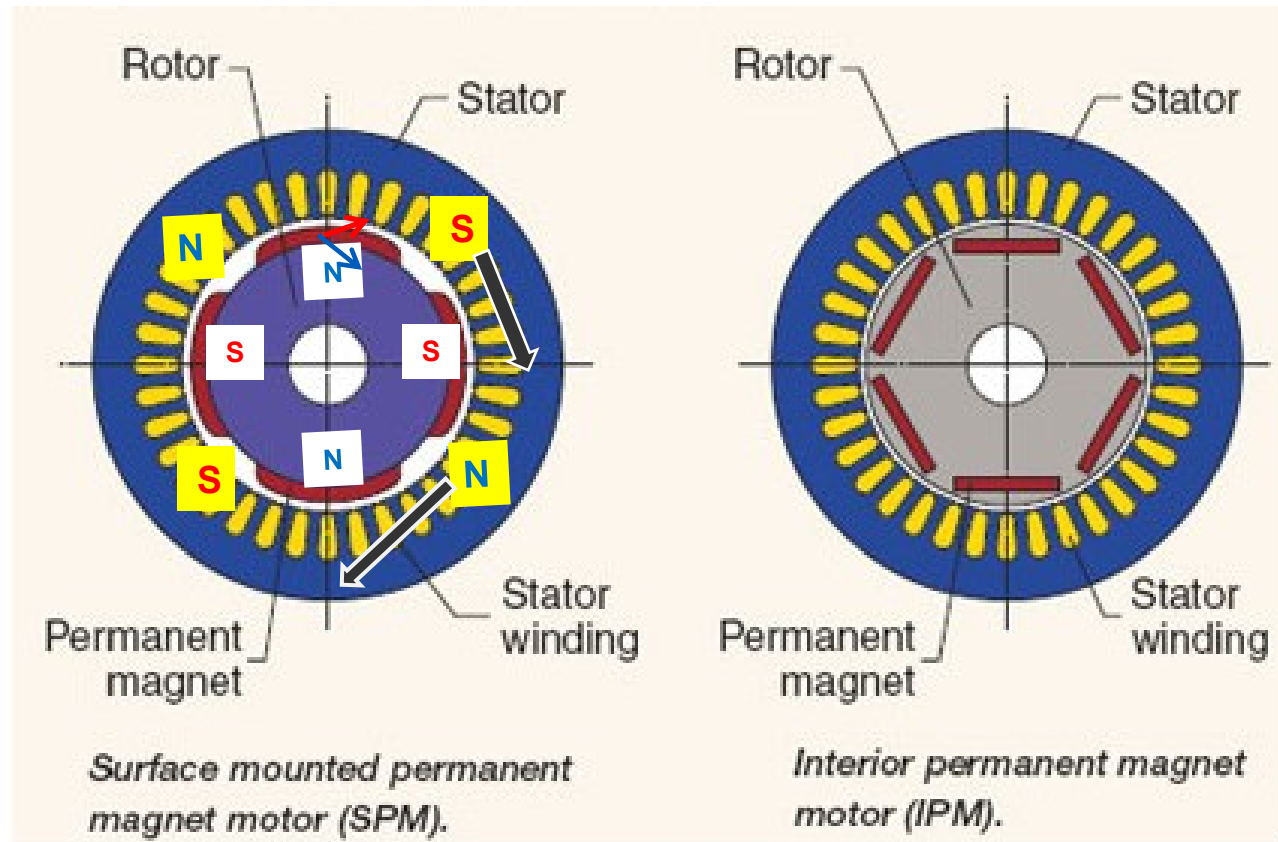


skew pole



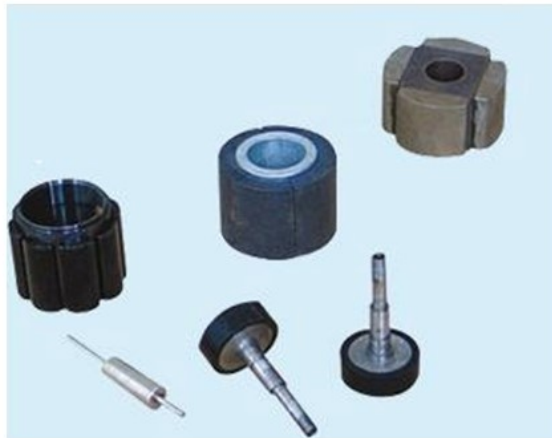
Classification of motors

- Permanent magnet motor
 - SPM and IPM

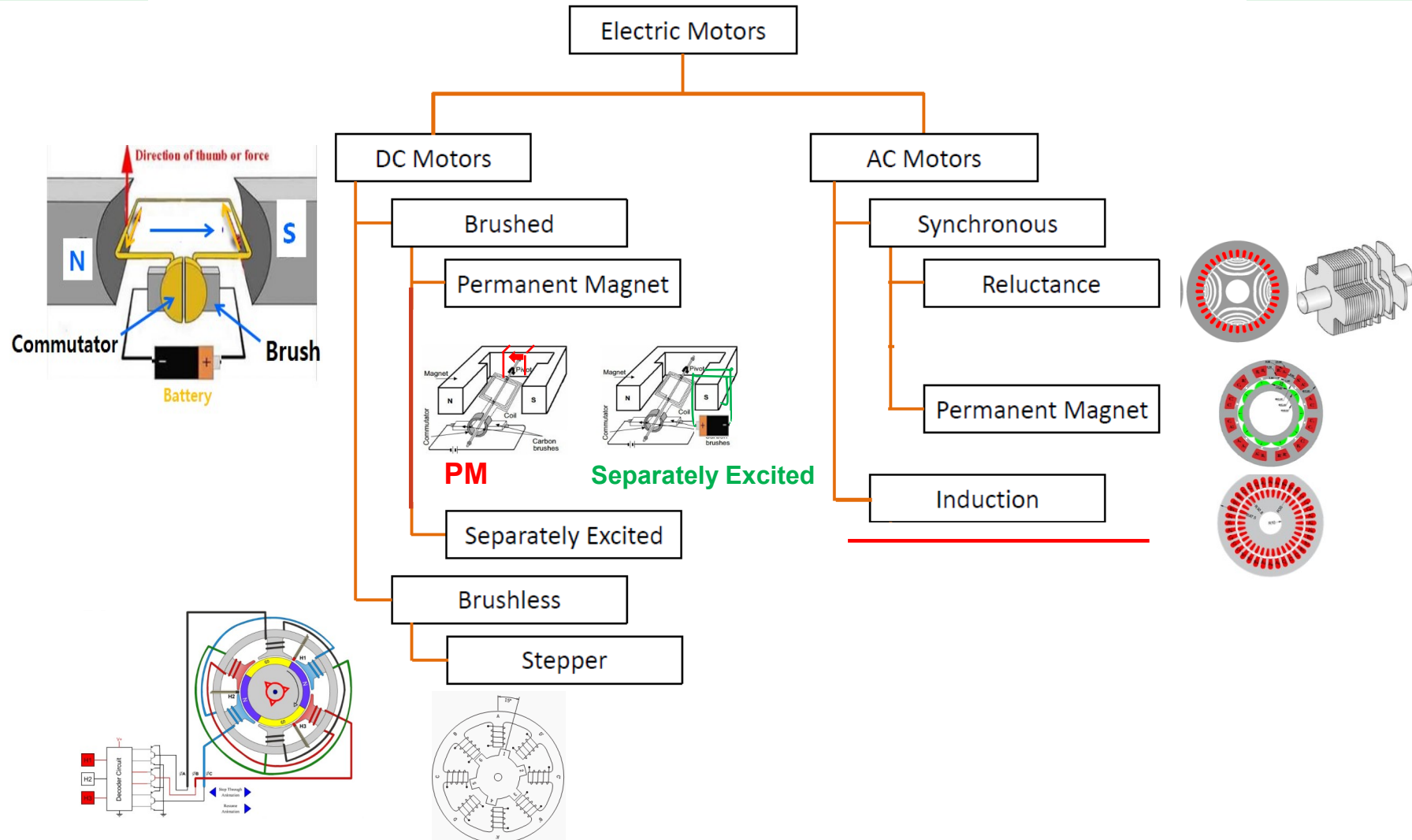


Classification of motors

- Permanent magnet motor
 - IPM motors have the permanent magnet imbedded into the rotor itself. Unlike their SPM counterparts, the location of the permanent magnets make IPM motors very mechanically sound, and suitable for operating at very high speeds
 - SPM and IPM rotor



Classification of motors



<https://electricalbaba.com/brushless-dc-bldc-motor/>

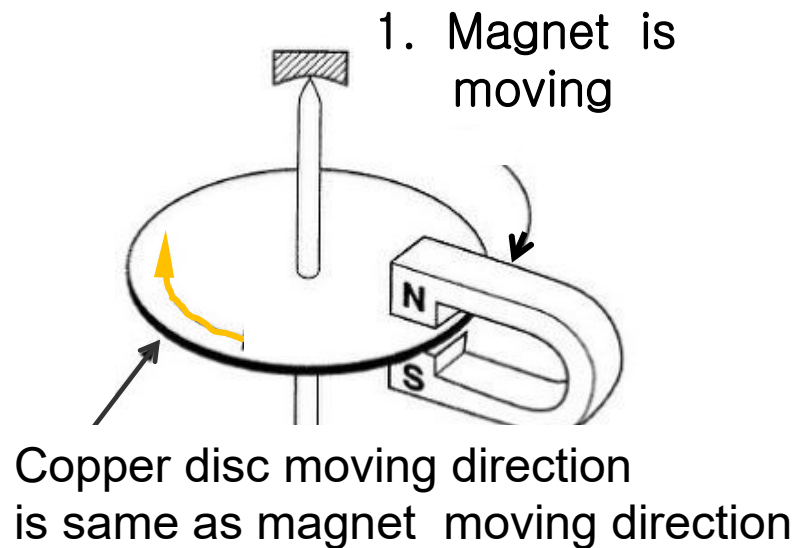
Classification of motors

- Induction motor

- Arago's disc is frequently used for explaining AC induction motors. The principle of Arago's disc goes that, when a disc made of copper or aluminum is sandwiched between magnets and the magnets are moved, eddy current is generated on the disc. And this eddy current causes the force that tries to move the disc in the moving direction of the magnets

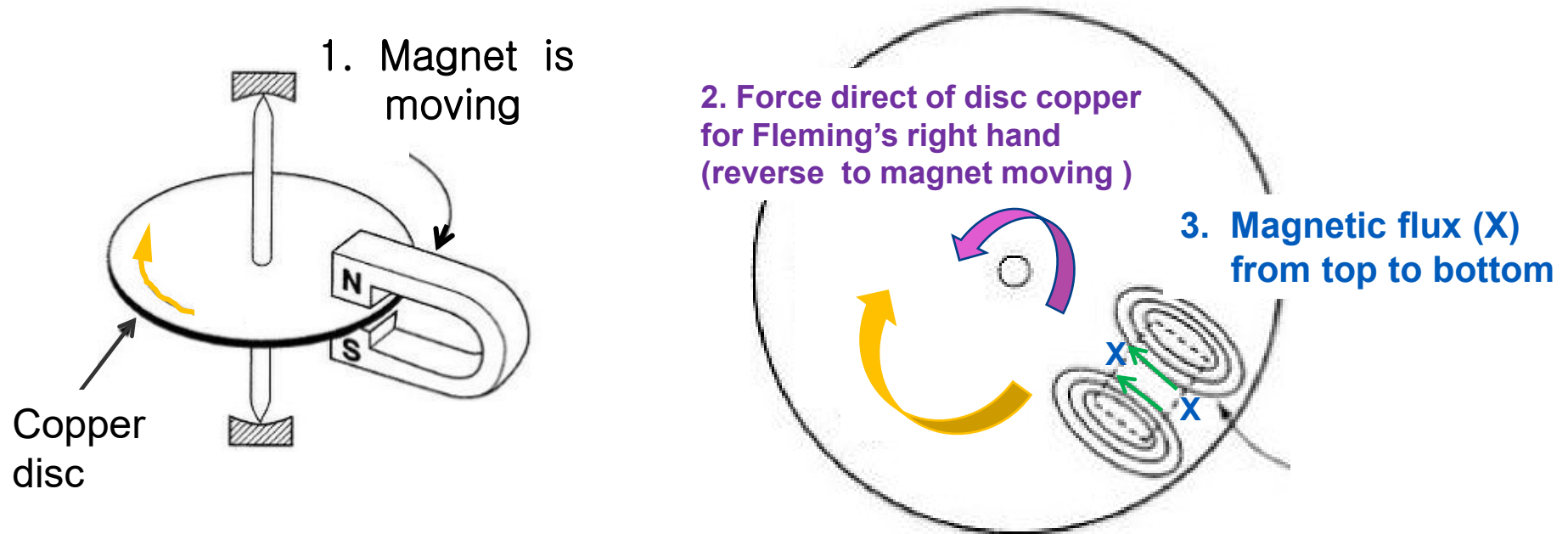
<https://www.youtube.com/watch?v=g0eA5L79Plc>

https://www.youtube.com/watch?v=e7ms3ewN_Qw



Classification of motors

- Induction motor

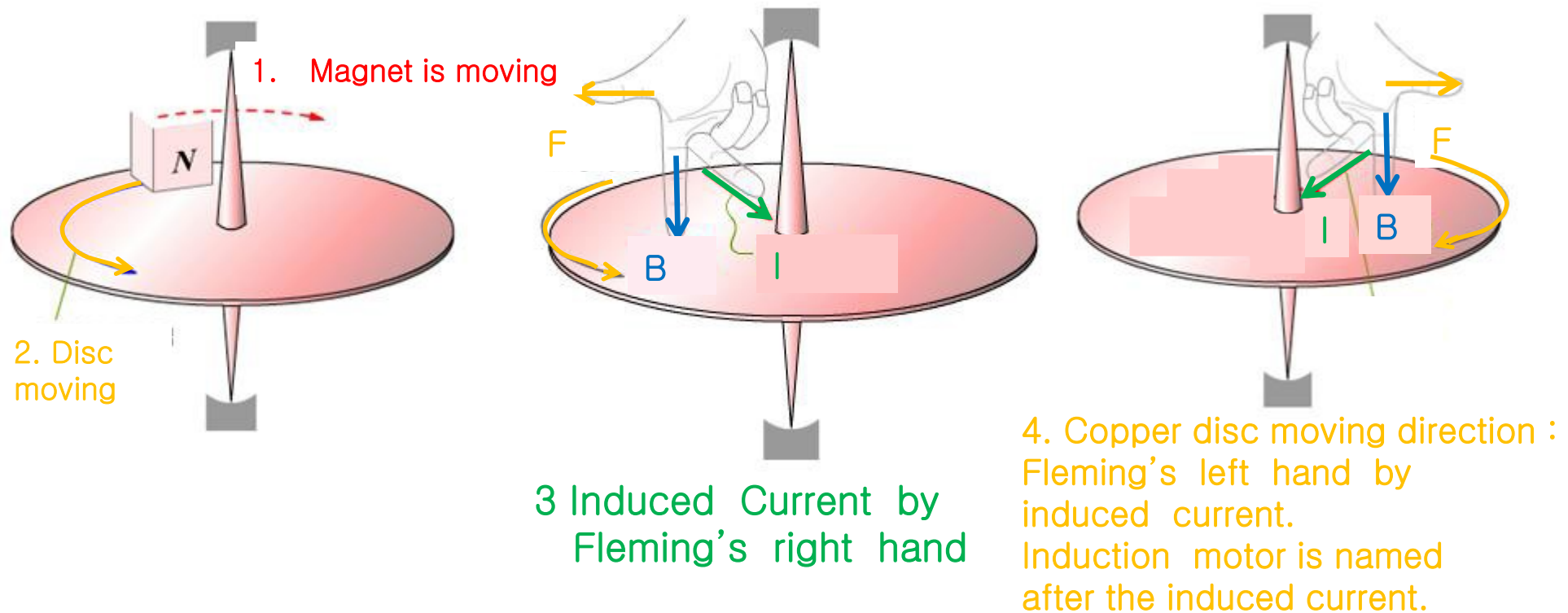


4. Induced Current by Fleming's right hand

5. Copper disc moving direction :
Fleming's left hand by induced current
Induction motor is named after the induced
current.

Classification of motors

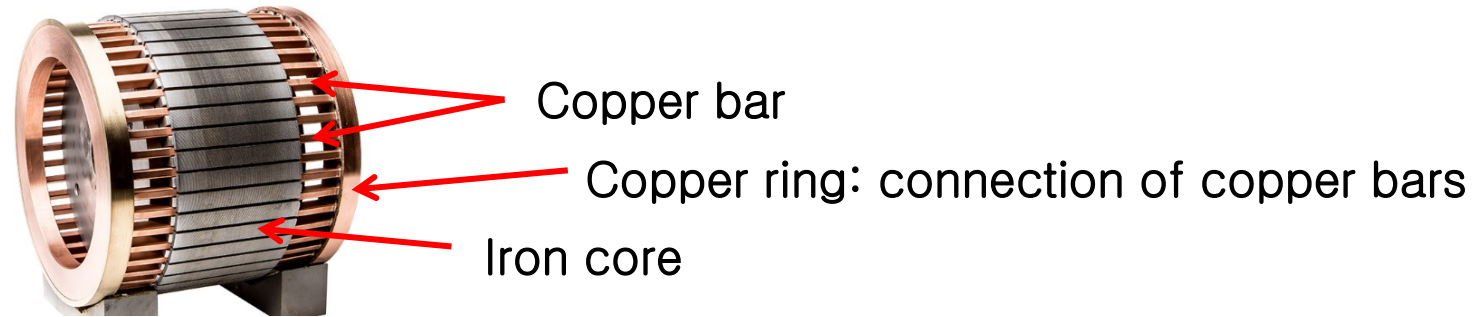
- Induction motor



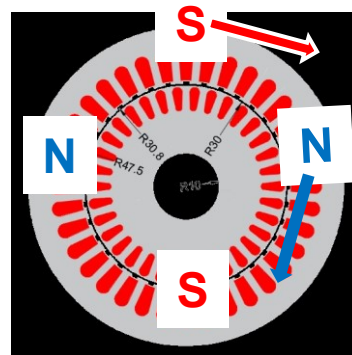
Classification of motors

- Induction motor:

- Stator is same as the reluctance motor and the PM motor
- Rotor has the copper or aluminum bar and iron core



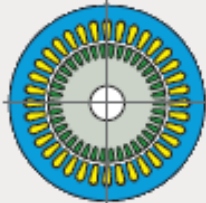
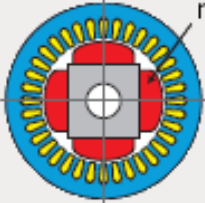
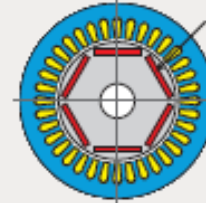
- Rotating magnetic field is rotating by 3 phase AC current



- Rotor is rotating by the induced current in rotor bar (Arago's disc)

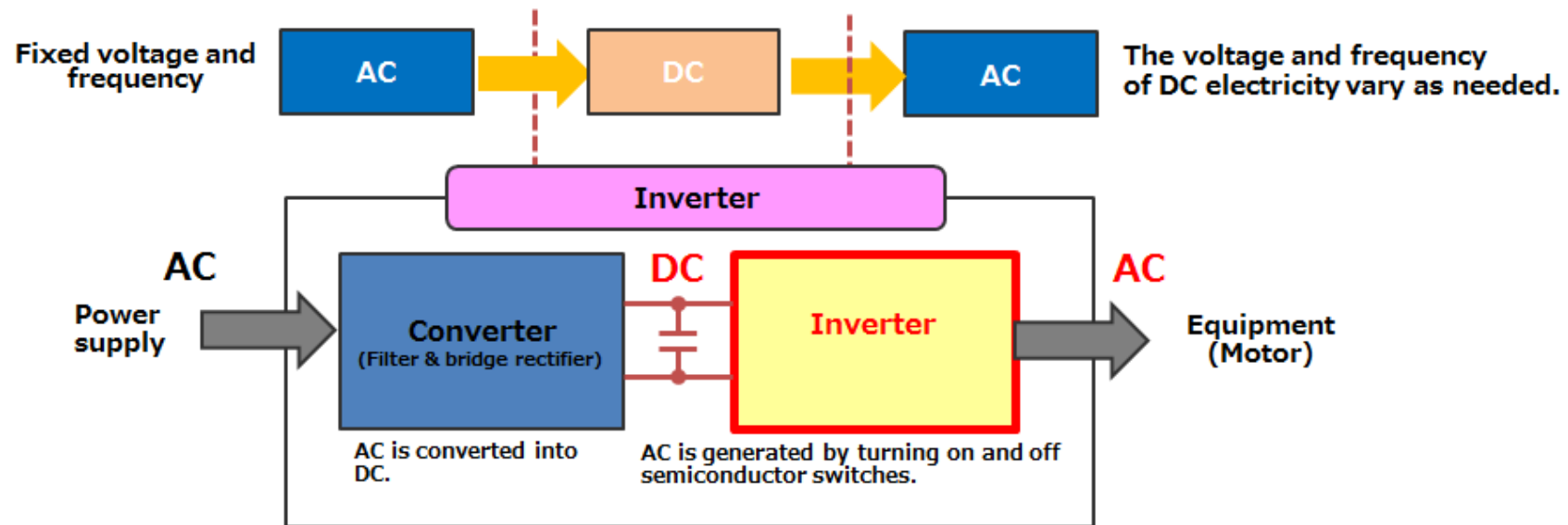
Classification of motors

- SPM, IPM and induction motor

	Induction motor	Synchronous motor	
		SPM motor	IPM motor
Rotor structure		 magnet	 magnet
Principle	An electric current flows through the rotor and rotates with a delay of the slip speed from the rotating magnetic field speed.	A magnet torque is generated, and the rotor rotates at the same speed as the rotating magnetic field.	A magnet torque and reluctance torque are generated, and the rotor rotates at the same speed as the rotating magnetic field.
Motor volume	Relatively bigger than synchronous motor	Very small	Small
Effectiveness and power factor	Good	Very good	Very good
Speed	Very fast	Fast	Very fast
Maximum torque	Very big	Big except for the case of servo that is very big	Big
Torque component	Induction	Magnet	Magnet and reluctance

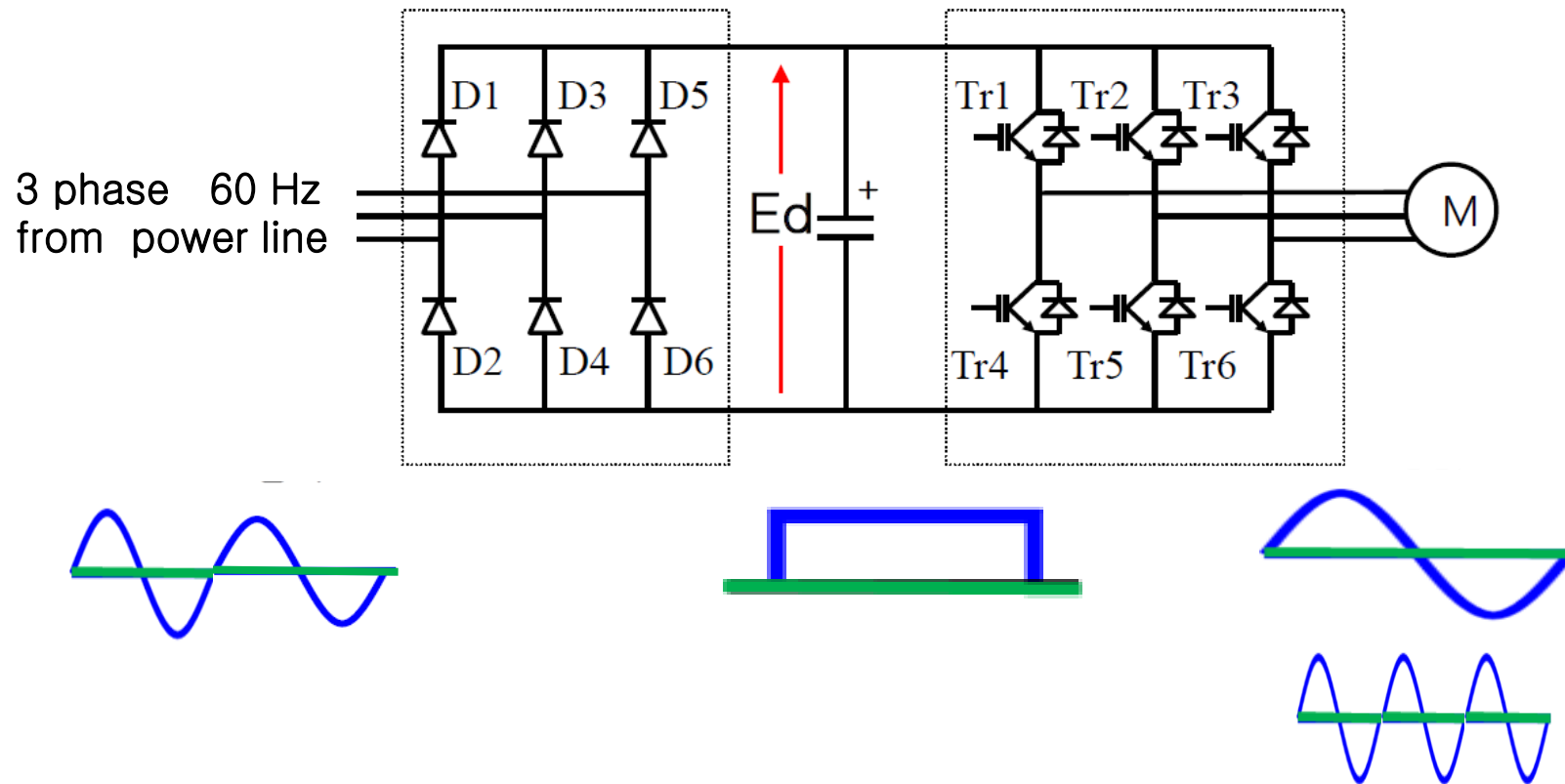
Classification of motors

- Speed changing for AC motor
 - motor speed = $120f$ (frequency) / p (poles) rpm !!!
 - For changing motor speed
 - Changing in put current(voltage) frequency



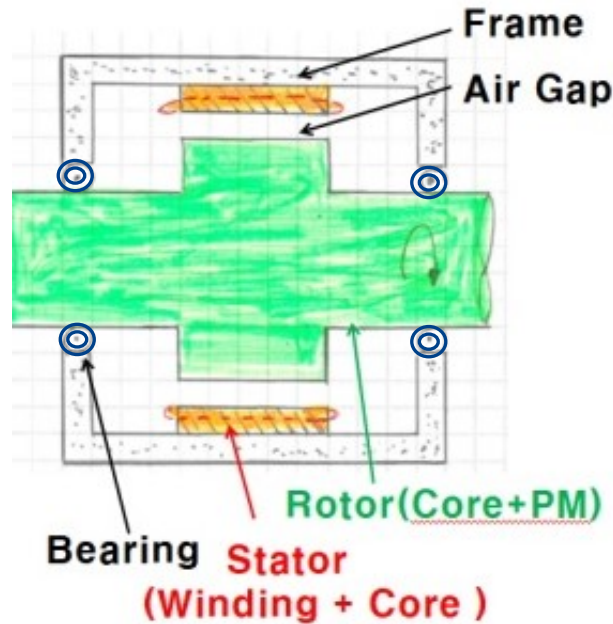
Classification of motors

- Speed changing for AC motor

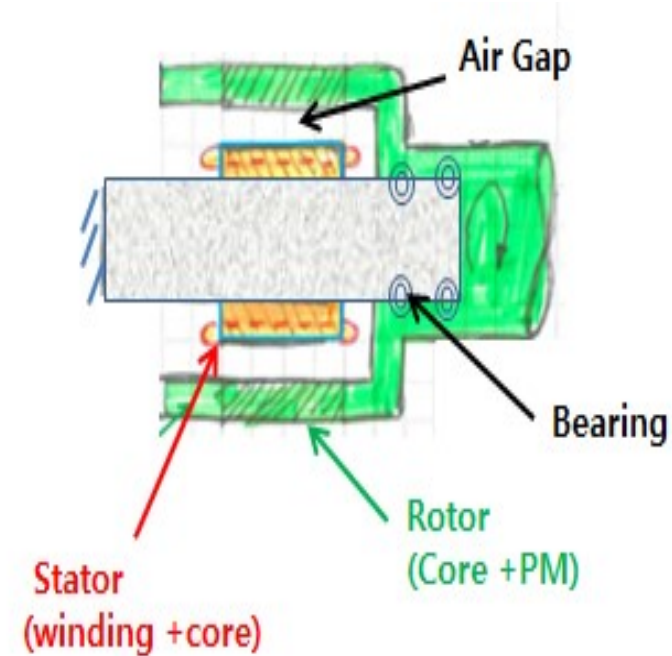


Classification of motors

- Inner rotor motor and outer rotor motor



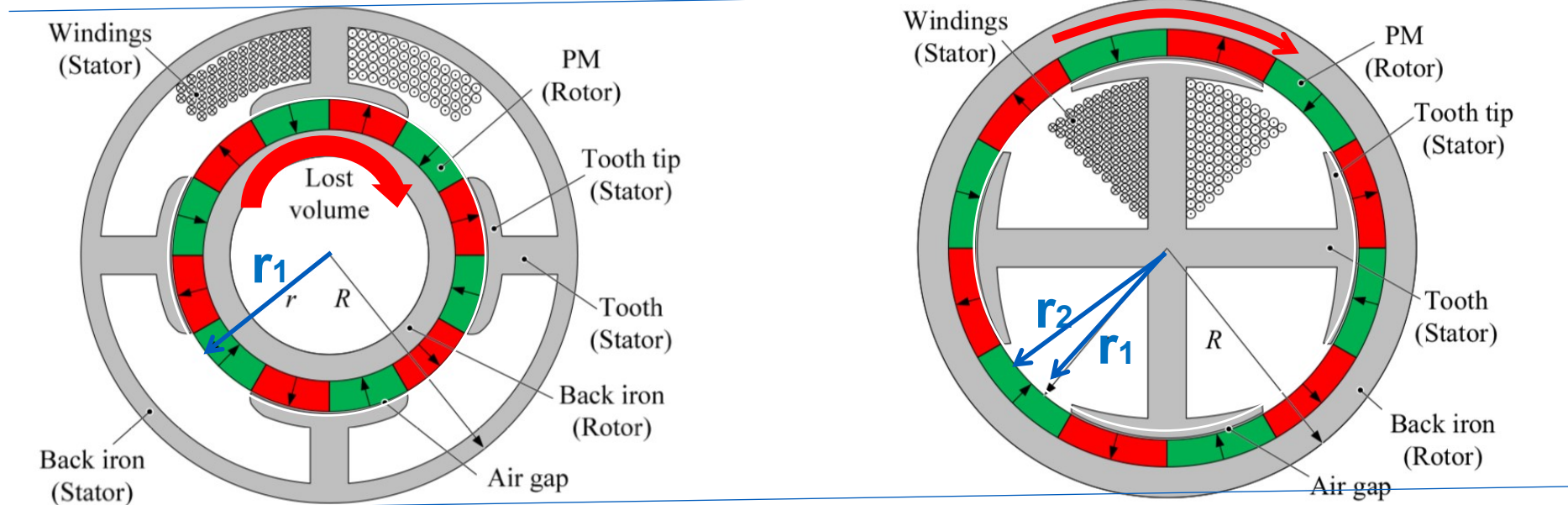
structure (good)
general purpose



structure (not good)
low speed and high torque
(washing machine or fan)

Classification of motors

- Inner rotor motor and outer rotor motor

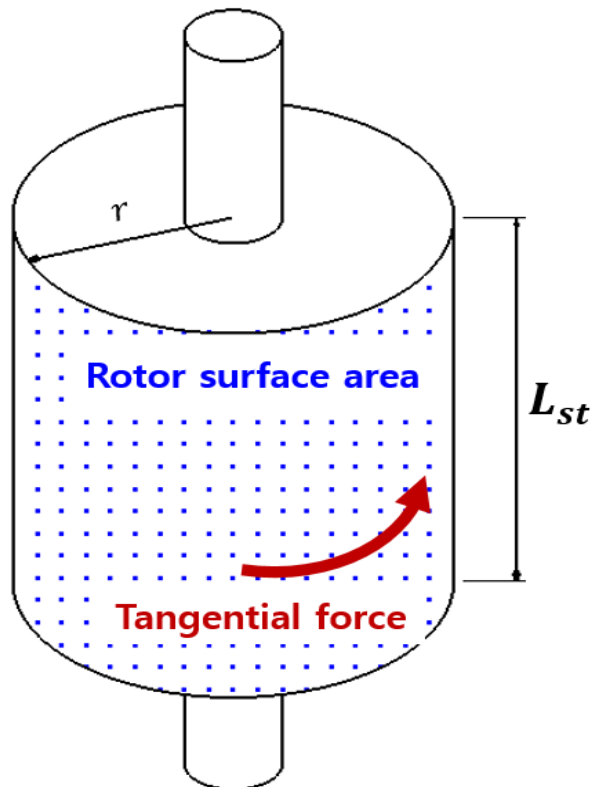


$$\begin{aligned}
 T(\text{torque}) &= \text{Tangential force} * r \\
 &= F_{sd} * \text{Rotor surface area} (2\pi r L_{st}) * r \\
 &= K * r^2
 \end{aligned}$$

Classification of motors

- Inner rotor motor and outer rotor motor

–Surface force density F_{sd} (N/m²) is Tangential force per Rotor surface area

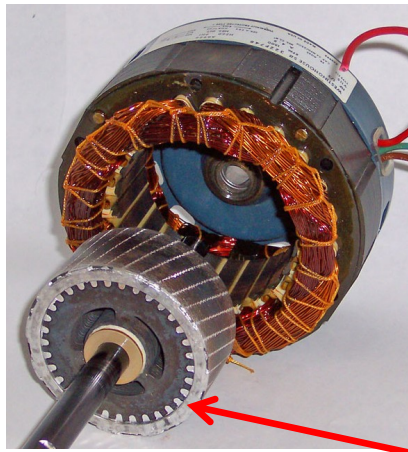


$$F_{sd} = \frac{\text{Tangential force}}{\text{Rotor surface area}(2\pi r L_{st})}$$

$$\begin{aligned} T(\text{torque}) &= \text{Tangential force} * r \\ &= F_{sd} * \text{Rotor surface area}(2\pi r L_{st}) * r \\ &= F_{sd} * \pi L_{st} * r^2 \end{aligned}$$

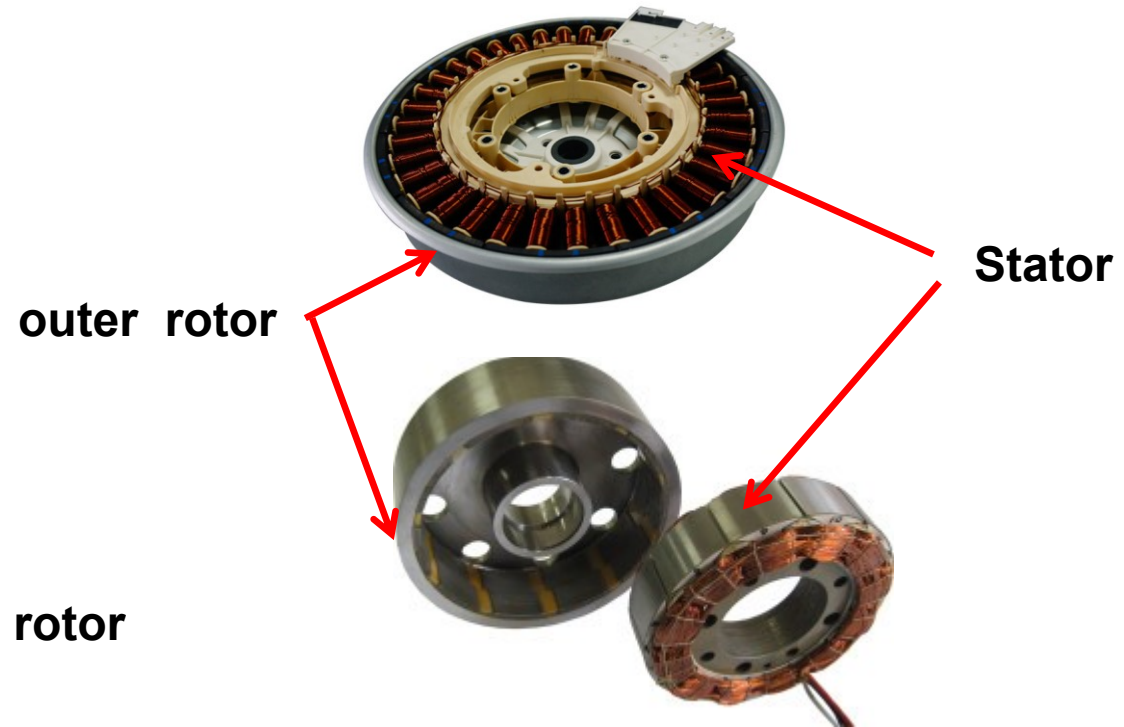
Classification of motors

- Inner rotor motor and outer rotor motor



Inner rotor

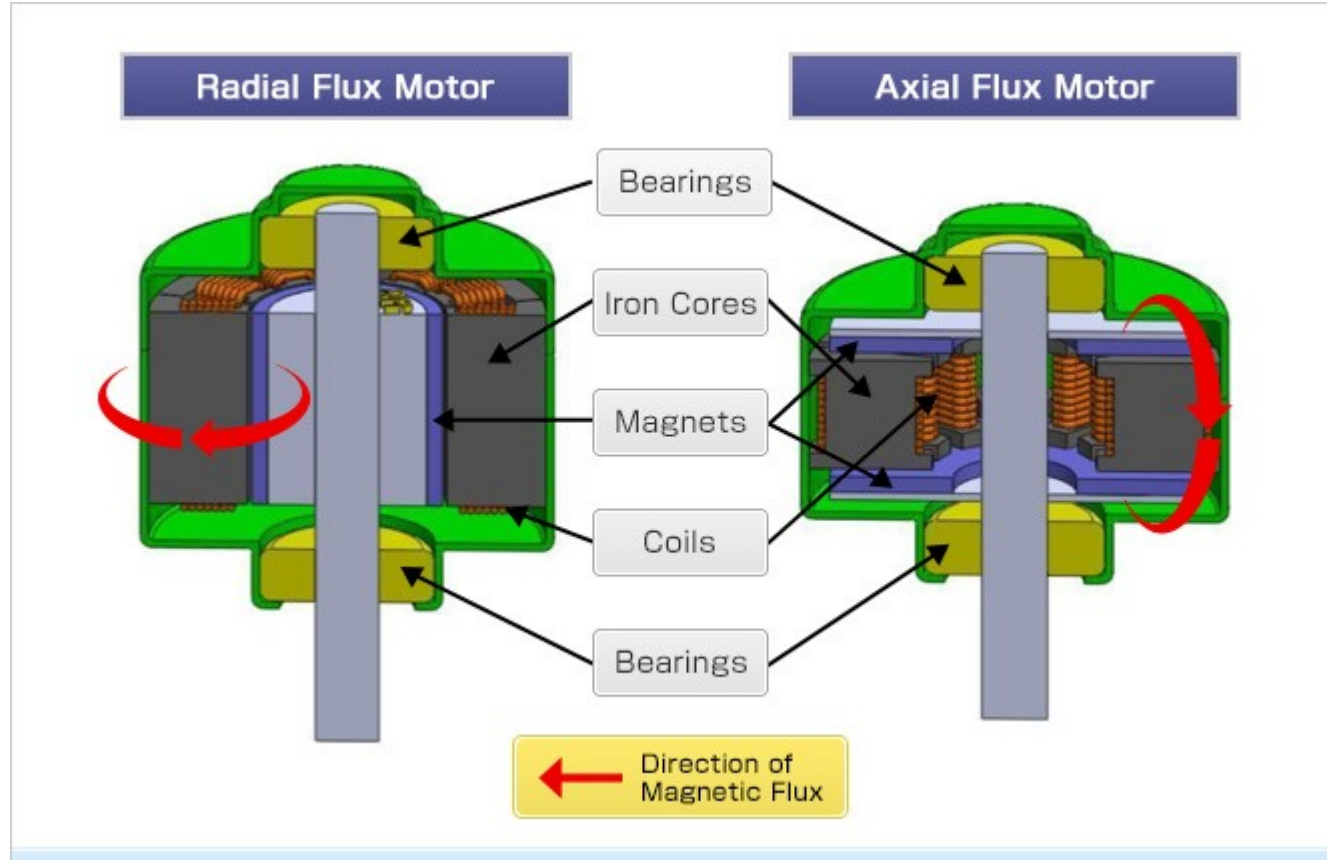
Inner rotor motor



Outer rotor motor

Classification of motors

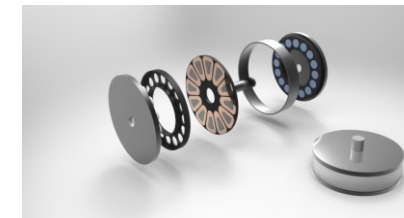
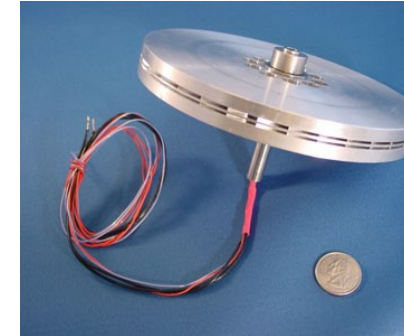
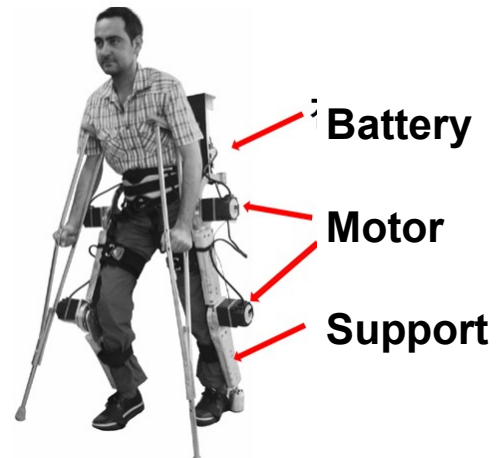
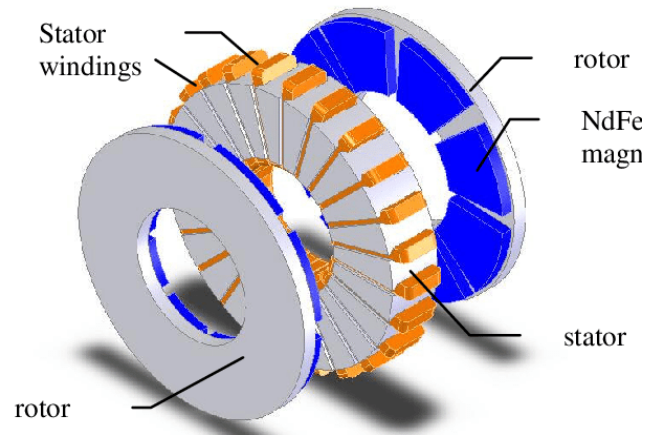
- Radial flux motor and axial flux(disk) motor



https://www.nidec.com/en-NA/technology/rd/innovative_motor/

Classification of motors

- Radial flux motor and axial flux motor



https://www.researchgate.net/figure/8-pole-24-slot-axial-flux-PM-reference-motor_fig2_224393995

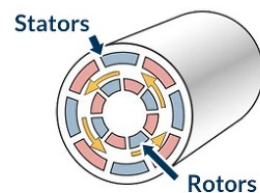
<https://endless-sphere.com/forums/viewtopic.php?t=14260>

Classification of motors

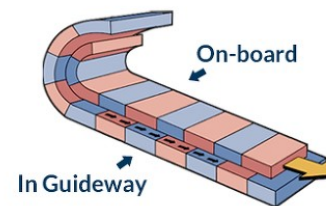
- Linear motor

A linear motor is an [electric motor](#) that has had its [stator](#) and [rotor](#) "unrolled" thus instead of producing a [torque](#) ([rotation](#)) it produces a linear [force](#) along its length. However, linear motors are not necessarily straight. Characteristically, a linear motor's active section has ends

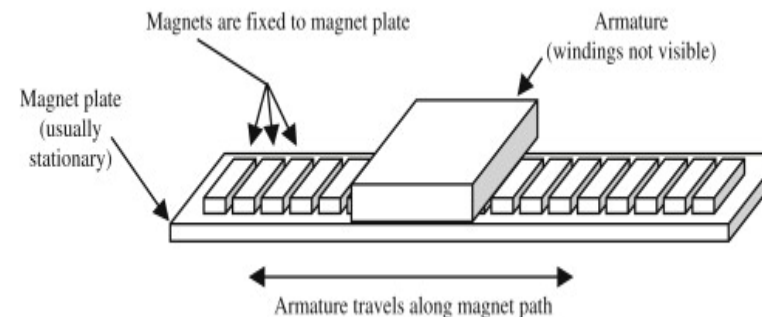
CONVENTIONAL MOTOR



LINEAR MOTOR



northeastmaalev.com



Classification of motors

▪ Linear motor

Advantages of linear motors:

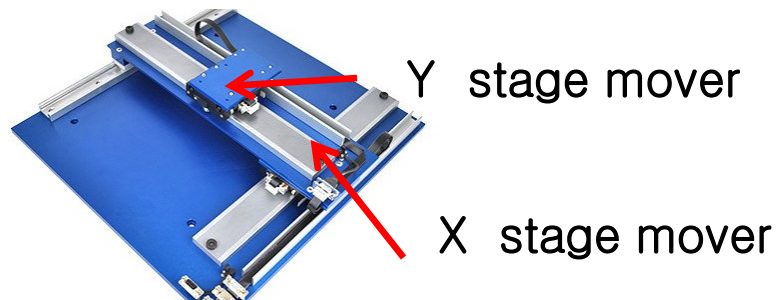
- There is no mechanical contact,
- The structure is simple
- Its operation can provide a wide range of speed operation, covering a few microns to several meters per second, especially at high speed is one of its outstanding advantages
- Acceleration, up to 10g
- Accuracy and repeatability are high due to the elimination of the intermediate links that affect accuracy.
- Easy to maintain, due to the small parts, no mechanical contact with the movement, thus greatly reducing the wear and tear of parts

Disadvantages of linear motors:

- One side (on board or in guide way) has long length.(expensive.)
- The dynamic stiffness of the linear motor is extremely low, can not play the role of buffer damping, high-----

Classification of motors

- Linear motor: application
 - X Y stage



- High speed magnetic levitation train



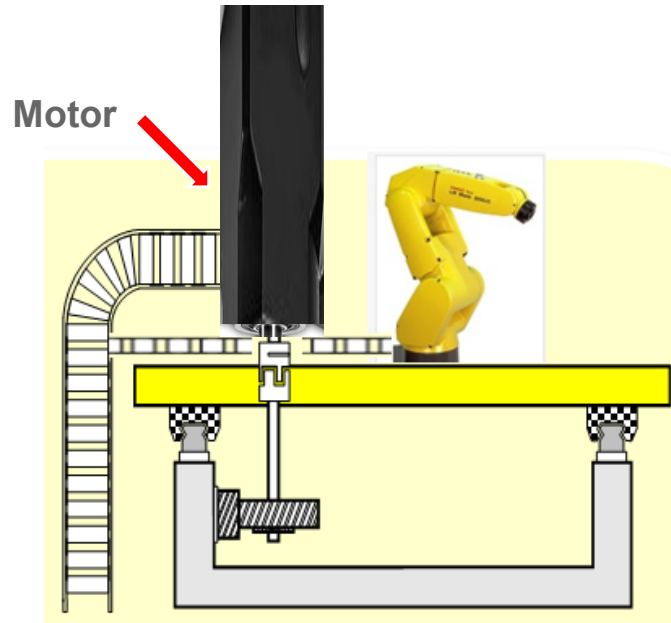
Transrapid (500km/h) in Shanghai
German-developed [high-speed train](#)



Superconducting a magnetic levitation
train in Japan

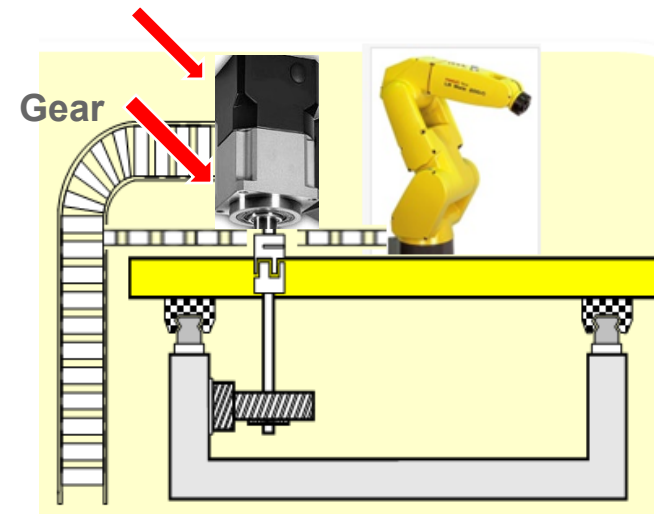
Classification of motors

- motor + gear
 - Load asks speed 600rpm and torque 40Nm
 - Motor 600rpm and torque 40Nm is too big because of big-torque
 - Solution : high-speed motor + gear



**Motor direct drive
for 600rpm and torque 40Nm**

High speed motor



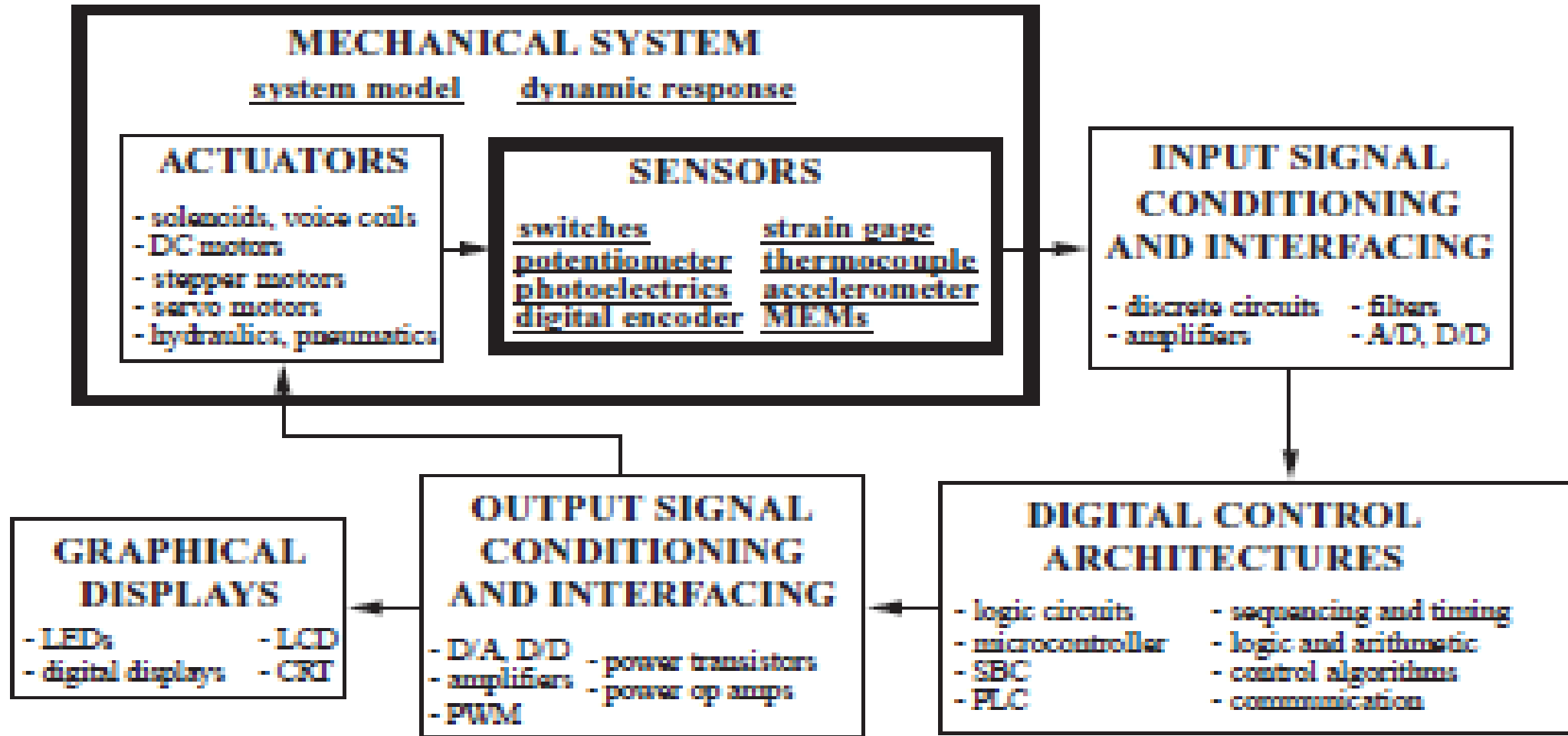
**Motor 2400 rpm torque 10Nm
Gear 600 rpm torque 40Nm**

Classification of motors

▪ Electrical and mechanical system analogy

<u>System</u>	<u>Potential</u>	<u>Flow</u>	<u>Resistance</u>	<u>Capacitance</u>	<u>Inductance</u>
Electrical	voltage	current	R	C	L
Mechanical	force	velocity	damper	spring	mass
Fluid	head	vol. flow	flow res.	surf. area	flow inertia
Magnetic	MMF(N*I) (magnetomotive force)	Φ , flux	reluctance		

Sensor

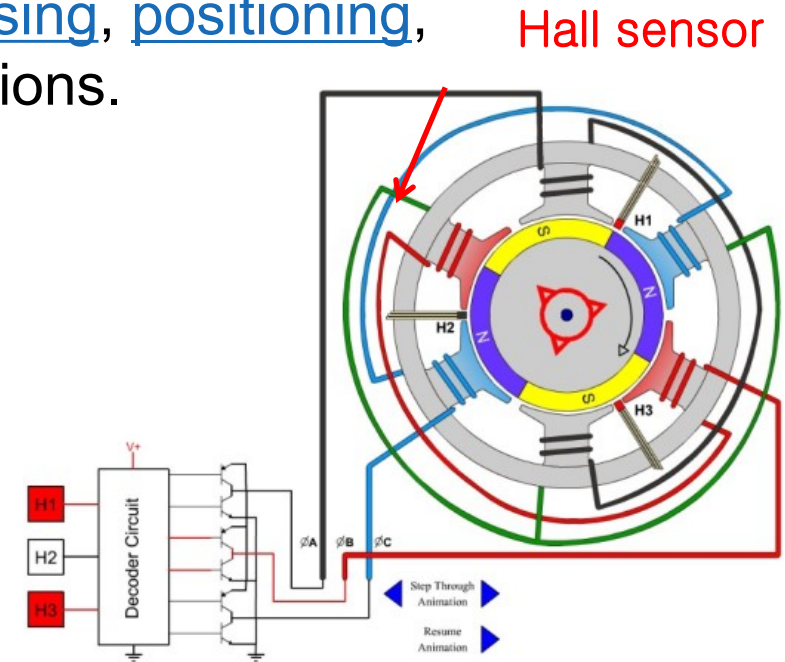
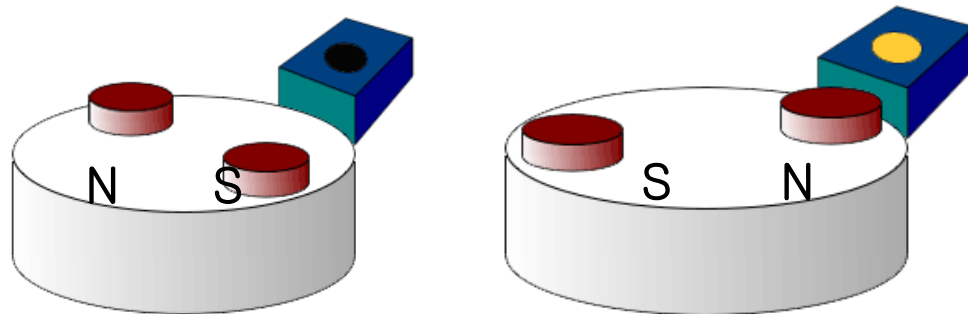


Sensor

▪ Hall sensor

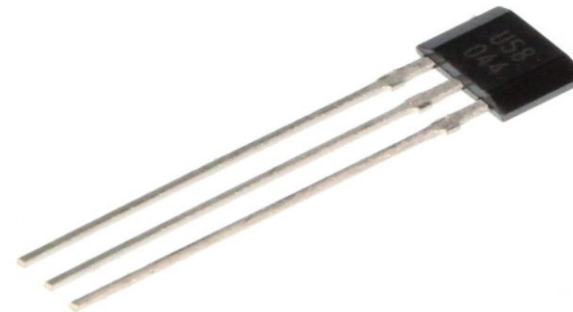
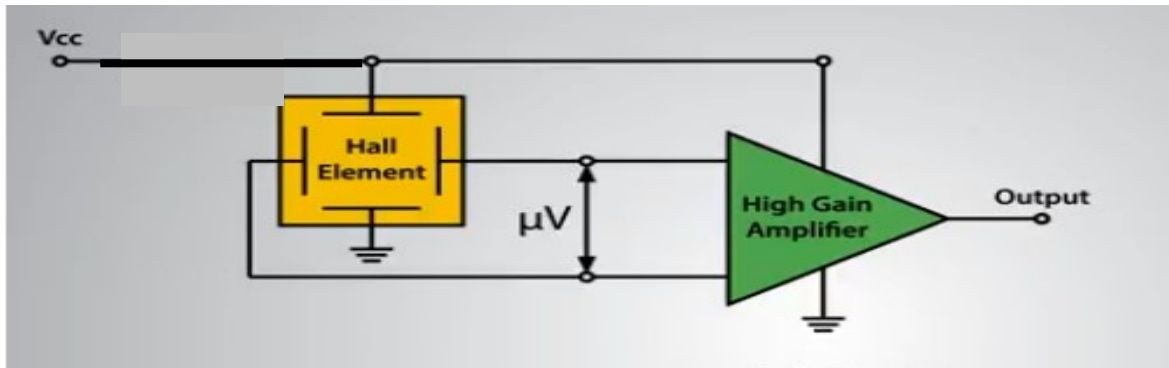
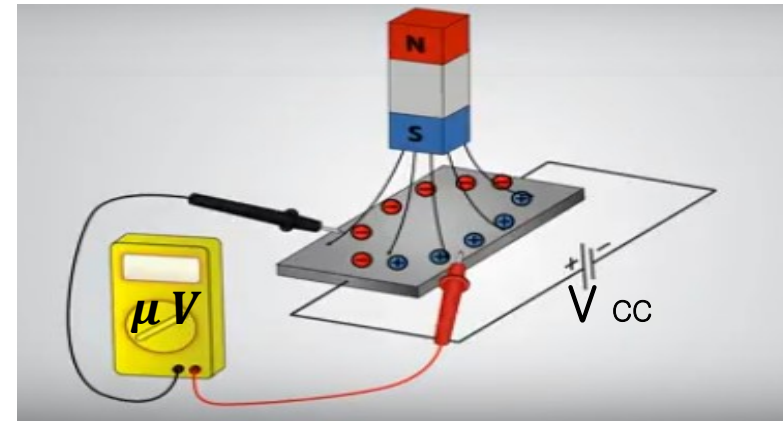
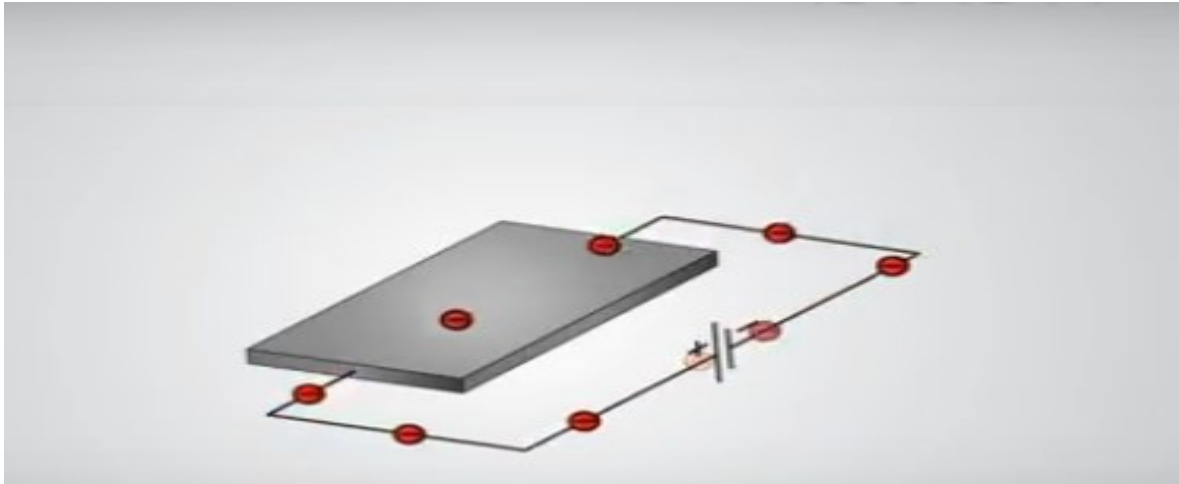
A **Hall effect sensor** is a device that is used to measure the magnitude of a magnetic field. Its output voltage is directly proportional to the magnetic field strength through it.

Hall effect sensors are used for proximity sensing, positioning, speed detection, and current sensing applications.



Sensor

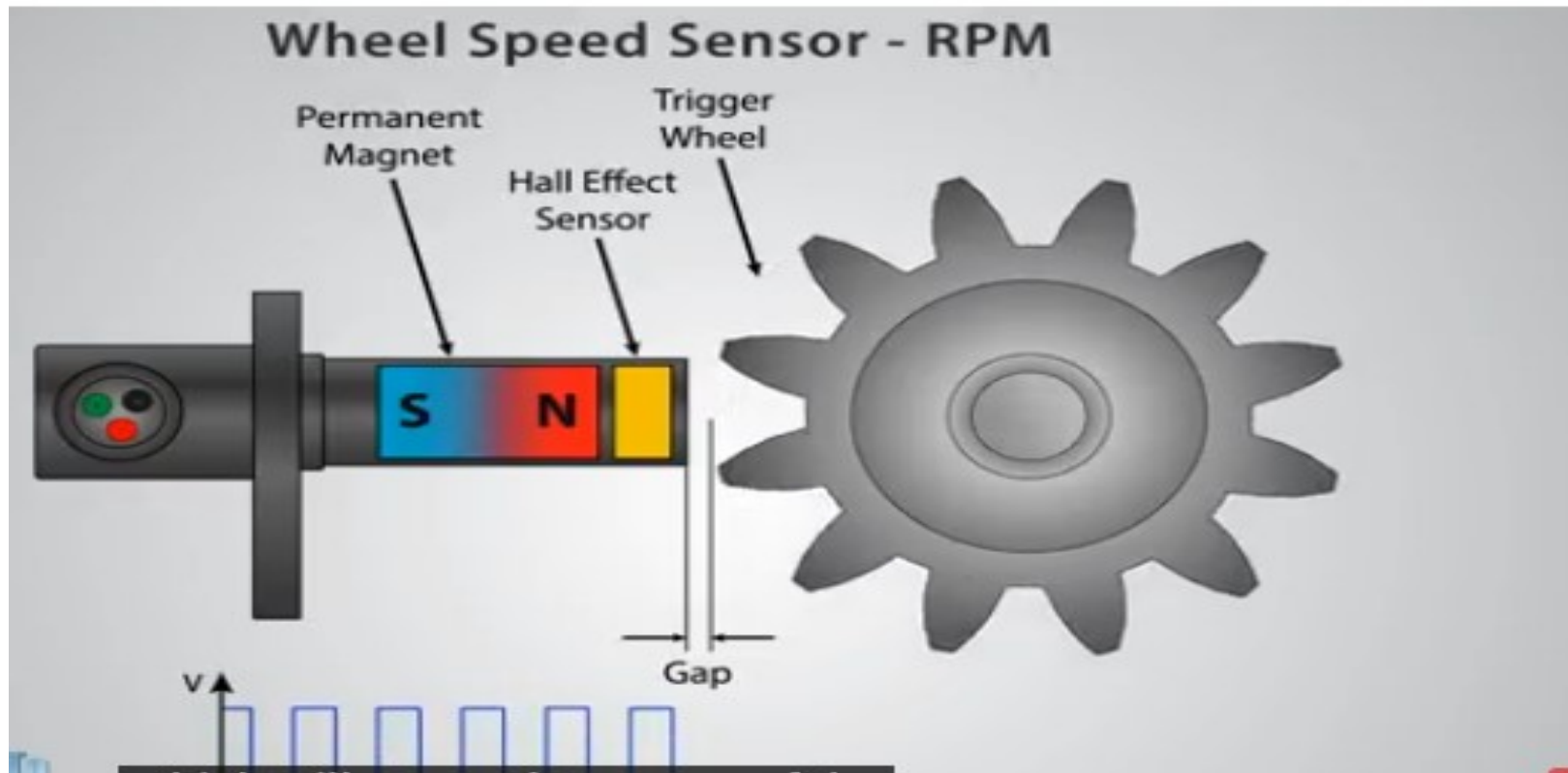
- Hall sensor



<https://blog.naver.com/nissei-gtr/221599187446>

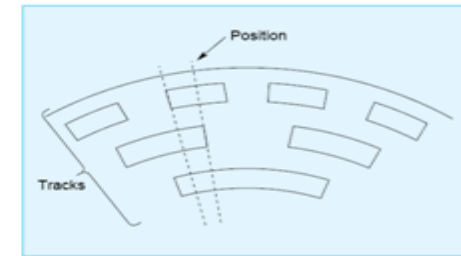
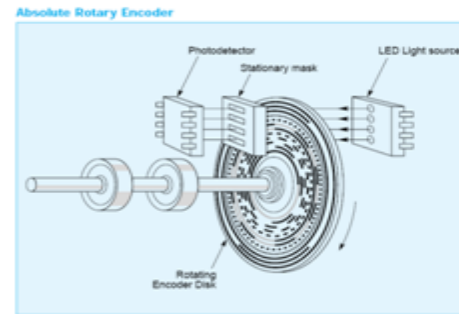
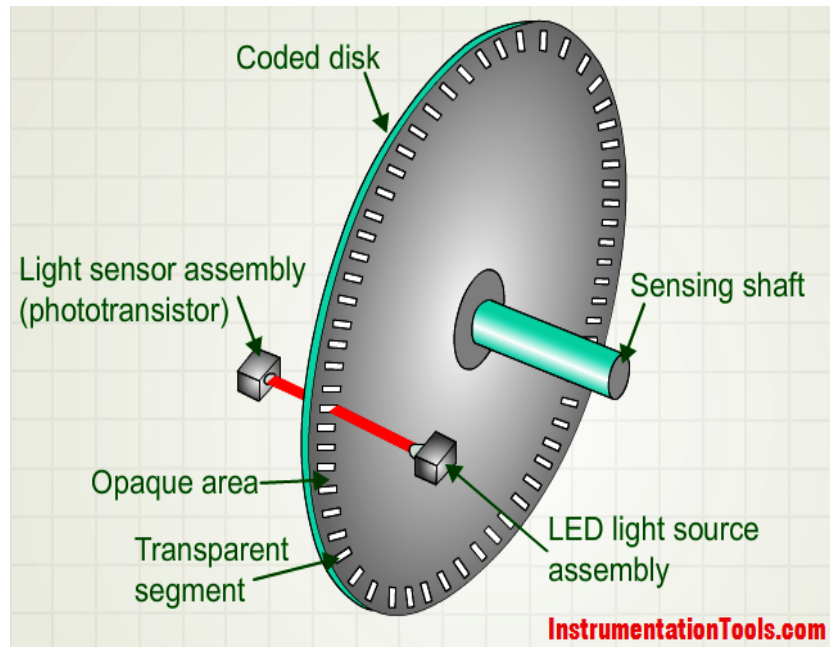
Sensor

- Hall sensor

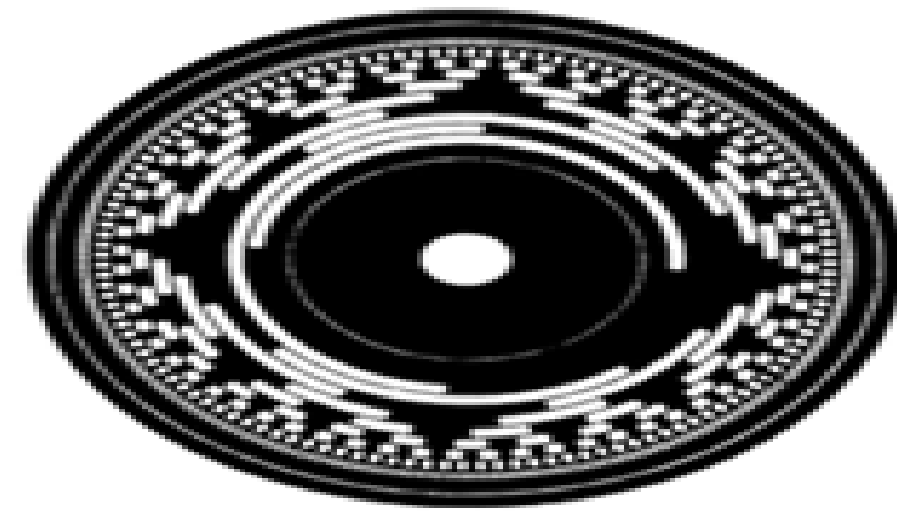


Sensor

- Rotor position sensor : Rotary Encoder



Typical disk pattern showing radial scanning method used to read position.



Encoder disk

Principle of Transistor

Figure1

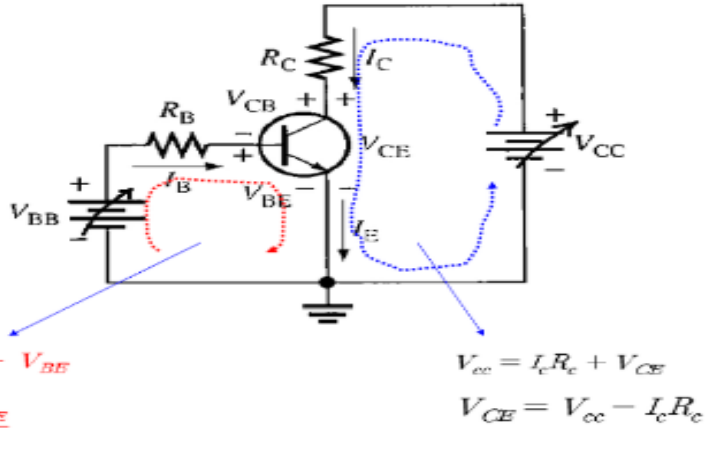
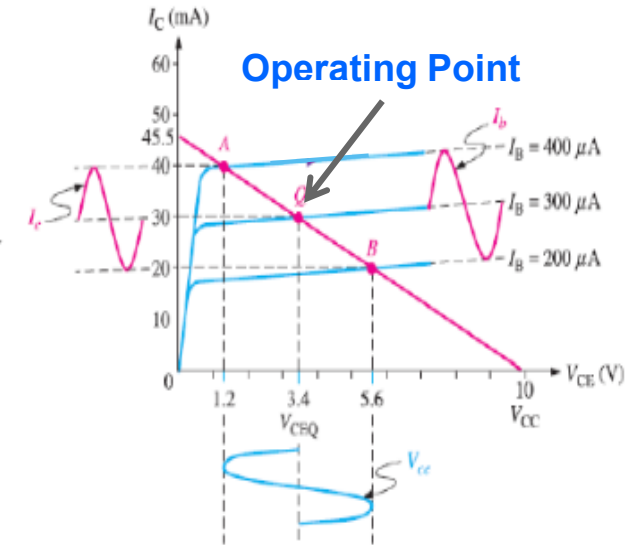
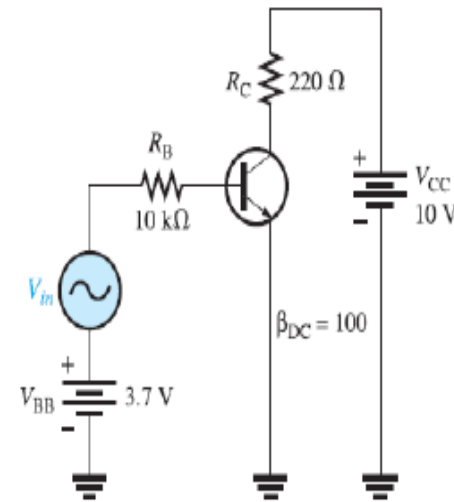


Figure2



Explain based on Figure 2. Set the I_B to $300\mu A$ and interpret it.

1) Flow $300\mu A$ of I_B in the circuit shown in Figure 2.

$$I_B = \frac{V_{BB} - V_{BE}}{R_B} = (3.7 - 0.7) \text{ V} / 10000 \text{ } \Omega = 0.0003 \text{ A} = 300\mu A$$

2) In Figure 2, increase the V_{CC} until I_C reaches 30mA.

As the I_C value increases, the V_{CE} value also increases linearly. (=resistance) resistance to $V_{CE} = 0.7 \text{ V} / 0.03 \text{ A} = 23.3 \text{ } \Omega$ (**Figure3 saturation region**) and $V_{CC} = V_{RC} + V_{CE} = 220 * 0.03 \text{ [V]} + 0.7 \text{ [V]} = 7.3 \text{ V}$

3) if $I_c = 10 \text{ mA} \rightarrow V_{CC} = V_{RC} + V_{CE} = 220 * 0.01 \text{ [V]} + 23.3 * 0.01 \text{ [V]} = 2.433 \text{ V}$

If $I_c = 20 \text{ mA} \rightarrow V_{CC} = V_{RC} + V_{CE} = 220 * 0.02 \text{ [V]} + 23.3 * 0.02 \text{ [V]} = 4.866 \text{ V}$

If $I_c = 30 \text{ mA} \rightarrow V_{CC} = V_{RC} + V_{CE} = 220 * 0.03 \text{ [V]} + 23.3 * 0.03 \text{ [V]} = 7.3 \text{ V}$

This means that the V_{CC} value up to 7.3 Volts increases the current linearly as voltage increases. (**Figure3 saturation region**)

4) If V_{CC} is increased by 7.3 volts or more

$$V_{CC} = V_{RC} + V_{CE}$$

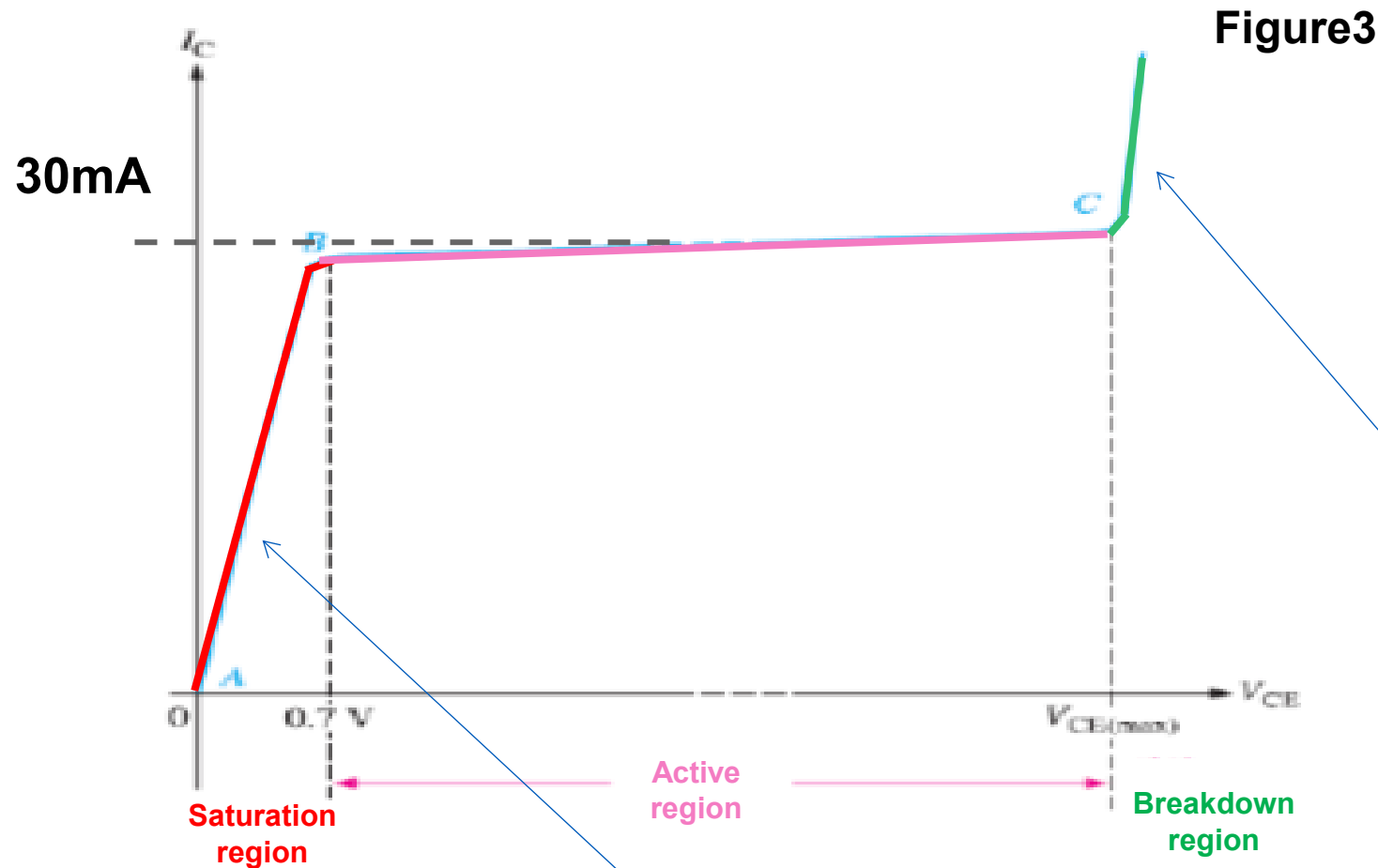
4-1) if $V_{CC} = 8 \text{ V} \rightarrow 8 \text{ V} = 220 * 0.03 \text{ V} + 1.4 \text{ V}$

4-2) if $V_{CC} = 9 \text{ V} \rightarrow 9 \text{ V} = 220 * 0.03 \text{ V} + 2.4 \text{ V}$

4-3) if $V_{CC} = 10 \text{ V} \rightarrow 10 \text{ V} = 220 * 0.03 \text{ V} + 3.4 \text{ V}$ (**Figure3 Active region**)

TR does amplification. In other words, we can get a large I_C (**30 mA**) by flowing a small I_B (**300μA**)

Principle of Transistor



The resistance is very low because it increases linearly very steeply.

The saturation area of the graph has a resistance component. This part corresponds to $0.7V / 0.03A = 23.3 \Omega$ in the preceding content and the larger the slope, the smaller the resistance.